

2D NMR

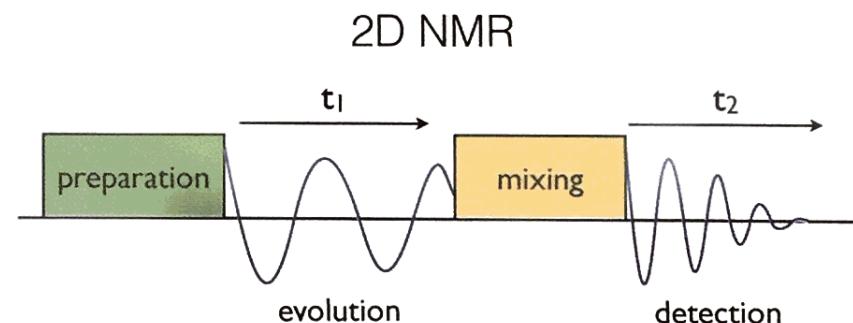
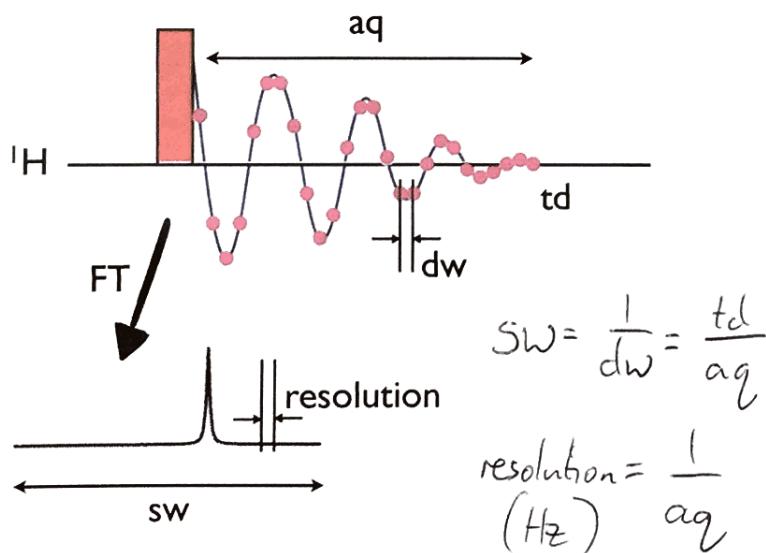
- Many spin systems and pulse sequences to choose between!
Focus on general aspects first...
- sw, td, aq
- Field strength, resolution and sensitivity

2D NMR

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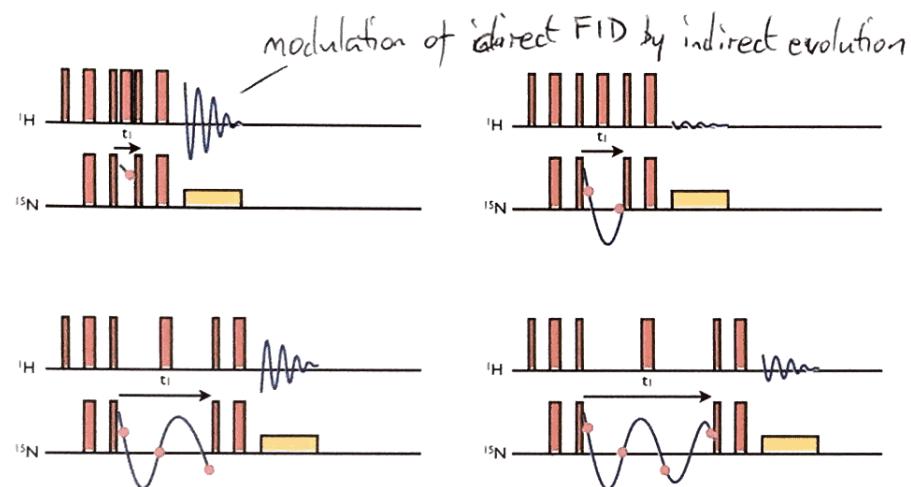
Recap: aq, td, sw and spectrum resolution



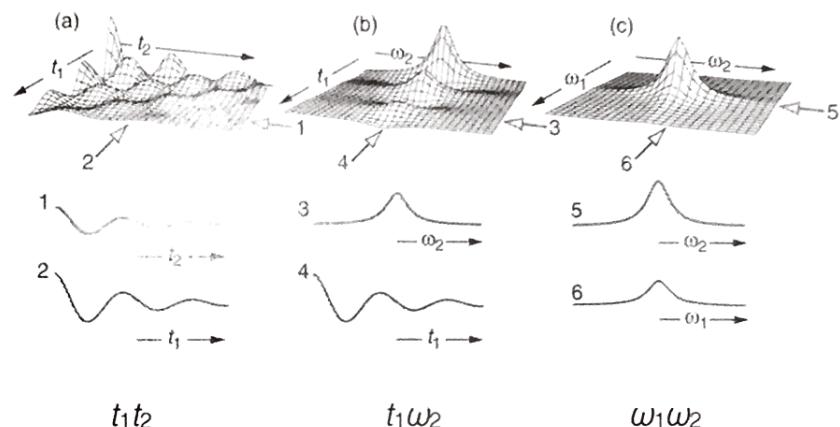
- Now we have two time dimensions
- Analysis of sw and resolution exactly the same as 1D
- Key difference from direct detection – long aq in t_1 isn't free!

(+ obvious extension to 3D etc.)

2D NMR

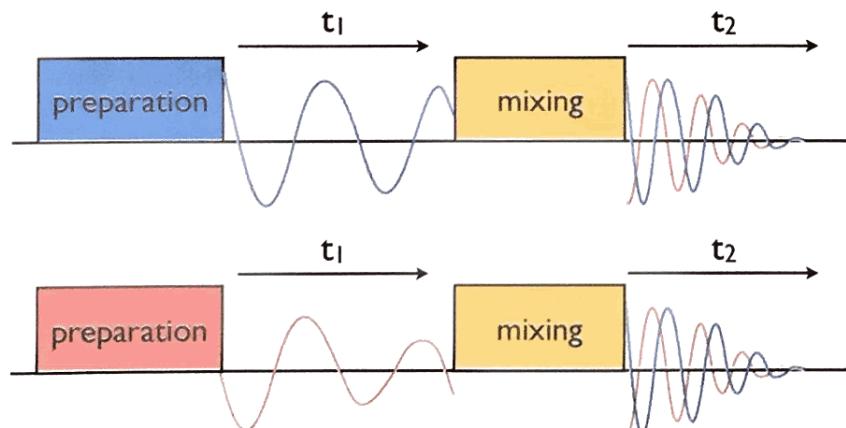


2D Fourier transformation



(Keeler, Understanding NMR Spectroscopy)

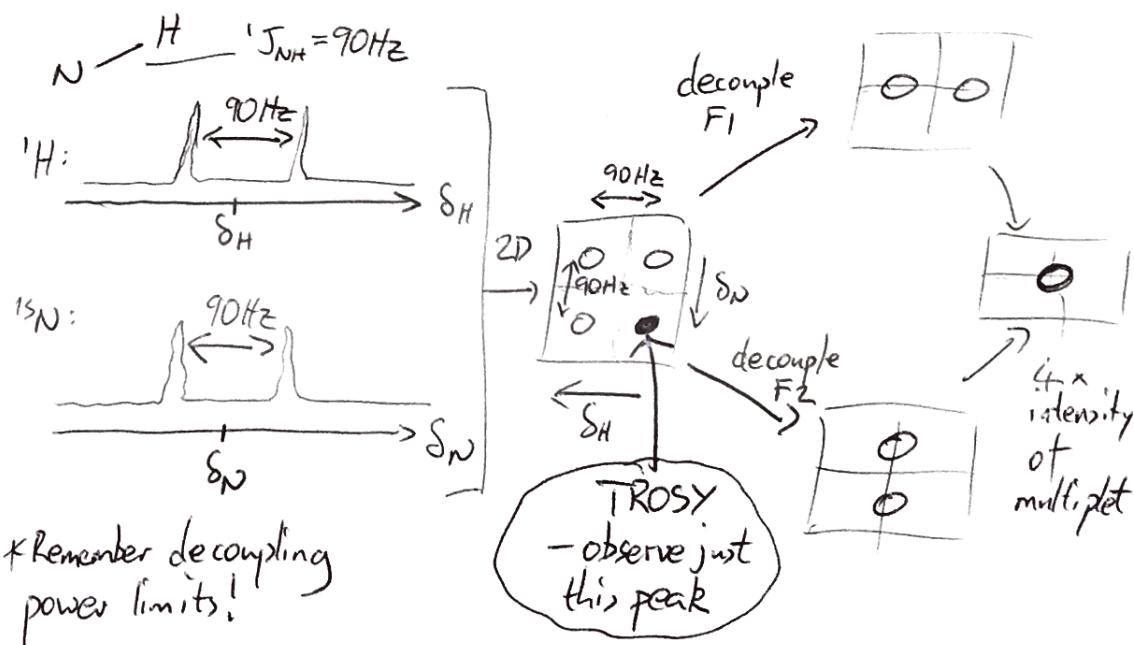
Quadrature detection in 2D



2 separate expts needed,
unlike direct dimension

hypercomplex data
(RR, RI, S
IR, II)

Multiplet structures



Resolution in the indirect dimension

$$SW(\text{Hz}) = \frac{\gamma B_0}{2\pi} \cdot SW(\text{ppm}) \times 10^{-6}$$

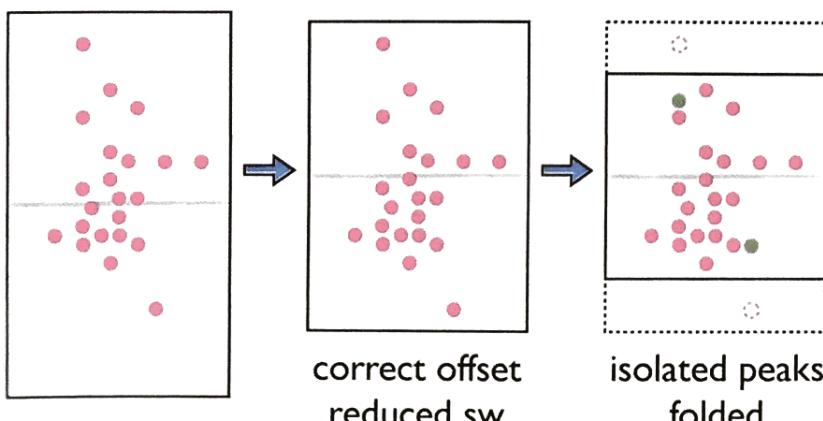
$$\Delta t = \frac{1}{SW(\text{Hz})} \propto \frac{1}{B_0} \quad \begin{matrix} \text{Stronger fields} \\ \Rightarrow \text{shorter delays} \end{matrix}$$

$$\text{resolution(Hz)} = \frac{1}{t_{\text{aq}}} = \frac{1}{N \cdot \Delta t} \propto \frac{SW(\text{ppm}) \cdot B_0}{N}$$

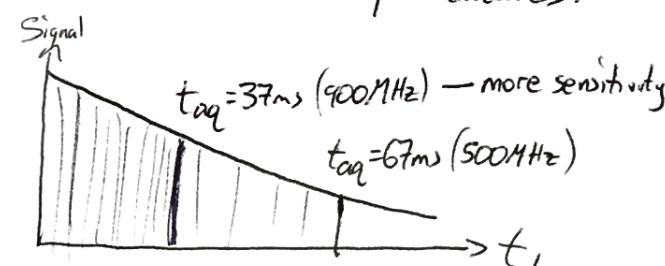
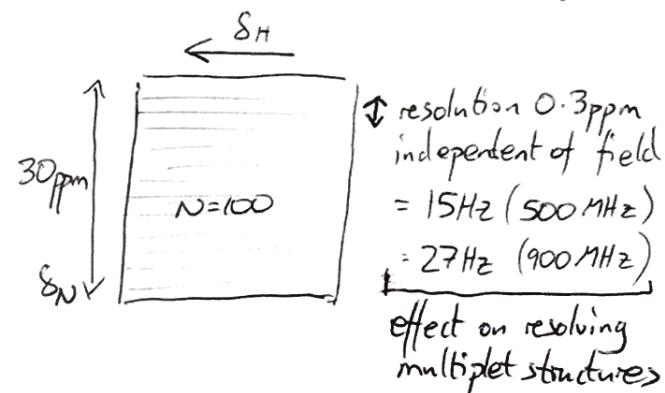
$$\text{resolution(ppm)} \propto \frac{SW(\text{ppm})}{N} \quad (\text{independent of } B_0)$$

Spectrum width in the indirect dimension: folding / aliasing

- Maximise resolution in indirect dimension by optimising the offset and minimising the spectrum width

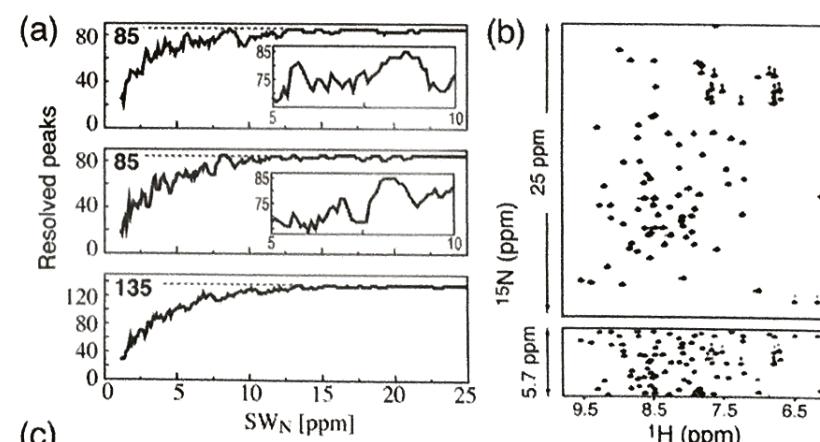


Resolution, sensitivity and field strength



Automated Spectral Compression for Fast Multidimensional NMR and Increased Time Resolution in Real-Time NMR Spectroscopy

Ewen Lescop, Paul Schanda, Rodolfo Rasia, and Bernhard Brügel*



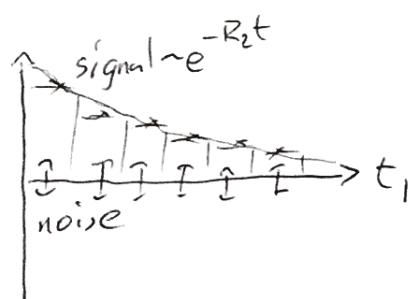
A bit extreme! but potentially useful
for fast kinetics, e.g. HD exchange

JACS 2007

Higher B_0 ,
fixed t_d and $sw(\text{ppm})$:

- same ppm resolution
- lower frequency resolution (Hz)
- higher sensitivity (on top of $B_0^{3/2}$ scaling)

Sensitivity



$$\text{signal} \propto \sum e^{-R_2 t_i} \approx \int_0^{T_{\text{tag}}} e^{-R_2 t} dt = \frac{1 - e^{-R_2 T_{\text{tag}}}}{R_2}$$

same amount of noise in each FID

$$\Rightarrow \text{noise} \propto \sqrt{T_{\text{tag}}}$$

$$\therefore \text{sensitivity} \propto \frac{1 - e^{-R_2 T_{\text{tag}}}}{R_2 \sqrt{T_{\text{tag}}}}$$

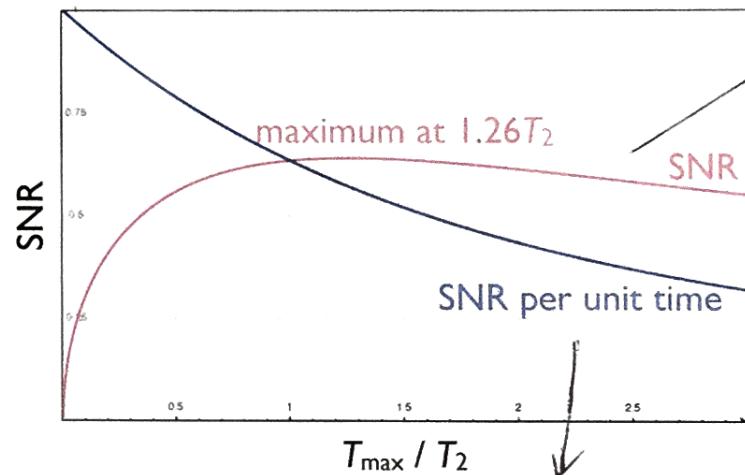
n.b. weird units $[\text{Hz}^{1/2}]$!

For fixed amount of wall-clock time:

$$\text{SNR} \propto \frac{1 - e^{-R_2 T_{\text{tag}}}}{R_2 T_{\text{tag}}}$$

2D experiments: COSY

Sensitivity → What question are you asking?



How do I get most signal in fixed amount of time?
- trade off with resolution

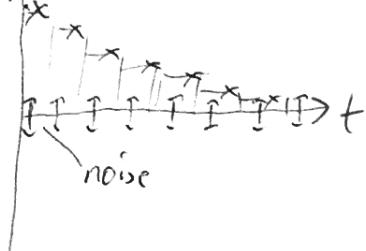
2D experiments: NOESY

Sample is stable - will SNR improve if I record longer evolution times?

Sensitivity

on-resonance ($\omega = 0$):

$$\text{signal} \propto \sum e^{-R_2 t} \approx \int_0^{t_{\text{tag}}} e^{-R_2 t} dt = \frac{1 - e^{-R_2 t_{\text{tag}}}}{R_2}$$

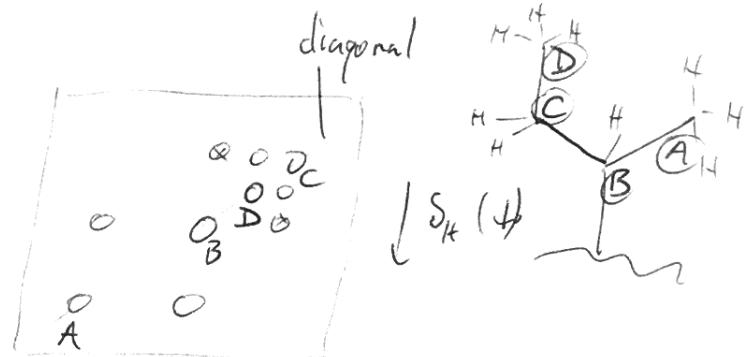
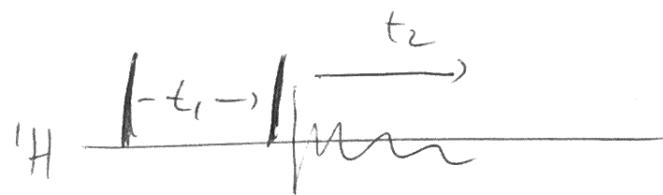


same amount of noise in each FID
 $\Rightarrow \text{noise} \propto \sqrt{t_{\text{tag}}}$

$$\therefore \text{sensitivity} \propto \frac{1 - e^{-R_2 t_{\text{tag}}}}{R_2 \sqrt{t_{\text{tag}}}} \quad (\text{NIB units: } s^{-1/2})$$

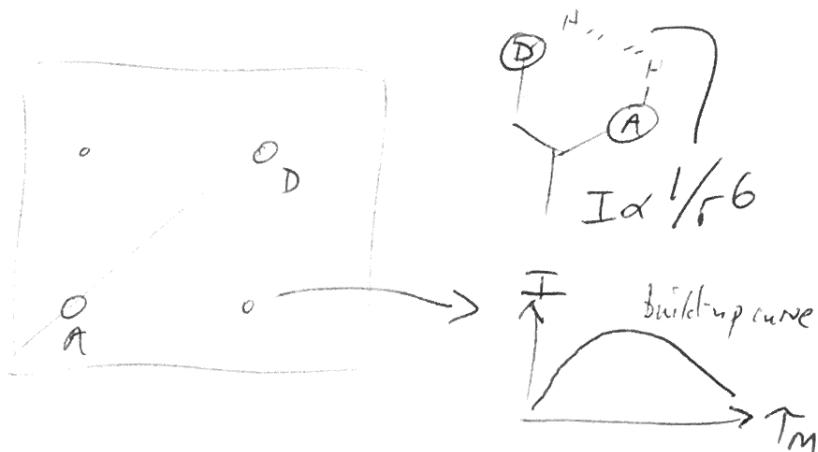
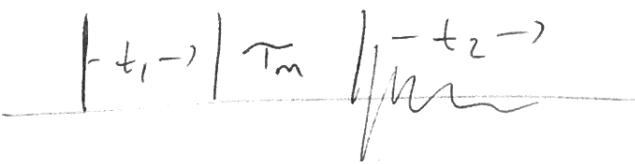
$$\text{For fixed amount of wall-clock time: } \text{SNR} \propto \frac{1 - e^{-R_2 t_{\text{tag}}}}{R_2 t_{\text{tag}}}$$

COSY

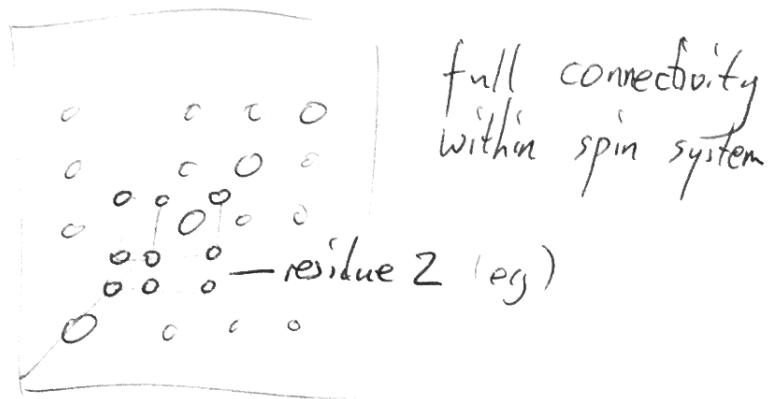
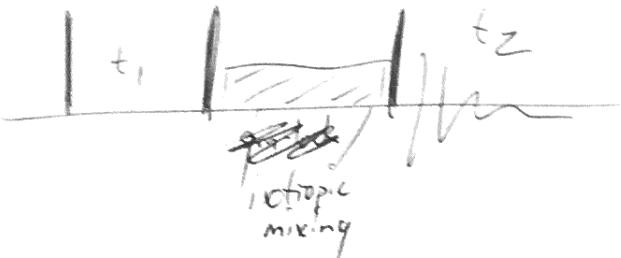


$$\xleftarrow{\quad} S_H (4) \xrightarrow{\quad}$$

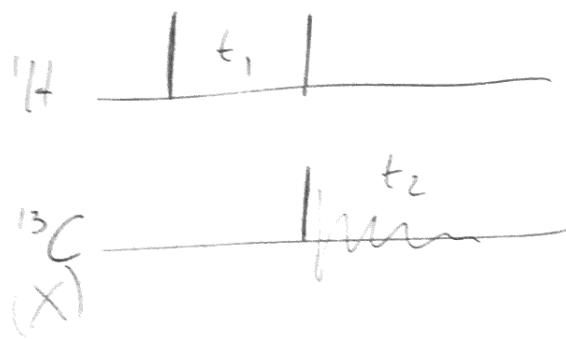
NOESY



TOCSY



HETCOR



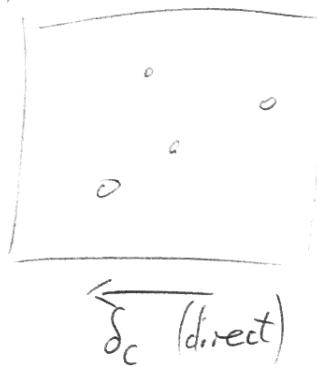
$^1\text{H} \rightarrow ^{13}\text{C} \rightarrow \text{detect}$

(X)

$$\text{SNR} \propto \gamma_{\text{ex}} \gamma_{\text{obs}}^{3/2}$$

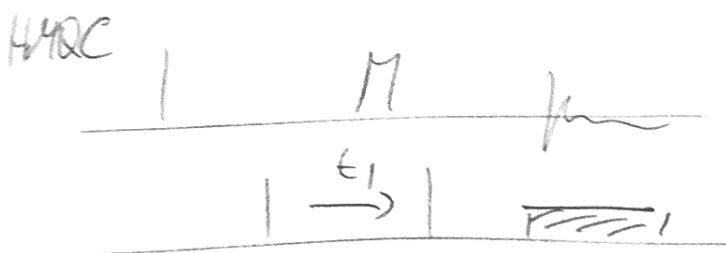
\Rightarrow better than direct detection

δ_{H} (indirect)



δ_c (direct)

HMQC / HSQC

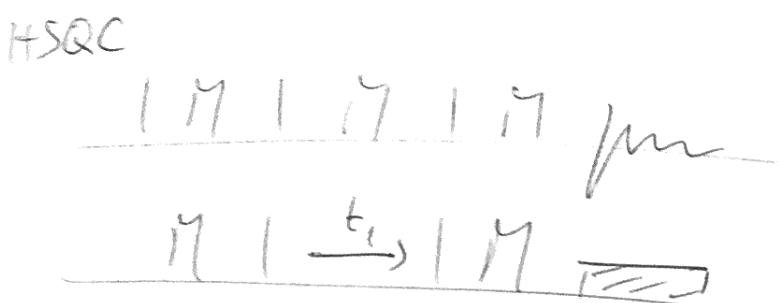


$^1\text{H} \rightarrow X \rightarrow ^1\text{H}$

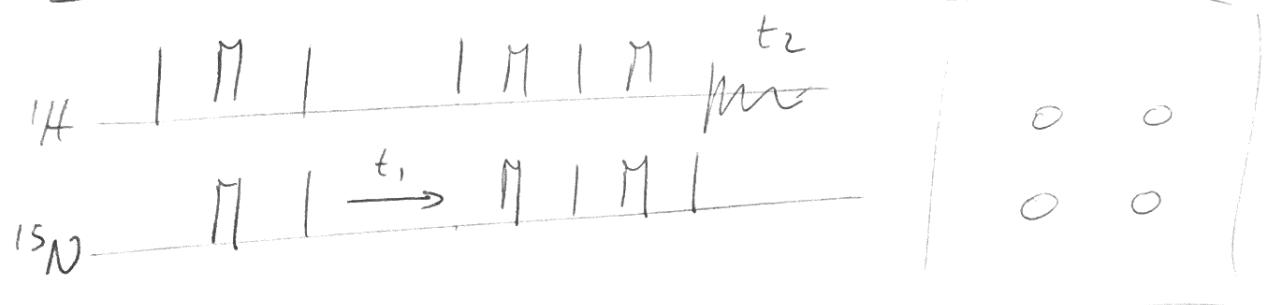
$$\text{SNR} \propto \gamma_{\text{ex}} \gamma_{\text{obs}}^{3/2}$$

$$\gamma_{\text{H}}/\gamma_{\text{C}} = 4 \Rightarrow 500 \times$$

$$\gamma_{\text{H}}/\gamma_{\text{N}} = 10 \Rightarrow 50,000 \times$$



TROSY



25% of signal - but ∇R_2

