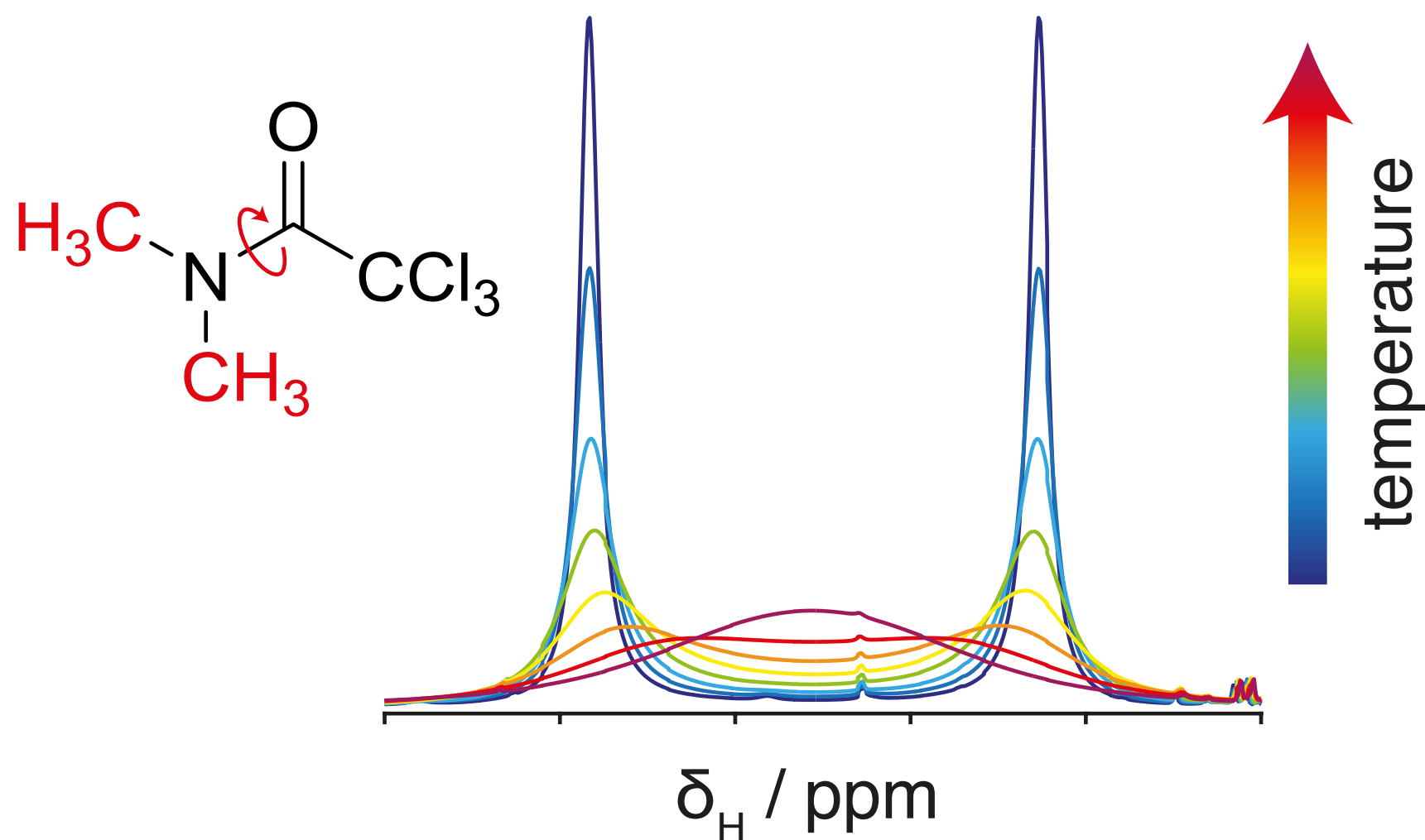


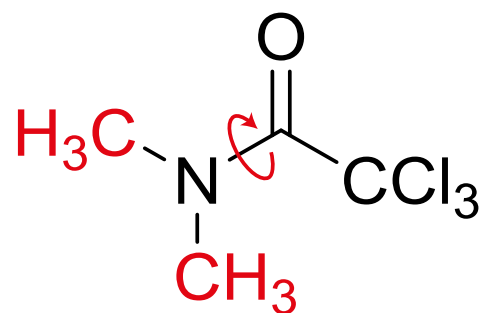
Chemical Exchange

Chris Waudby

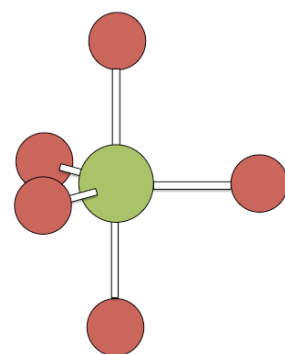
www.waudbylab.org



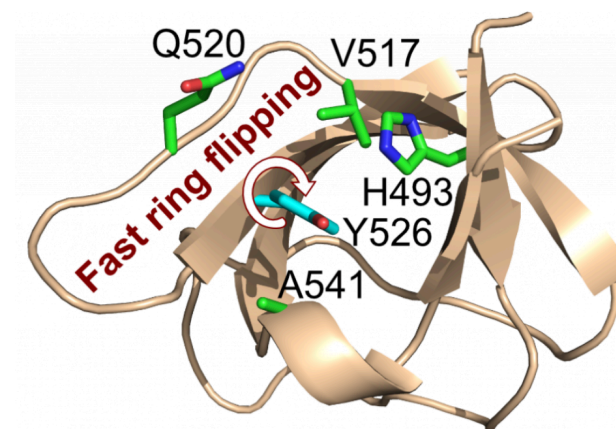
Chemical exchange is everywhere!



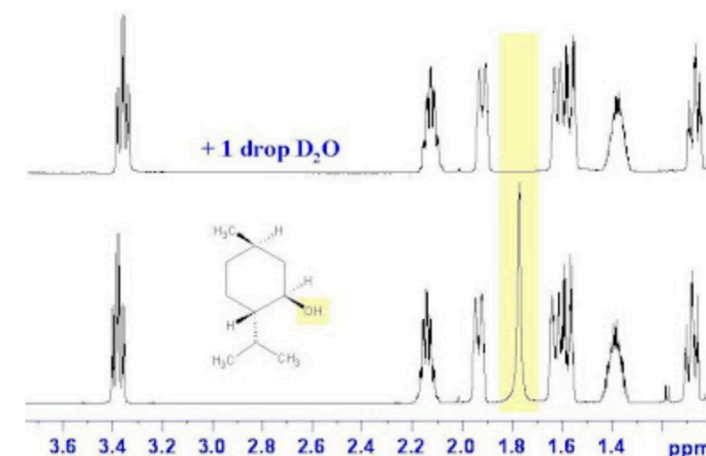
bond rotation



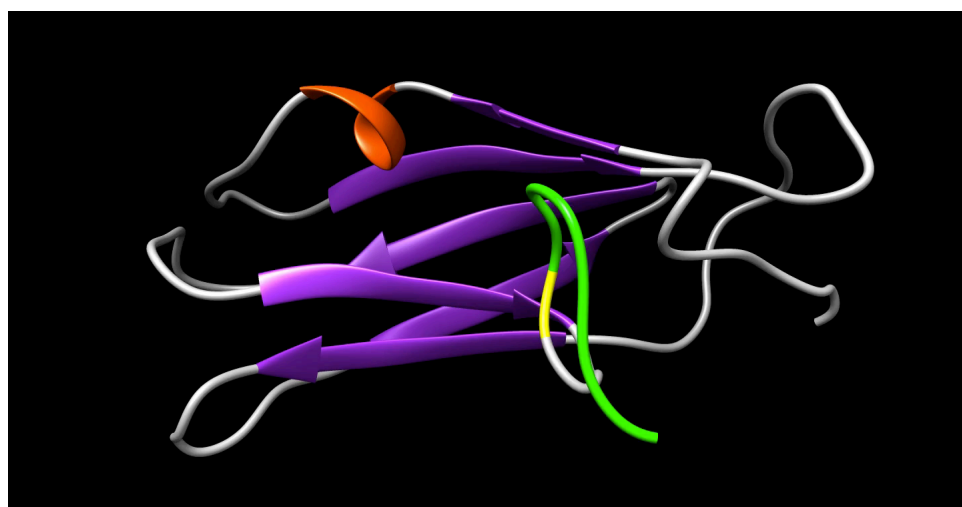
fluxionality



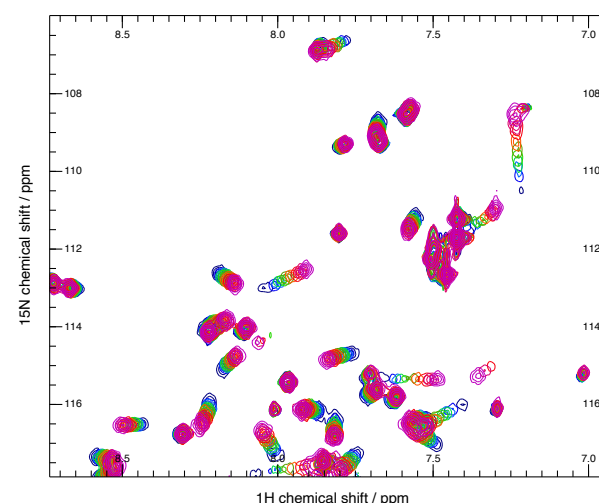
ring flips



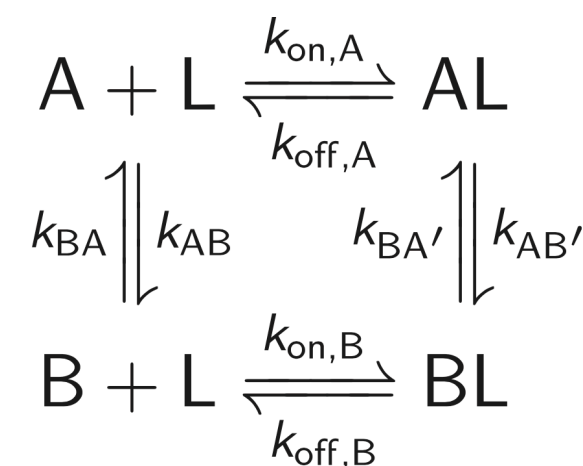
hydrogen exchange



protein folding, unfolding and intermediate formation

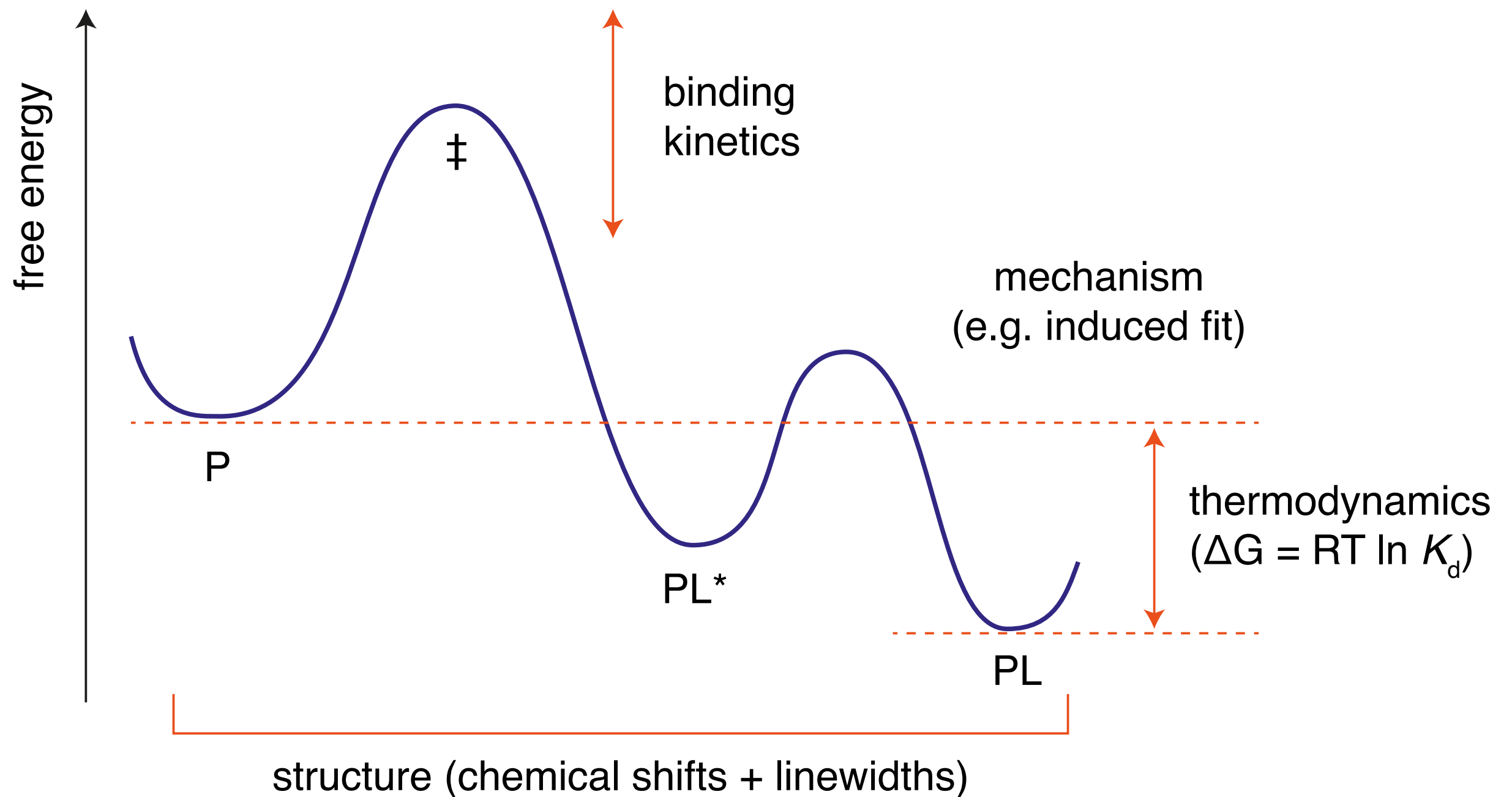


ligand binding / host-guest recognition



allostery

What information can NMR provide?



A note on units

linear frequencies = 2π x angular frequencies

measured in **Hz**
(cycles per second = $1 / \text{period}$)

usually written as **ν , $\Delta\nu$**

relaxation rates (R_1 , R_2) are
not measured in Hz and
cannot be compared with
angular frequency differences

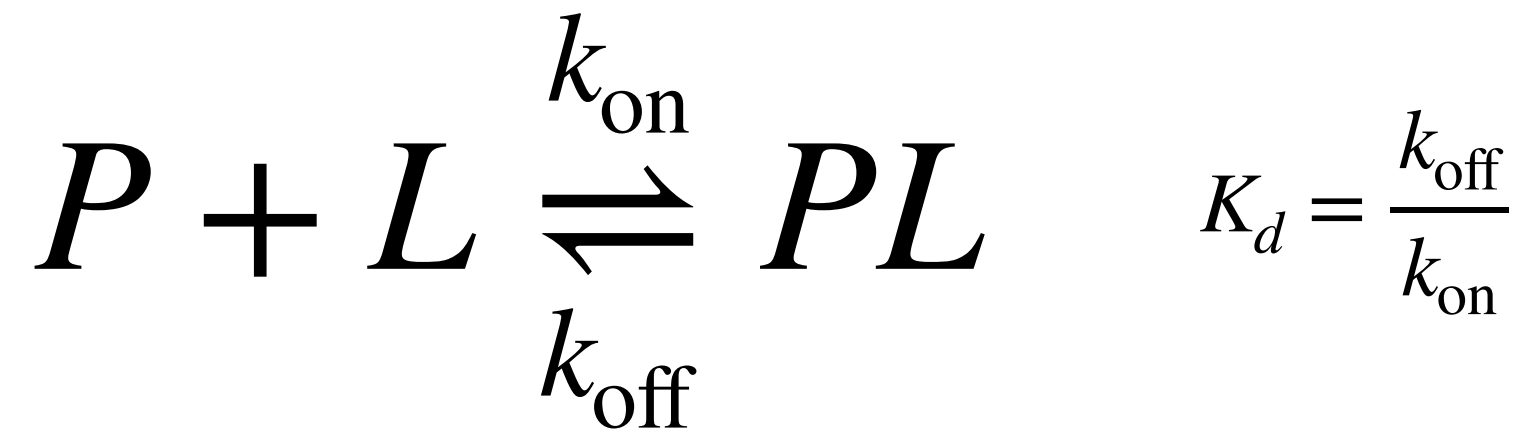
first-order rate constants (e.g. k_{off} , k_{ex})
are **not** measured in Hz and **cannot**
be compared with angular frequency
differences

measured in **s^{-1}**
(**rad s^{-1}** , but radians are implicit)

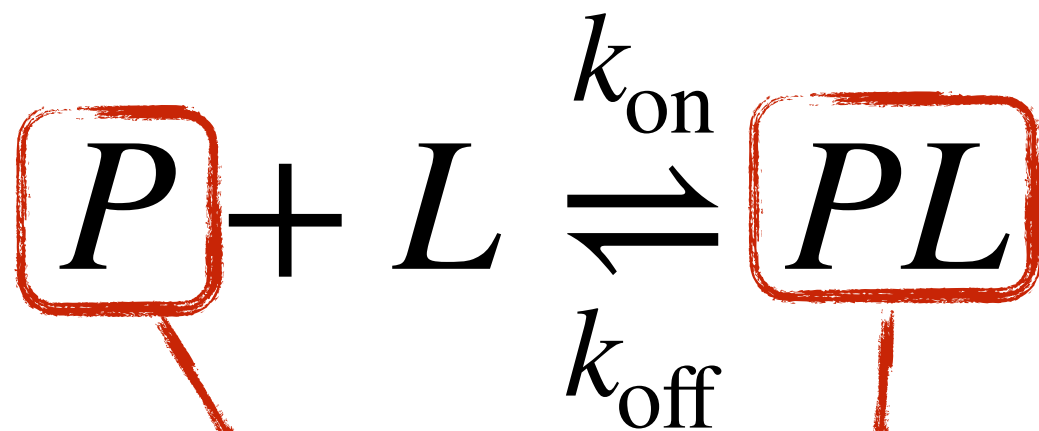
usually written as **ω , $\Delta\omega$**

**relaxation rates (R_1 , R_2) are
also measured in s^{-1}** and can
be compared with angular
frequency differences

**first-order rate constants (e.g. k_{off} ,
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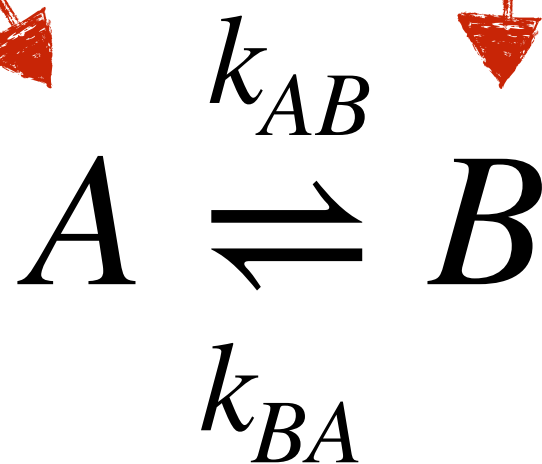


Molecules:

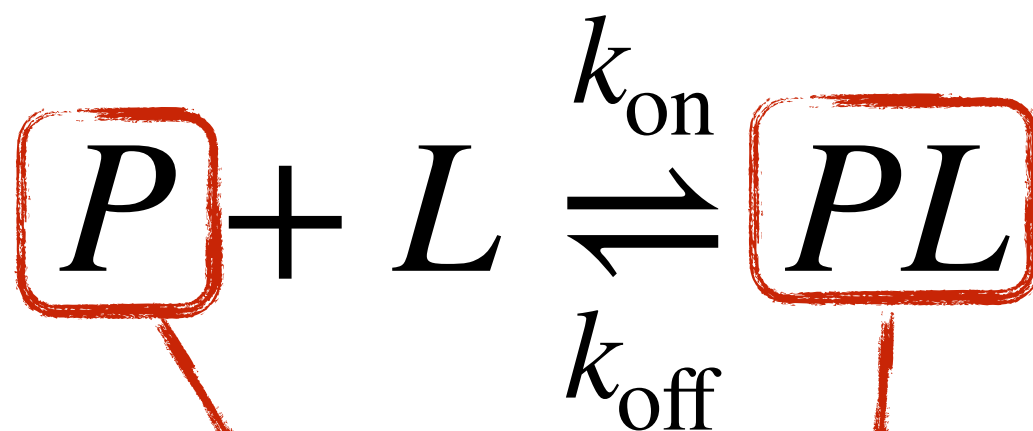


$$K_d = \frac{k_{\text{off}}}{k_{\text{on}}}$$

'P' nuclei:

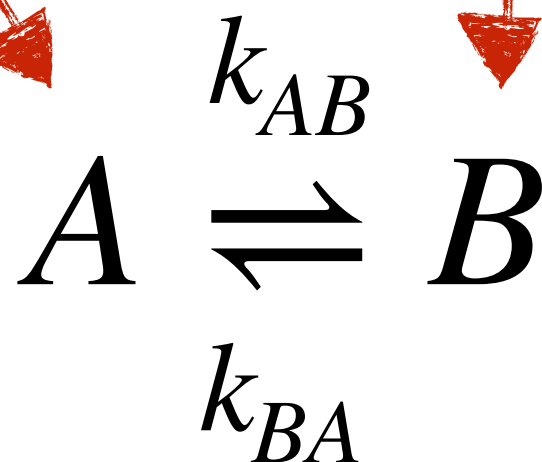


Molecules:



$$K_d = \frac{k_{\text{off}}}{k_{\text{on}}}$$

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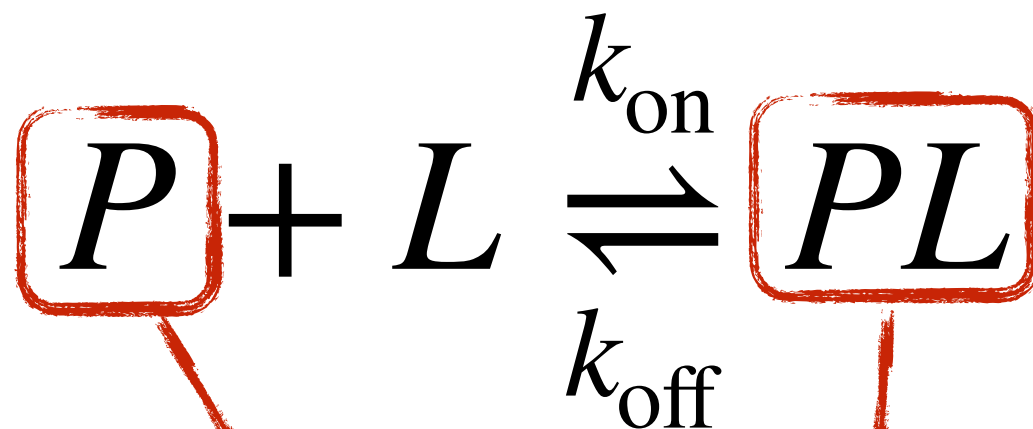


$$k_{AB} = k_{\text{on}}[L]$$

$$k_{BA} = k_{\text{off}}$$

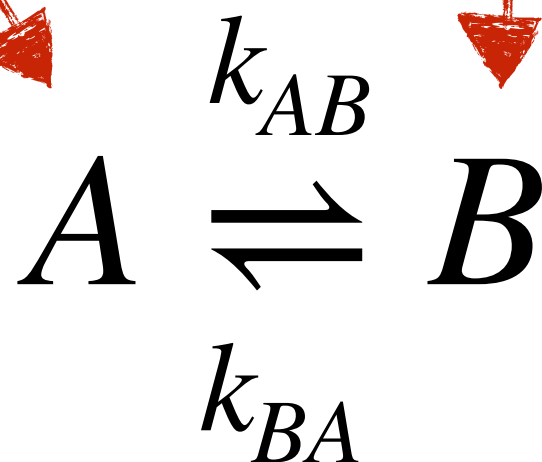
$$L = \frac{1}{2} \left[L_0 - P_0 - K_d + \sqrt{(L_0 + P_0 + K_d)^2 - 4P_0L_0} \right]$$

Molecules:



$$K_d = \frac{k_{\text{off}}}{k_{\text{on}}}$$

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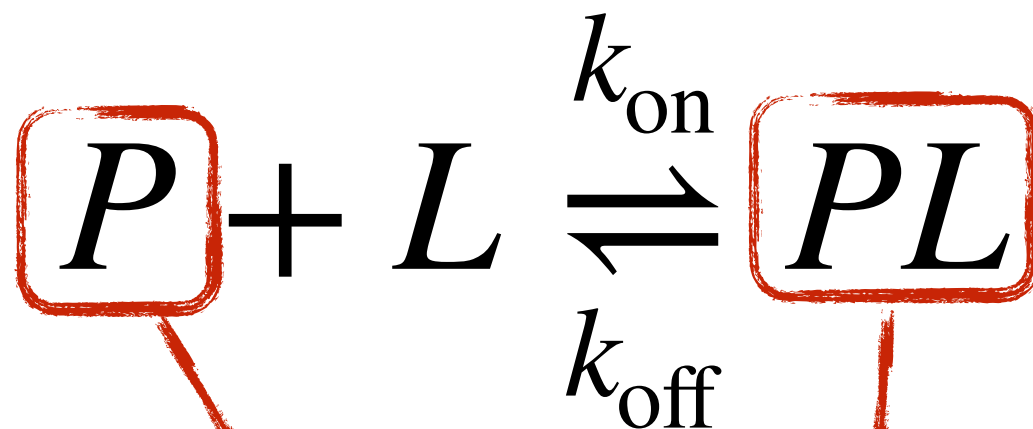
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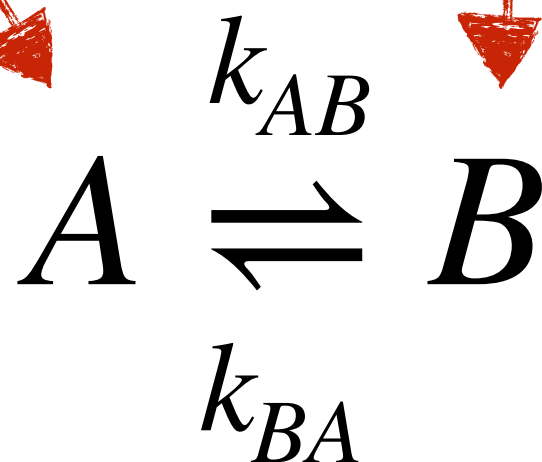
At dynamic equilibrium, chemical exchange processes are **always** first order (because perturbations from fluctuations are small)

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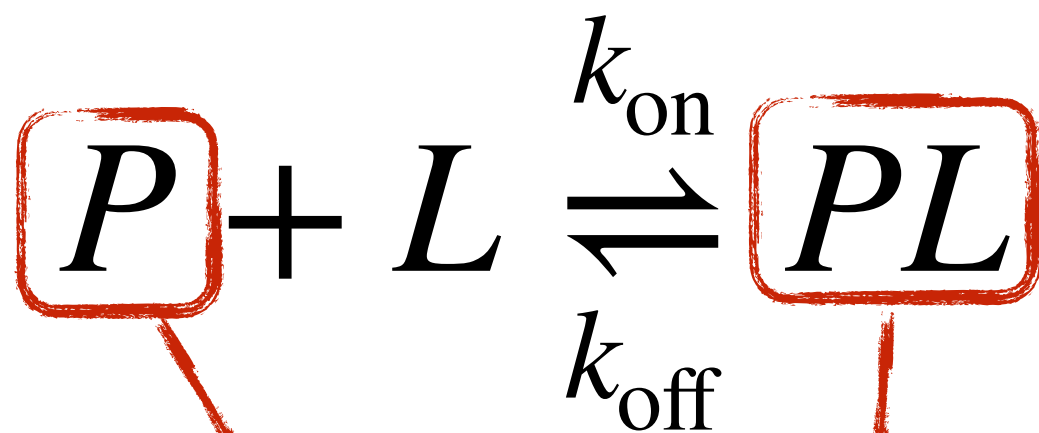
$$L = \frac{1}{2} \left[L_0 - P_0 - K_d + \sqrt{(L_0 + P_0 + K_d)^2 - 4P_0L_0} \right]$$

Equilibrium populations:

$$p_A = \frac{k_{BA}}{k_{AB} + k_{BA}} \quad p_B = \frac{k_{AB}}{k_{AB} + k_{BA}}$$

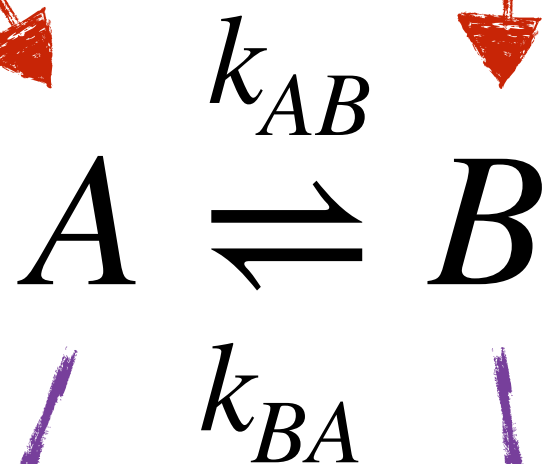
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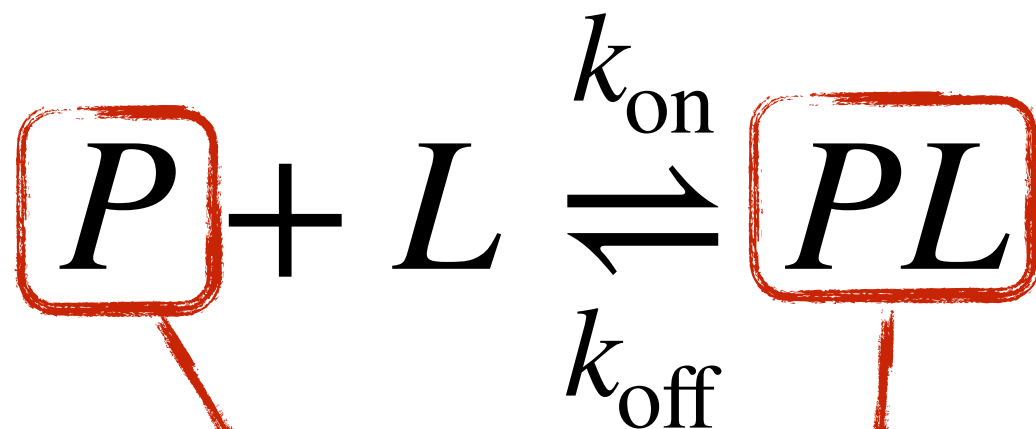
'P' nuclei:



$$\omega_A, R_{2,A}$$

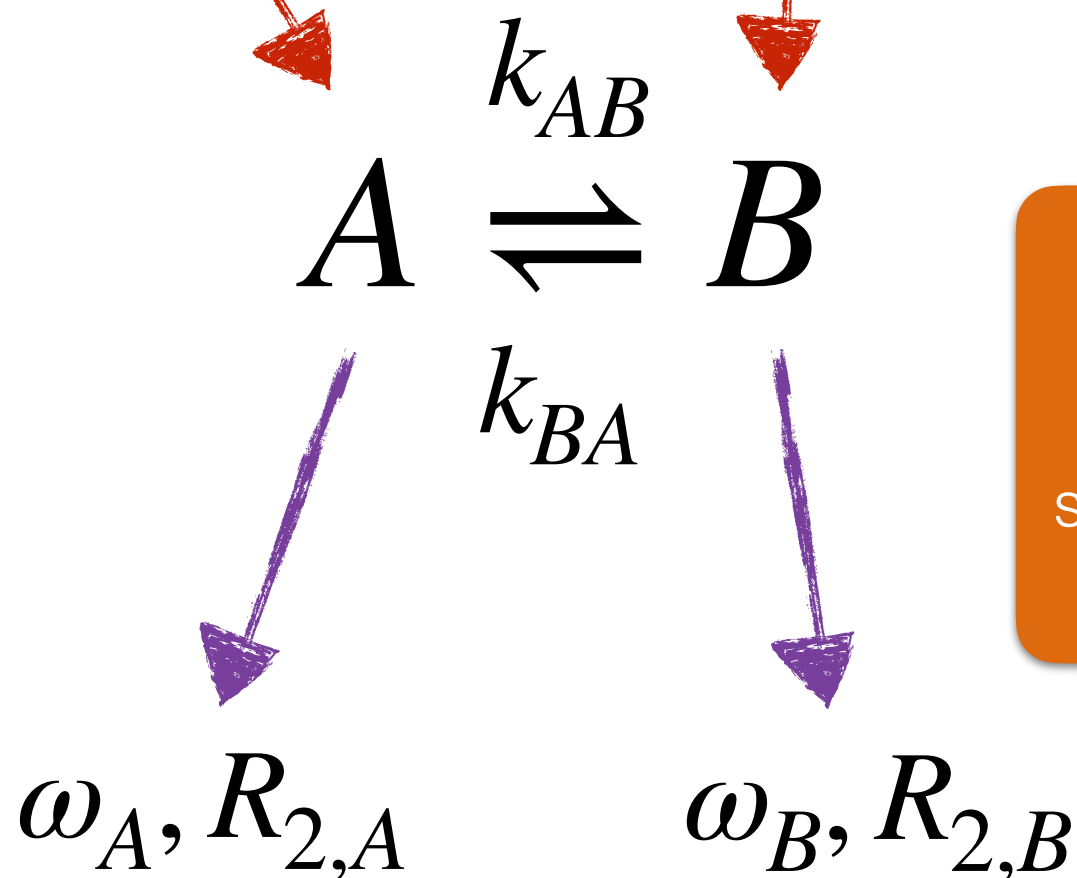
$$\omega_B, R_{2,B}$$

Molecules:



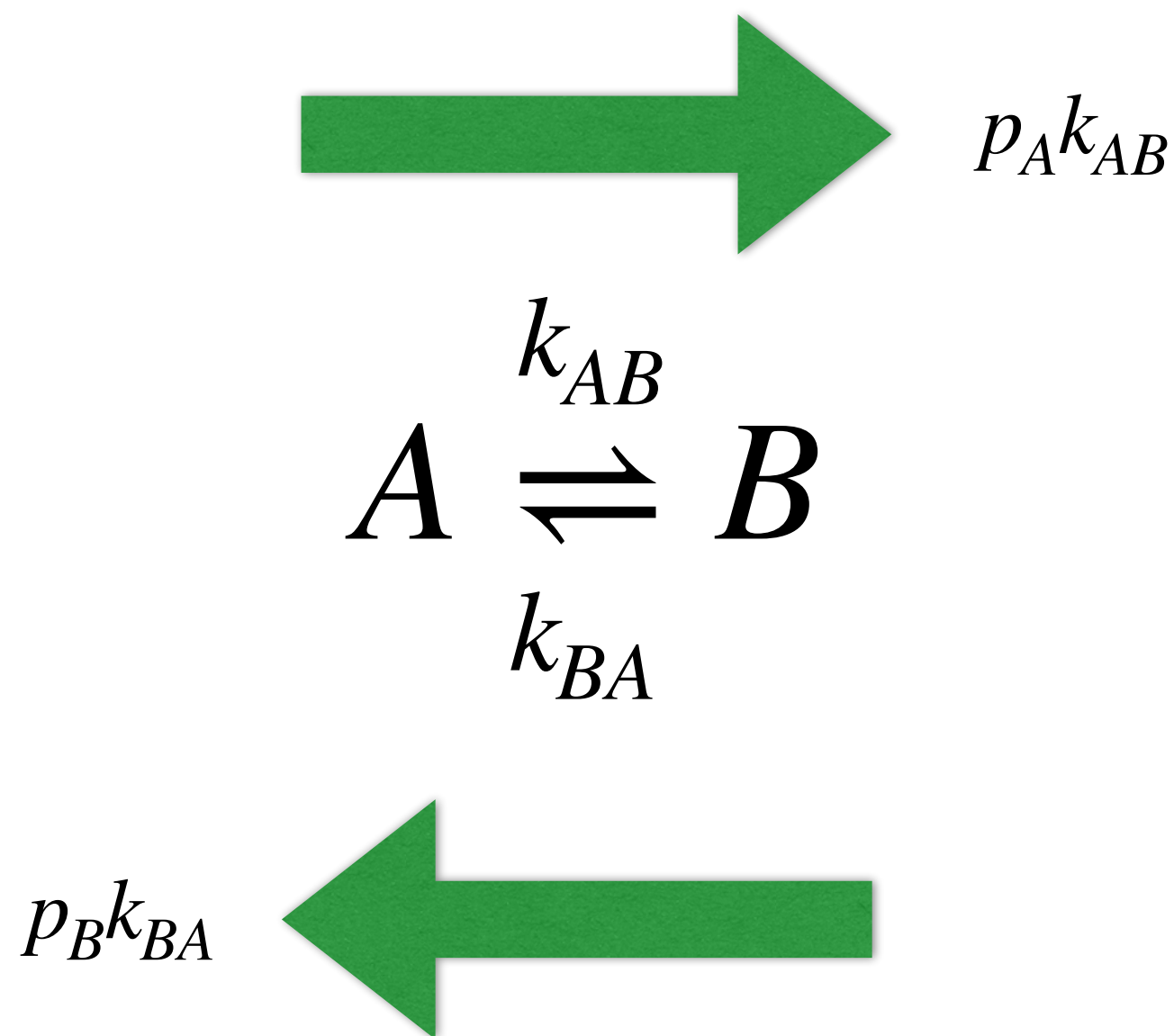
$$K_d = \frac{k_{\text{off}}}{k_{\text{on}}}$$

'P' nuclei:

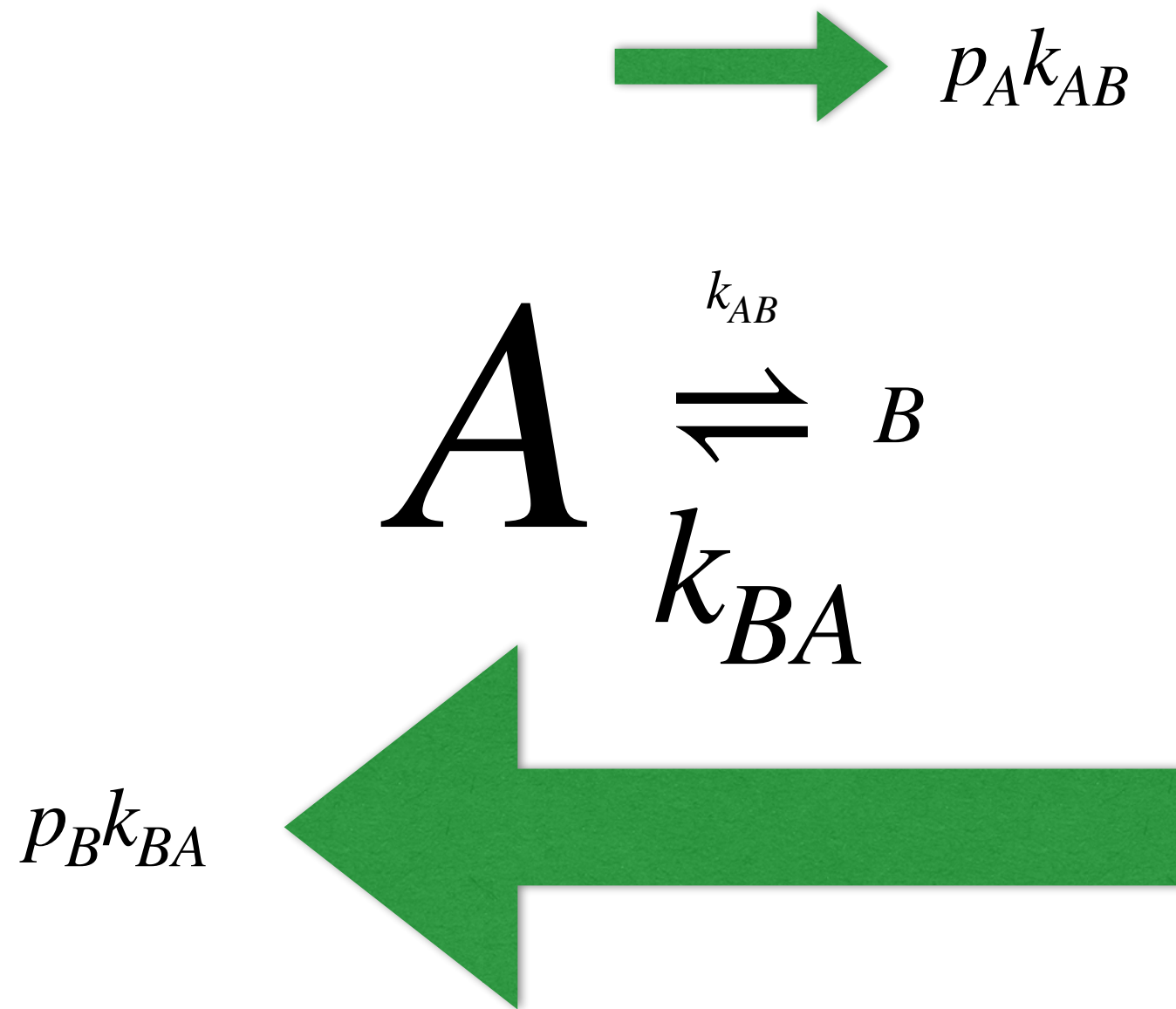


N.B. states are a global property
every spin in a molecule will exist in states A and B – but the difference in chemical shifts may be negligible

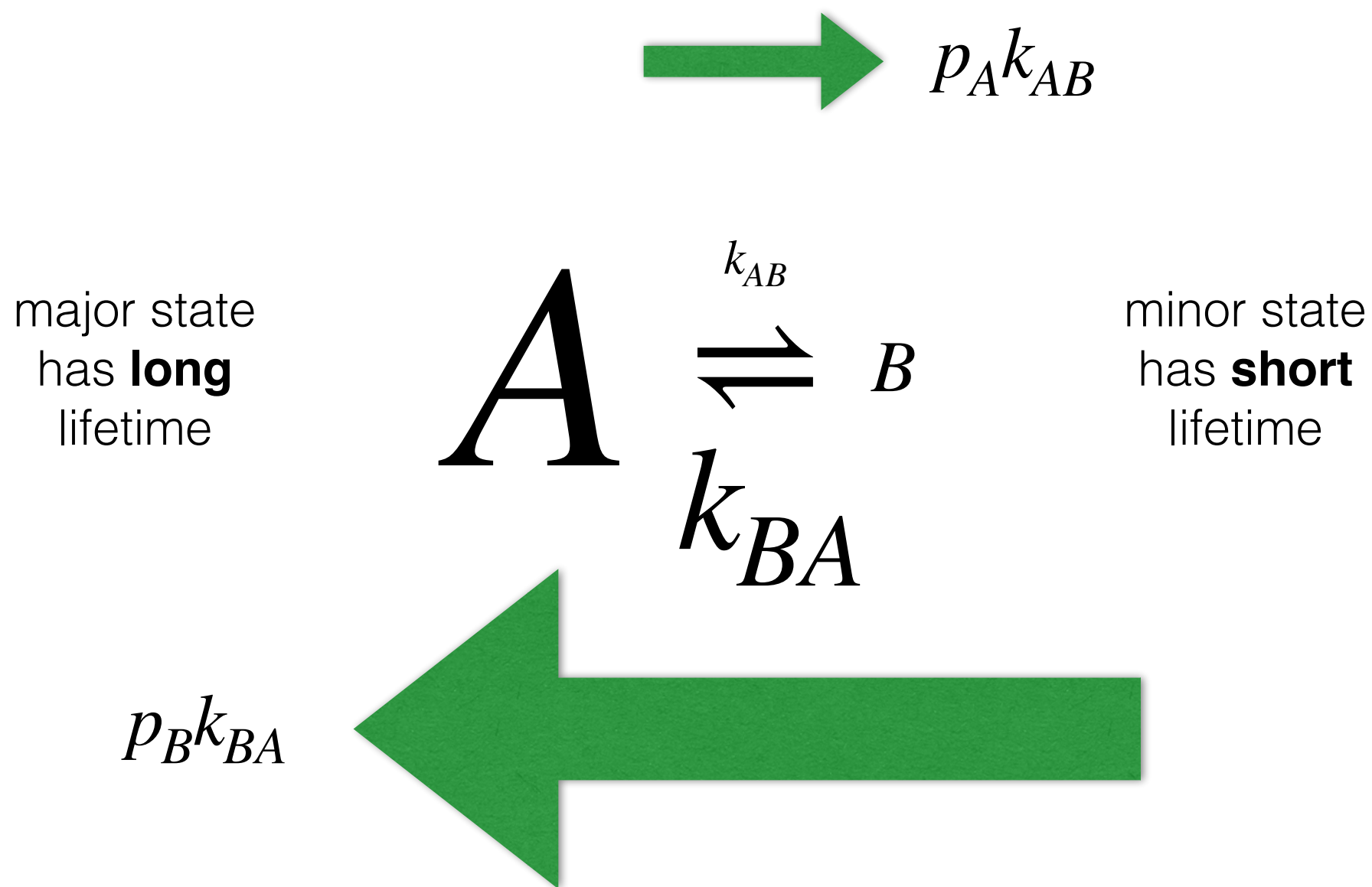
Forward and backward flux is equal at dynamic equilibrium



Forward and backward flux is equal at dynamic equilibrium

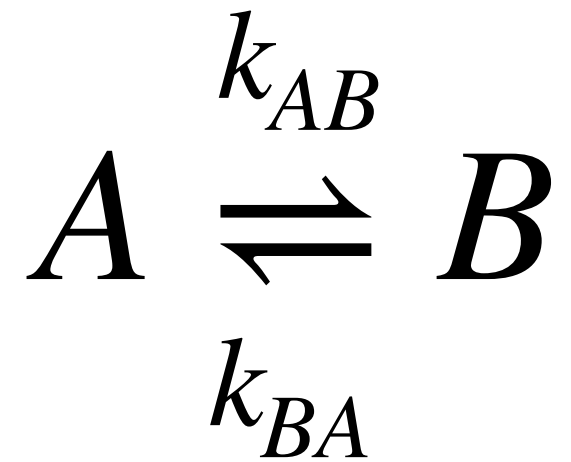


Forward and backward flux is equal at dynamic equilibrium



Chemical exchange kinetics at dynamic equilibrium

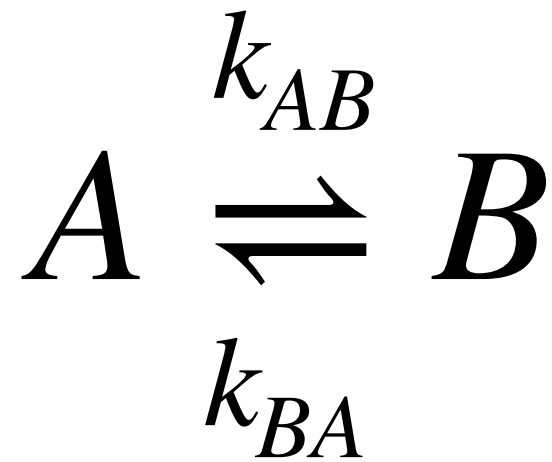
We can write the rate equations:



$$\frac{dA}{dt} = -k_{AB}A + k_{BA}B$$

$$\frac{dB}{dt} = k_{AB}A - k_{BA}B$$

Chemical exchange kinetics at dynamic equilibrium



We can write the rate equations:

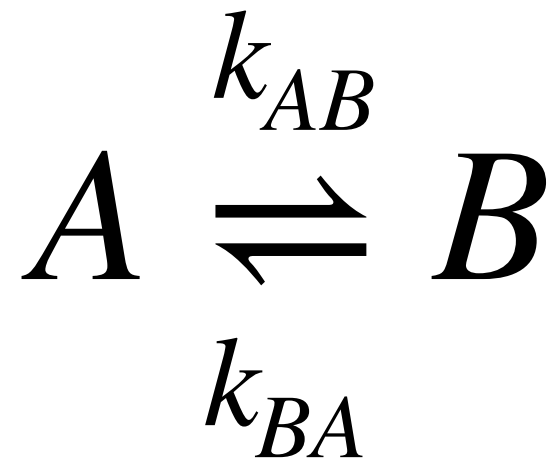
$$\frac{dA}{dt} = -k_{AB}A + k_{BA}B$$

$$\frac{dB}{dt} = k_{AB}A - k_{BA}B$$

Or more compactly using matrix notation:

$$\frac{d\vec{M}}{dt} = \frac{d}{dt} \begin{pmatrix} A \\ B \end{pmatrix} = \begin{pmatrix} -k_{AB} & k_{BA} \\ k_{AB} & -k_{BA} \end{pmatrix} \cdot \begin{pmatrix} A \\ B \end{pmatrix} = K \cdot \vec{M}$$

Chemical exchange kinetics at dynamic equilibrium



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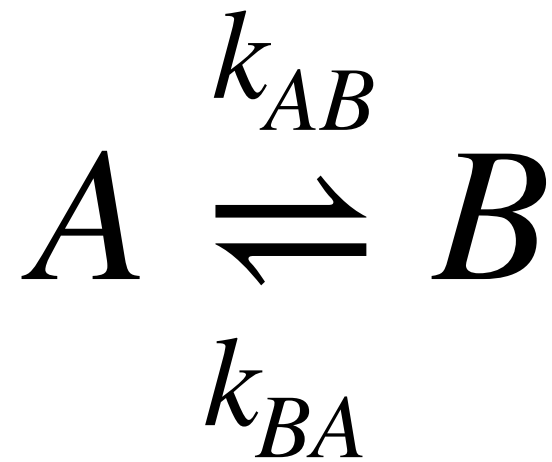
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The solution to this is:

$$\vec{M}(t) = e^{Kt} \cdot \vec{M}(0)$$

K is the **exchange operator** (or superoperator if you're being fancy!)

Eigenvalues of the exchange operator



The exchange operator, \mathbf{K} :

$$K = \begin{pmatrix} -k_{AB} & k_{BA} \\ k_{AB} & -k_{BA} \end{pmatrix}$$

has two eigenvalues:

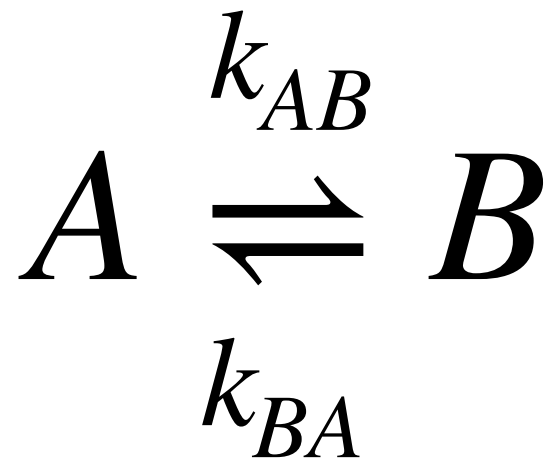
$$\lambda = \{0, k_{AB} + k_{BA}\}$$

These represent the chemical relaxation rates of the system (*i.e. the rates of return to equilibrium following a perturbation*)

One eigenvalue is always zero – this just represents the equilibrium state that does not change over time

The second eigenvalue is often referred to as the exchange rate, $k_{\text{ex}} = k_{AB} + k_{BA}$.

Eigenvalues of the exchange operator



The exchange operator, \mathbf{K} :

$$K = \begin{pmatrix} -k_{AB} & k_{BA} \\ k_{AB} & -k_{BA} \end{pmatrix}$$

Knowledge of the exchange rate is critical to understanding chemical exchange in NMR: It is the quantity against which differences in spectroscopic parameters are compared in order to define fast, intermediate and slow exchange regimes

One eigenvalue is always zero – this just represents the equilibrium state that does not change over time

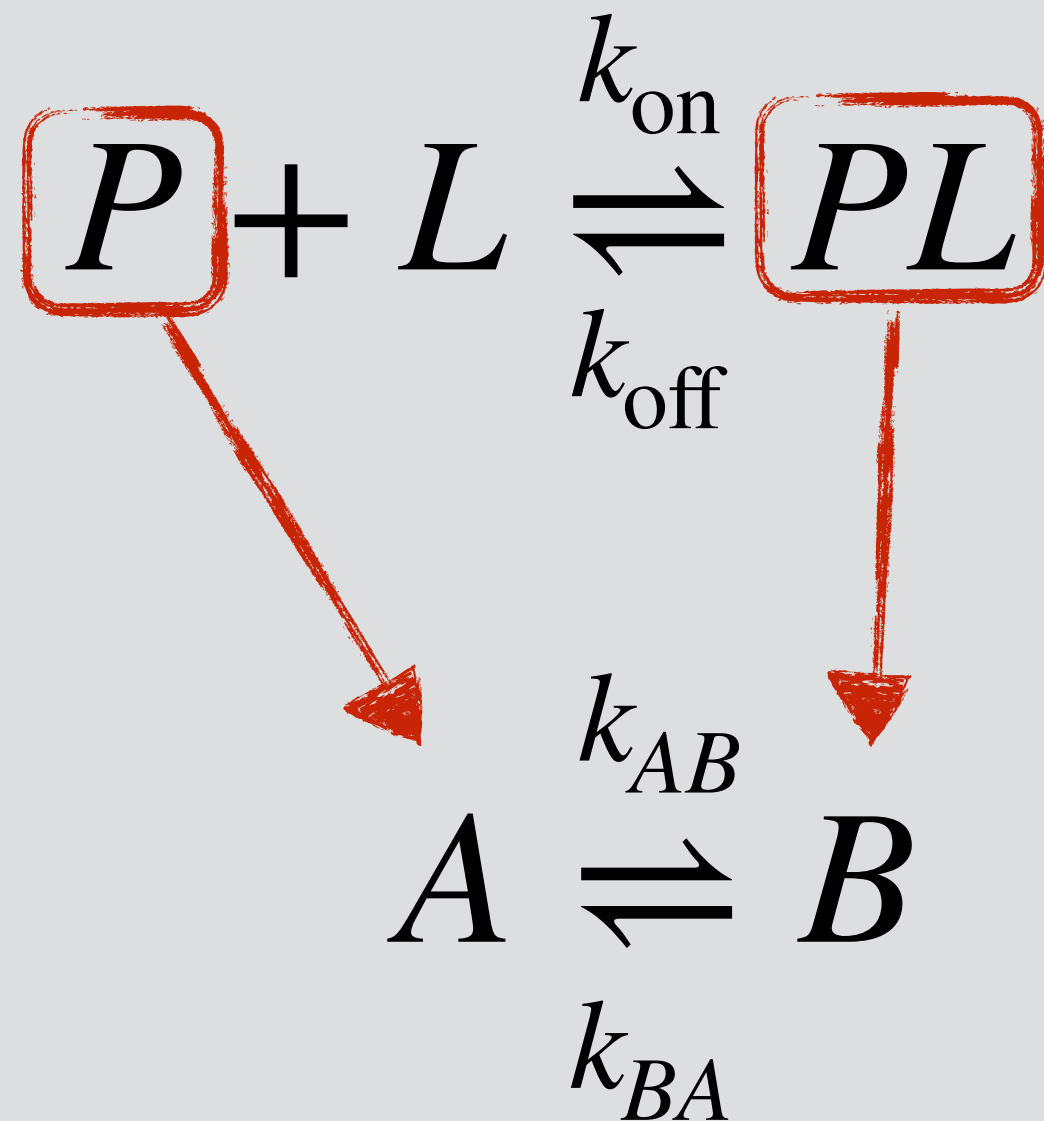
The second eigenvalue is often referred to as the exchange rate, $k_{\text{ex}} = k_{AB} + k_{BA}$.

Example

$$\begin{aligned}k_{\text{ex}} &= k_{AB} + k_{BA} \\ &= k_{\text{on}}[L] + k_{\text{off}}\end{aligned}$$

e.g. $K_d = 20 \mu\text{M}$
 $k_{\text{off}} = 1000 \text{ s}^{-1}$
 $\Rightarrow k_{\text{on}} = 5 \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$

$[P]_0 = 100 \mu\text{M}$
 $[L]_0 = 50 \mu\text{M}$



$$k_{AB} = k_{\text{on}}[L]$$

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$$L = \frac{1}{2} \left[L_0 - P_0 - K_d + \sqrt{(L_0 + P_0 + K_d)^2 - 4P_0L_0} \right]$$

Example

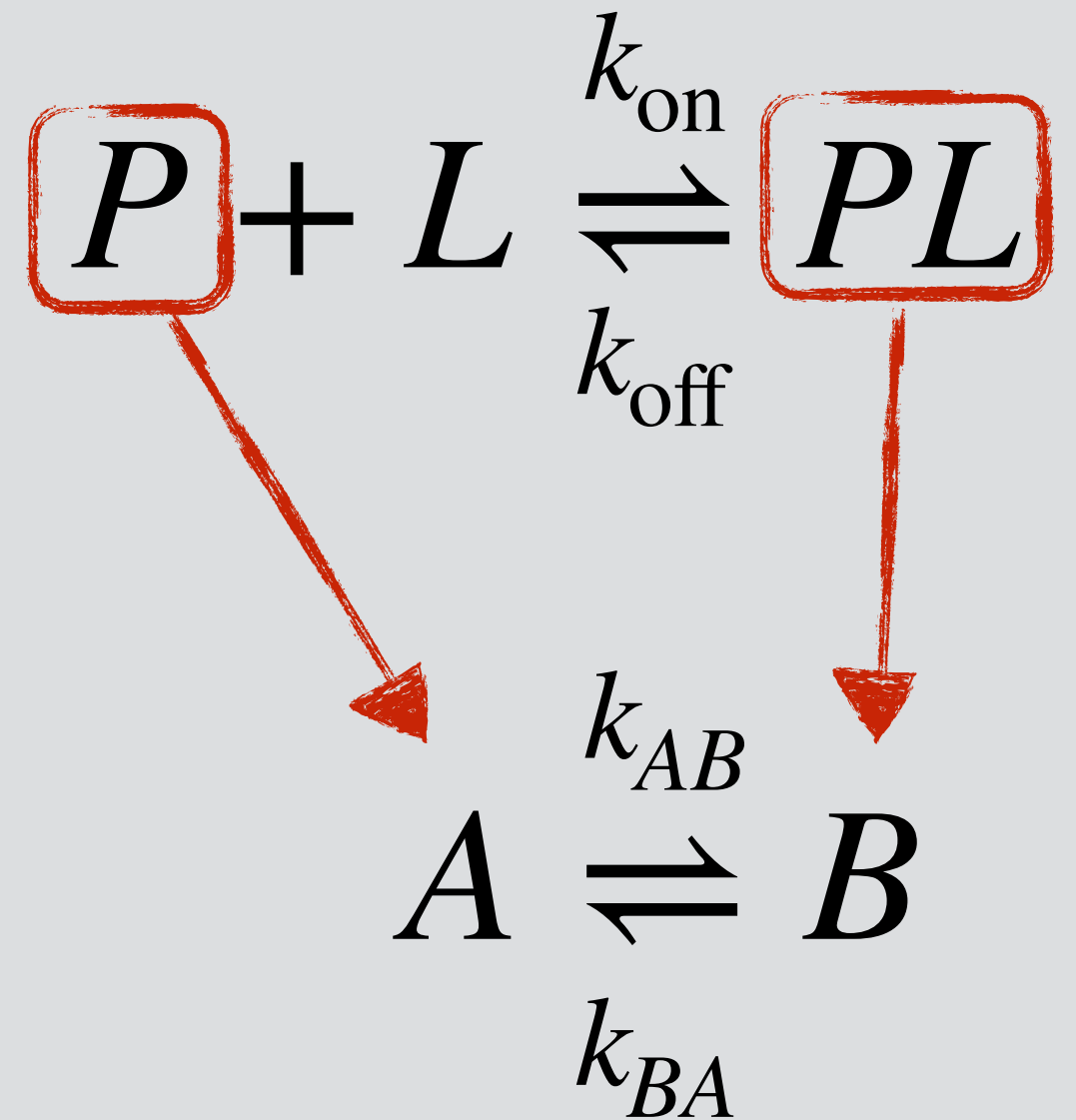
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$[P]_0 = 100 \mu\text{M}$
 $[L]_0 = 50 \mu\text{M}$

$\Rightarrow [L] = 12 \mu\text{M}$
 $\Rightarrow k_{AB} = k_{\text{on}}[L] = 600 \text{ s}^{-1}$

$k_{\text{ex}} = 1600 \text{ s}^{-1}$



$$k_{AB} = k_{\text{on}}[L]$$

$$k_{BA} = k_{\text{off}}$$

$$L = \frac{1}{2} \left[L_0 - P_0 - K_d + \sqrt{(L_0 + P_0 + K_d)^2 - 4P_0L_0} \right]$$

Example

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$$\begin{aligned}[P]_0 &= 100 \mu\text{M} \\ [L]_0 &= 50 \mu\text{M}\end{aligned}$$

$$\begin{aligned}\Rightarrow [L] &= 12 \mu\text{M} \\ \Rightarrow k_{AB} = k_{\text{on}}[L] &= 600 \text{ s}^{-1}\end{aligned}$$

$$\mathbf{k_{\text{ex}} = 1600 \text{ s}^{-1}}$$

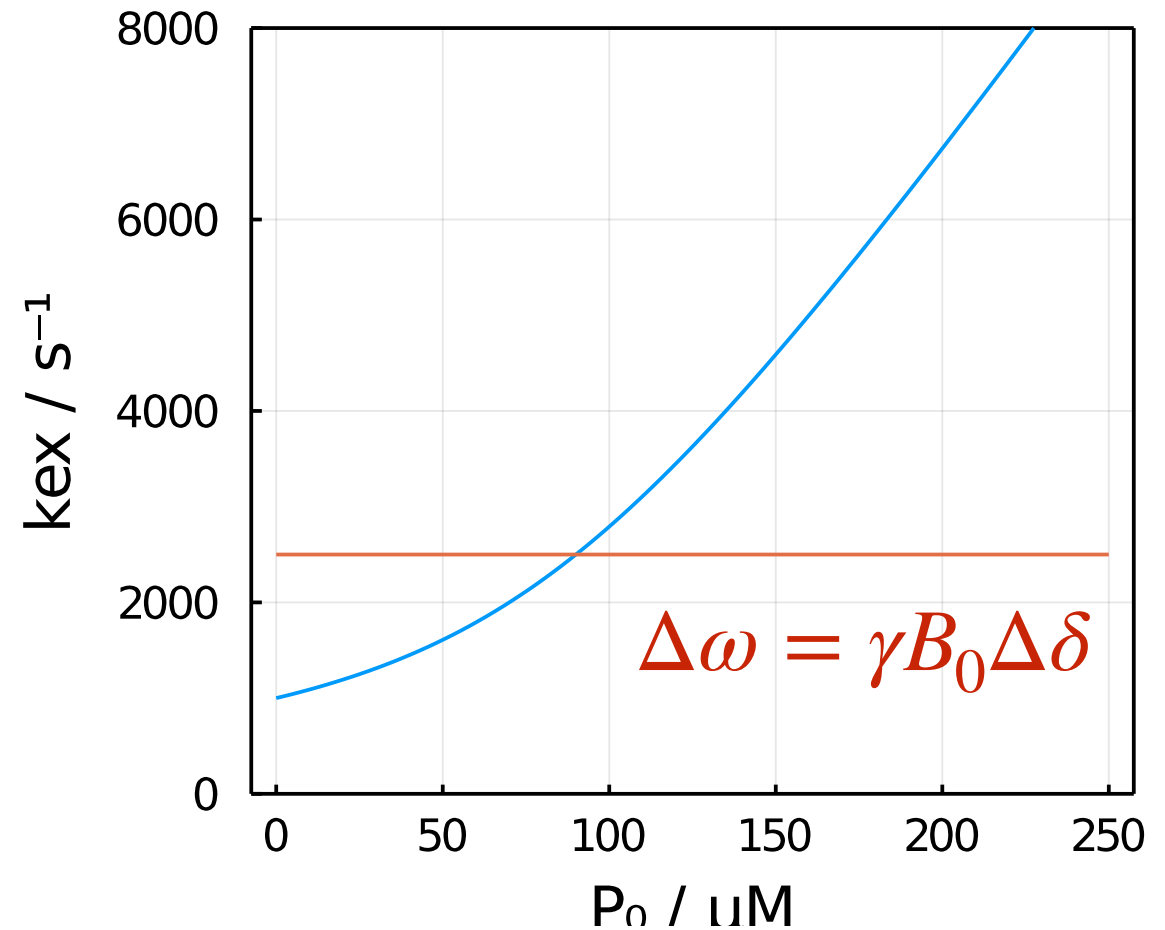
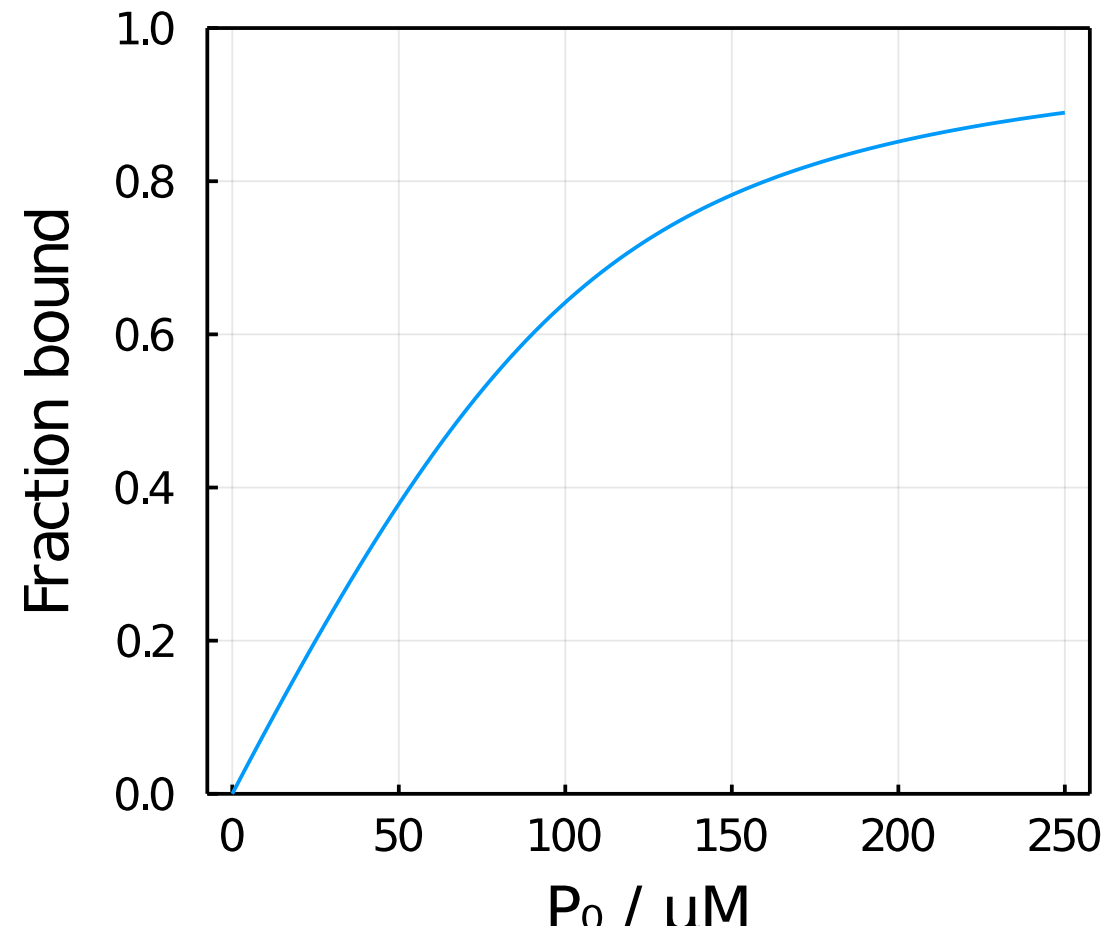
$$\Delta\omega = \gamma B_0 \Delta\delta$$

$$\begin{aligned}\text{e.g. } \Delta\delta (^1\text{H}) &= 0.5 \text{ ppm} \\ &800 \text{ MHz}\end{aligned}$$

$$\begin{aligned}\Delta\nu &= 400 \text{ Hz} \\ \mathbf{\Delta\omega = 2\pi \Delta\nu = 2500 \text{ s}^{-1}}\end{aligned}$$

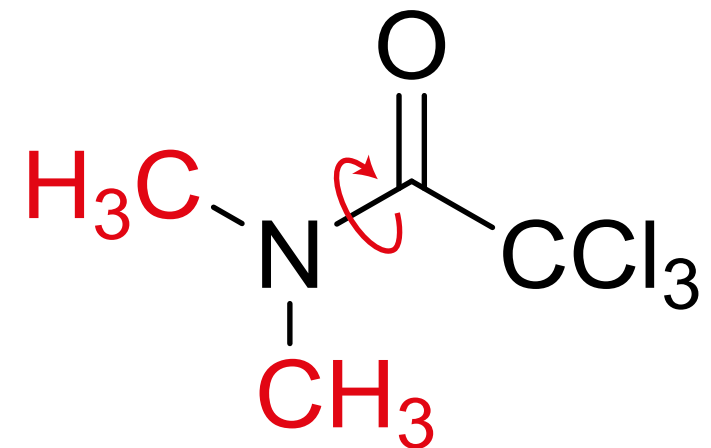
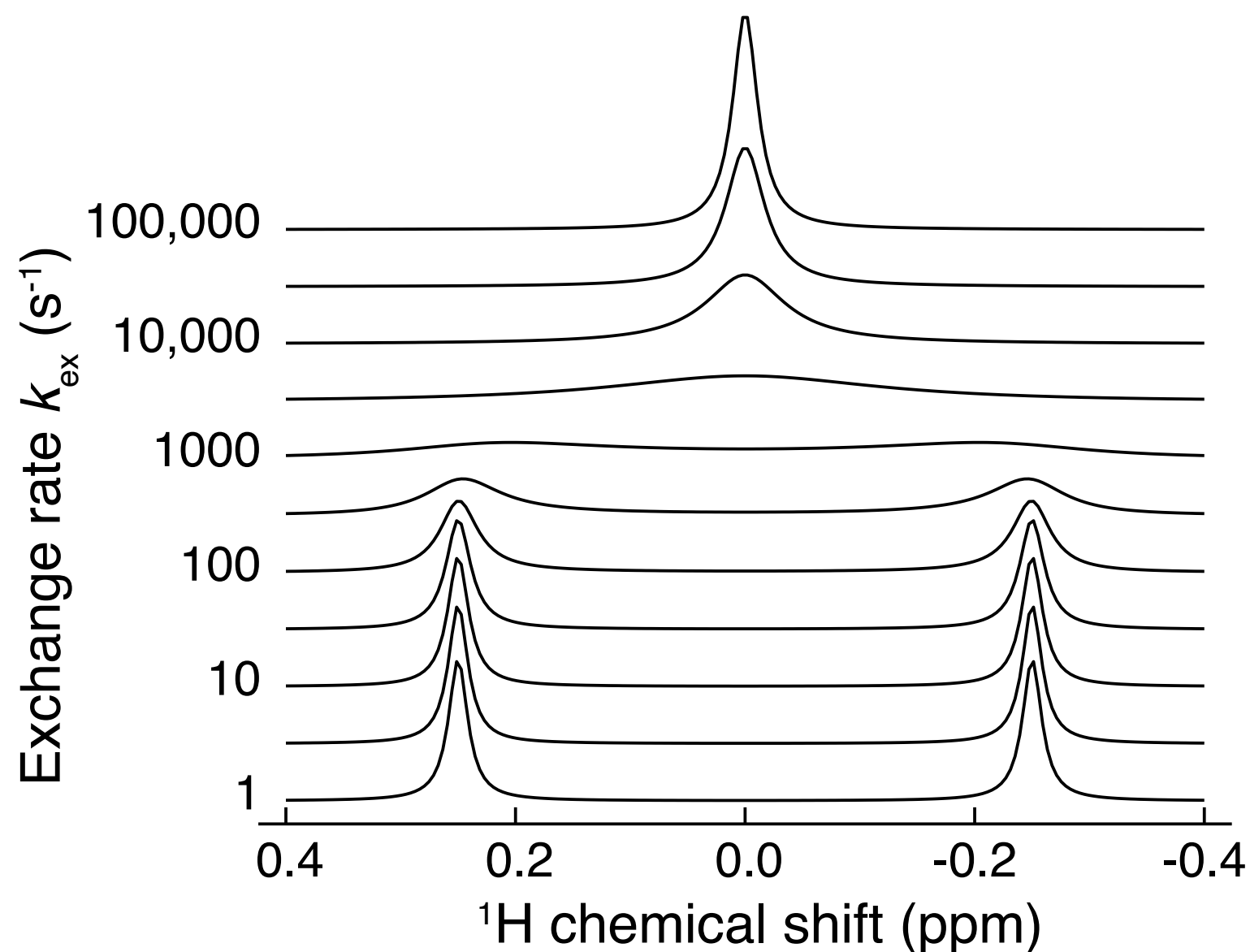
The exchange rate increases along a titration

$$\begin{aligned}k_{\text{ex}} &= k_{AB} + k_{BA} \\ &= k_{\text{on}}[L] + k_{\text{off}}\end{aligned}$$



$$\begin{aligned}K_d &= 20 \mu\text{M} \\ k_{\text{off}} &= 1000 \text{ s}^{-1} \\ [P]_0 &= 100 \mu\text{M} \\ \Delta\delta (^1\text{H}) &= 0.5 \text{ ppm (800 MHz)}\end{aligned}$$

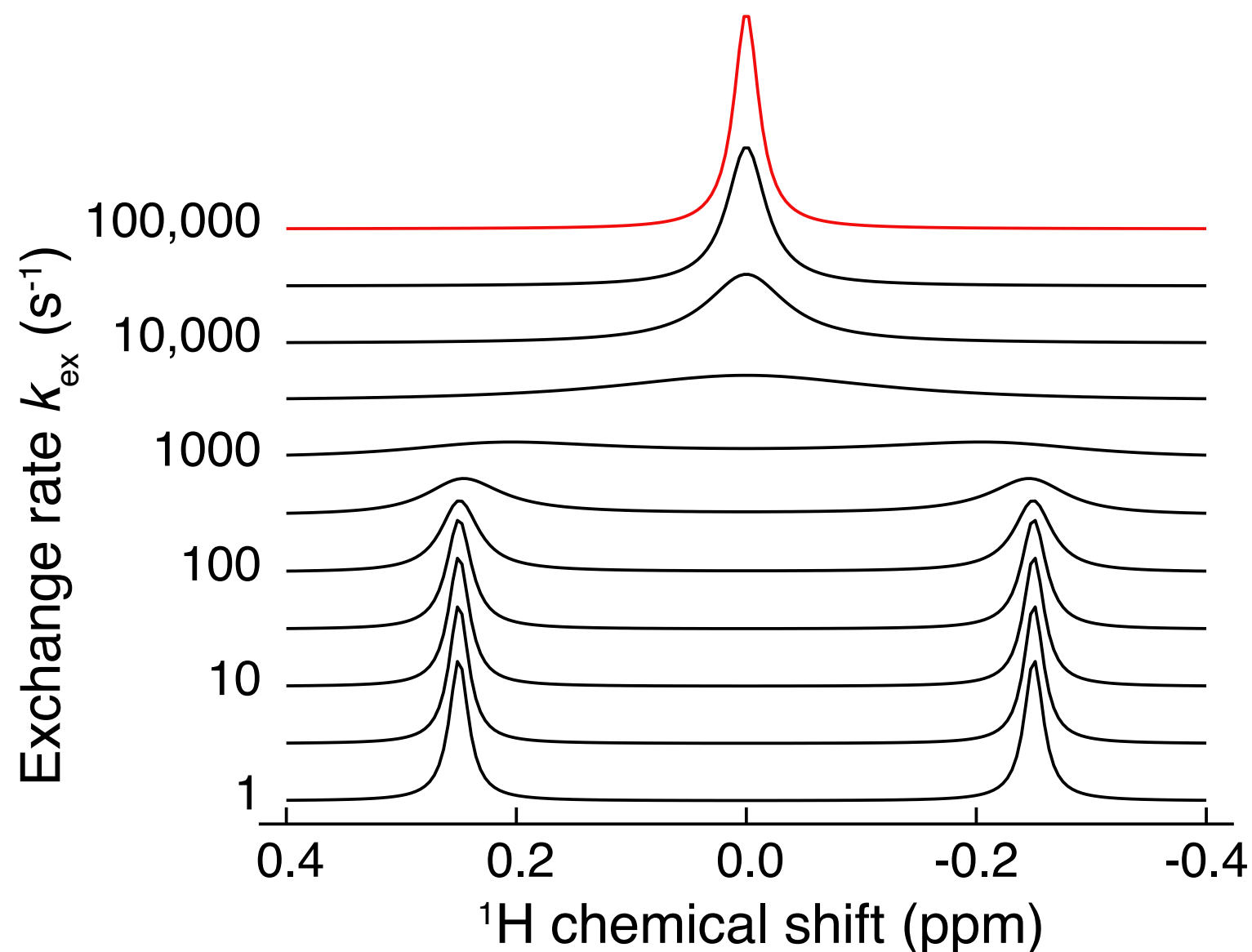
Chemical exchange regimes



two sites, related by symmetry
=> equal populations

Simulated resonance line shapes for a ^1H chemical shift difference of 0.5 ppm at 800 MHz ($\Delta\omega = 2500 \text{ s}^{-1}$) and the indicated exchange rate, k_{ex}

Chemical exchange regimes: fast exchange ($k_{\text{ex}} \gg \Delta\omega$)

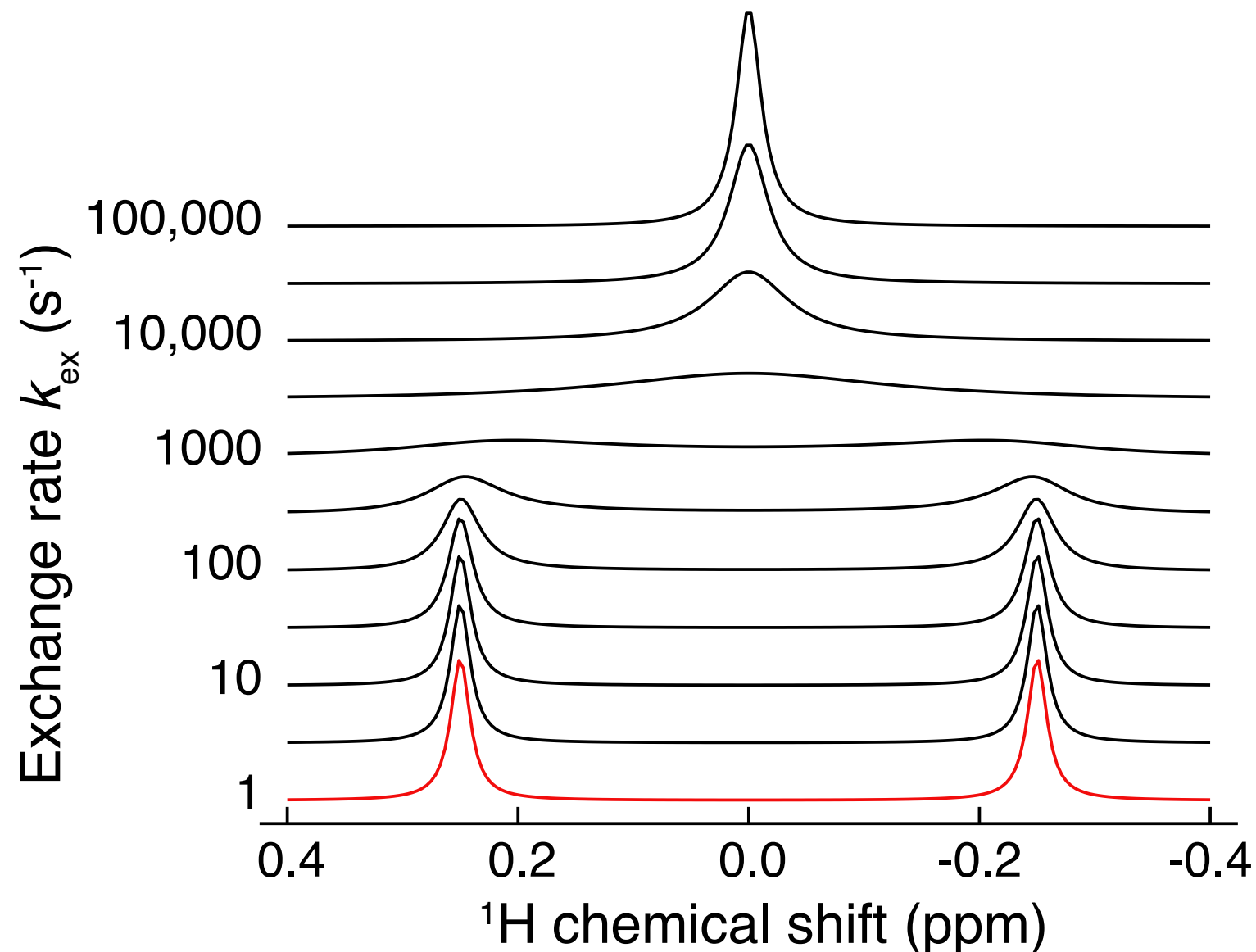


Molecules are jumping between states so rapidly that only a single averaged frequency can be detected

Single resonance observed at average of individual chemical shifts

Linewidth (R_2) is average of individual resonances

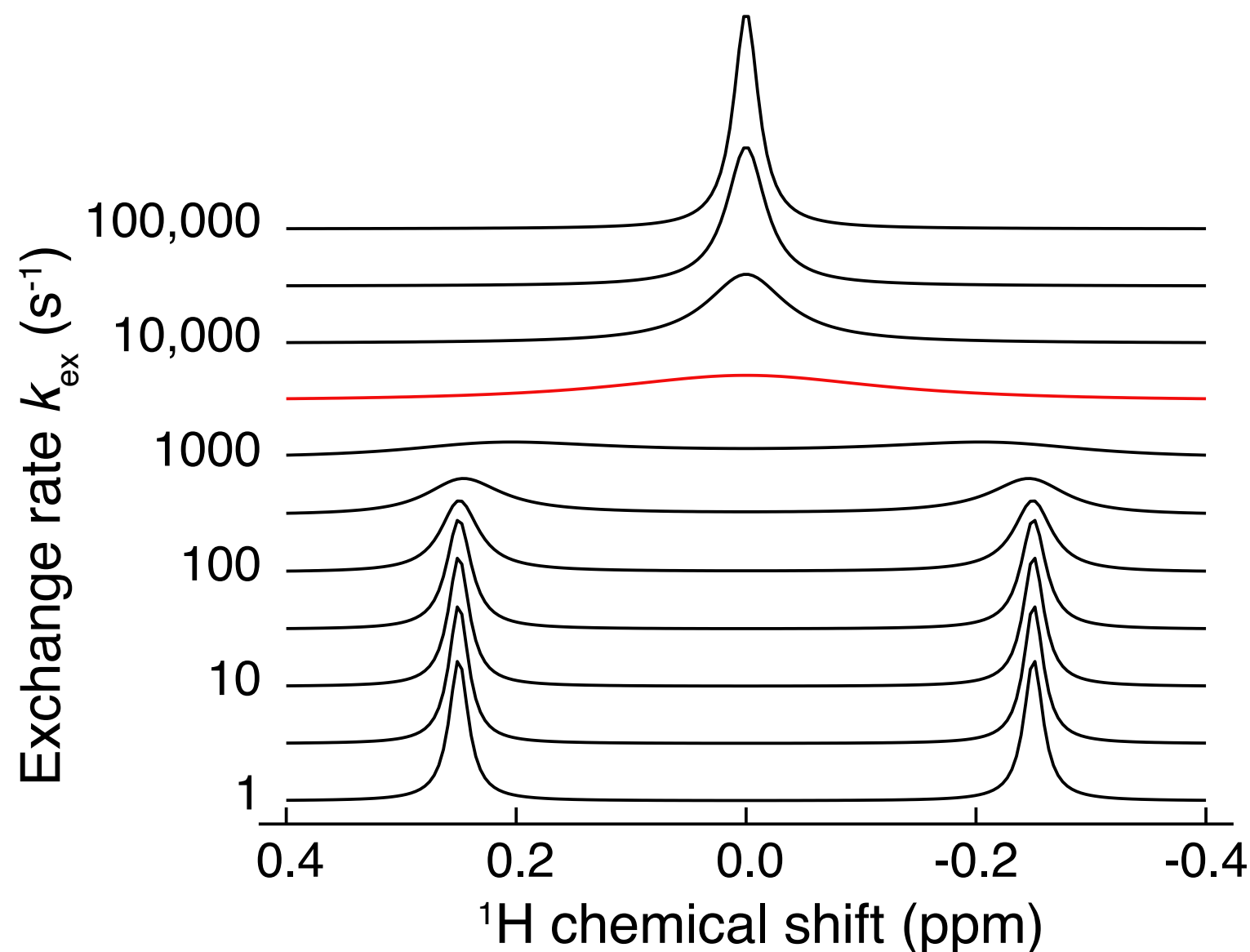
Chemical exchange regimes: slow exchange ($k_{\text{ex}} \ll \Delta\omega$)



Molecules effectively never exchange during free induction decay – like two separate chemical species

Individual resonances observed

Chemical exchange regimes: intermediate exchange ($k_{\text{ex}} \approx \Delta\omega$)



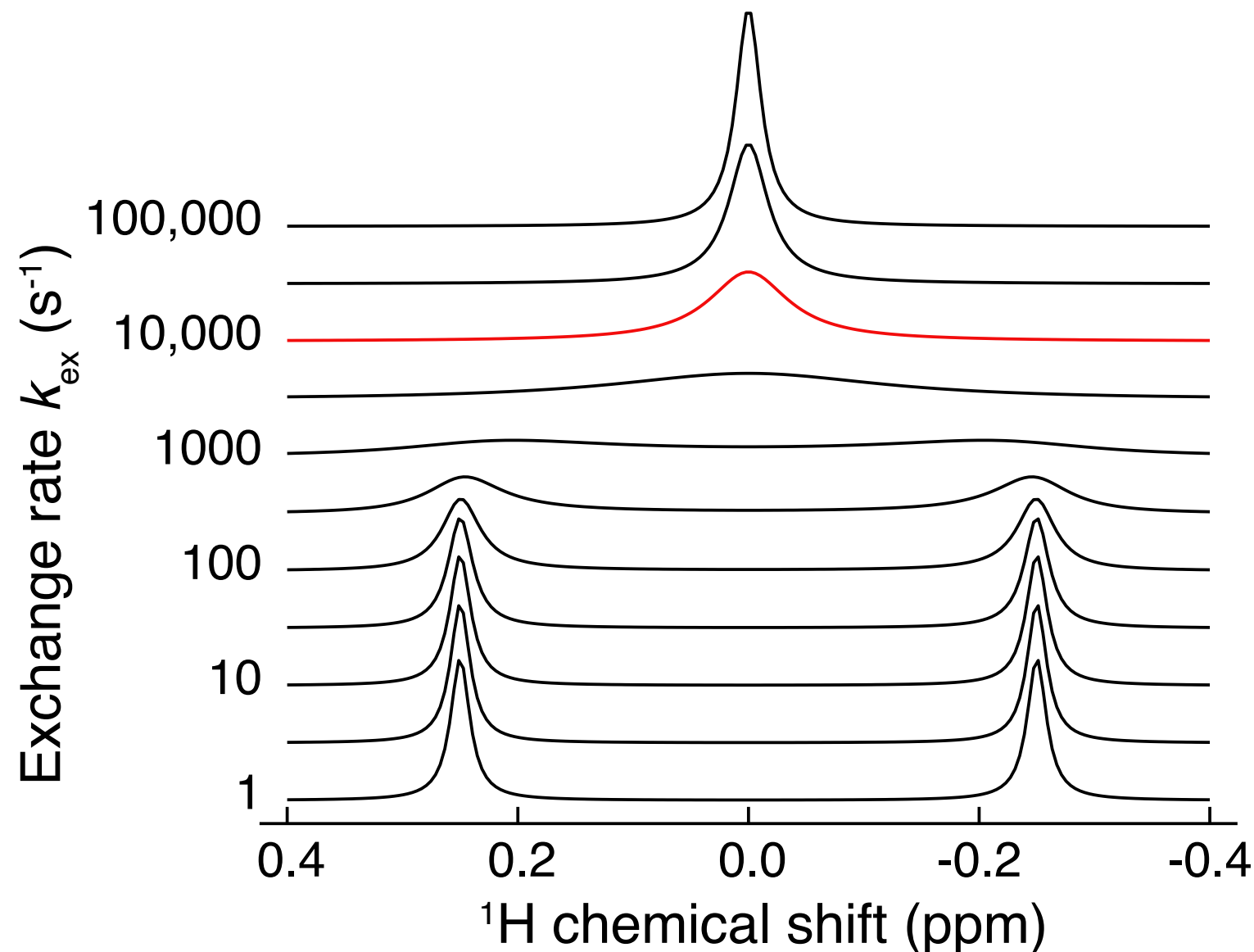
Severe line broadening results when the exchange rate is comparable to the frequency difference – the intermediate exchange regime

The coalescence point, defined by vanishing first and second derivatives, occurs when

$$k_{\text{ex}} = |\Delta\omega| / \sqrt{2}$$

Identification of the coalescence point provides a simple way to determine exchange rates – but more sophisticated approaches are available!

Chemical exchange regimes: fast-intermediate exchange ($k_{\text{ex}} > \Delta\omega$)



As a signal in fast exchange approaches the coalescence point, its line width increases and intensity decreases due to **exchange broadening**:

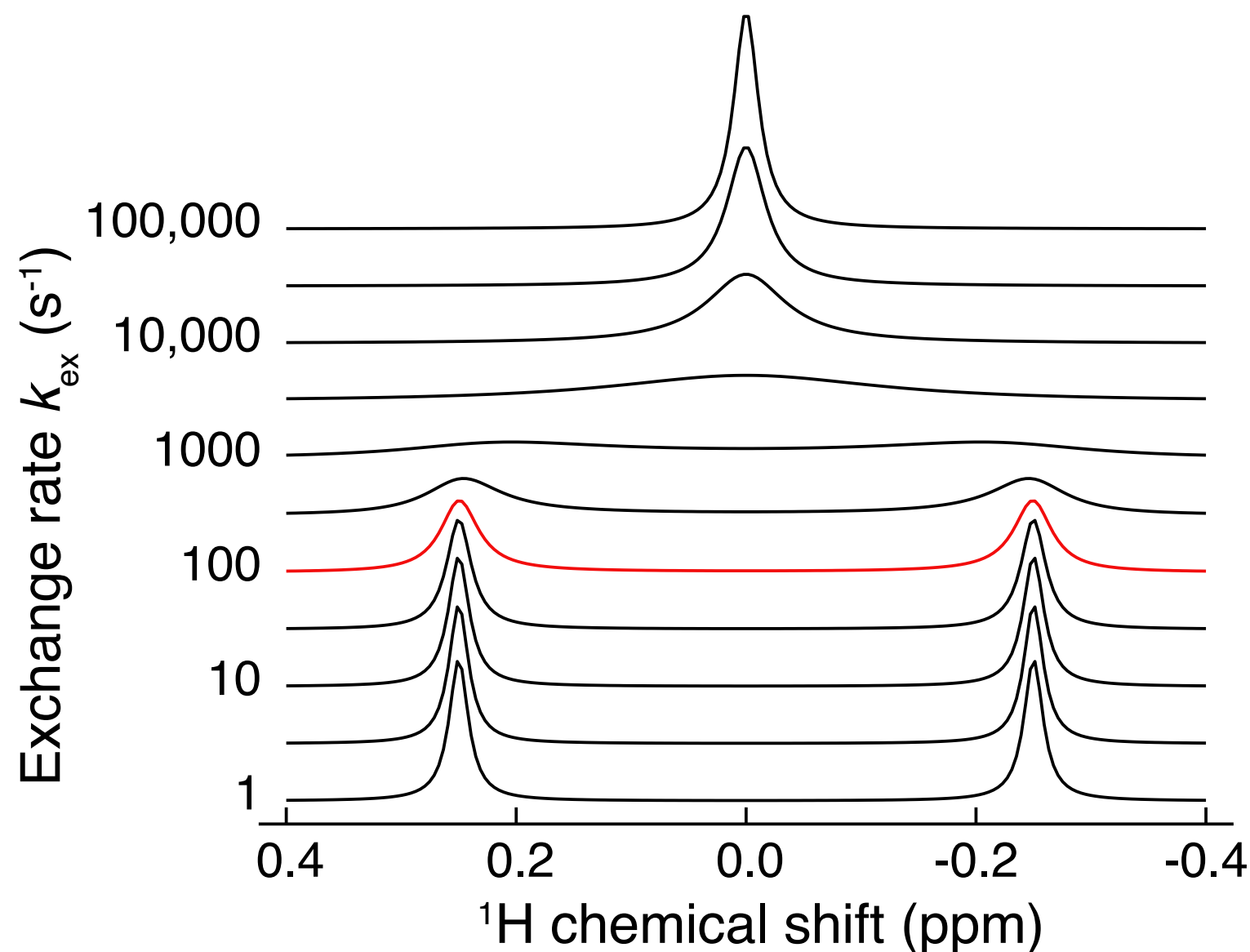
$$R_{2,\text{obs}} = R_{2,0} + R_{\text{ex}}$$

The exchange broadening contribution depends on the populations, exchange rate and frequency difference:

$$R_{\text{ex}} = \frac{p_A p_B \Delta\omega^2}{k_{\text{ex}}}$$

Note that the frequency difference is also proportional to the magnetic field strength – exchange broadening is more severe at higher field strengths

Chemical exchange regimes: slow-intermediate exchange ($k_{\text{ex}} < \Delta\omega$)



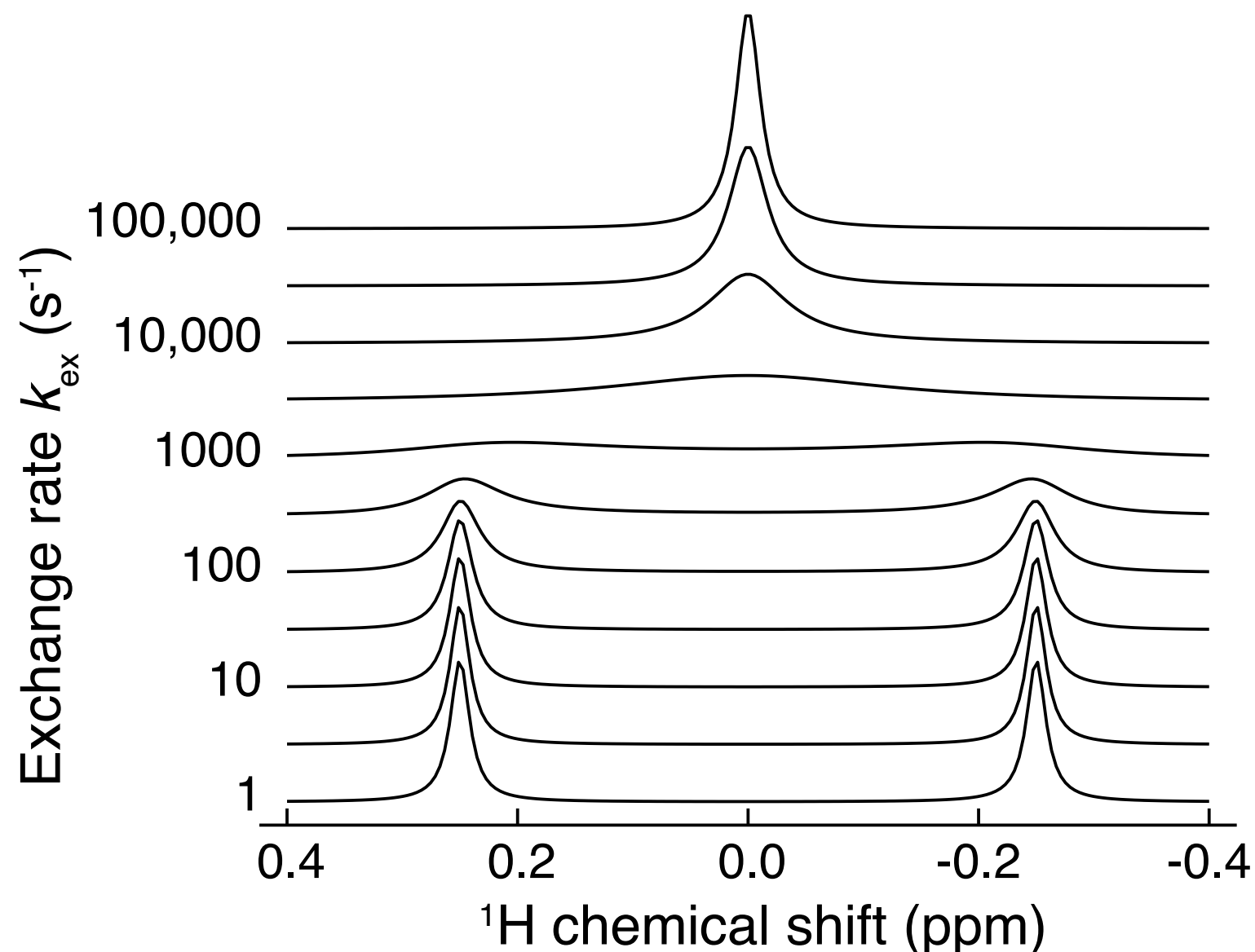
Resonances in slow exchange approaching the coalescence point also experience **lifetime line broadening**:

$$R_{\text{ex,A}} = k_{AB}$$

This arises from the irreversible loss of magnetisation from spins exchanging during the FID

Lifetime line broadening is independent of the chemical shift difference, population and magnetic field strength

Chemical exchange regimes: how sensitive is NMR?



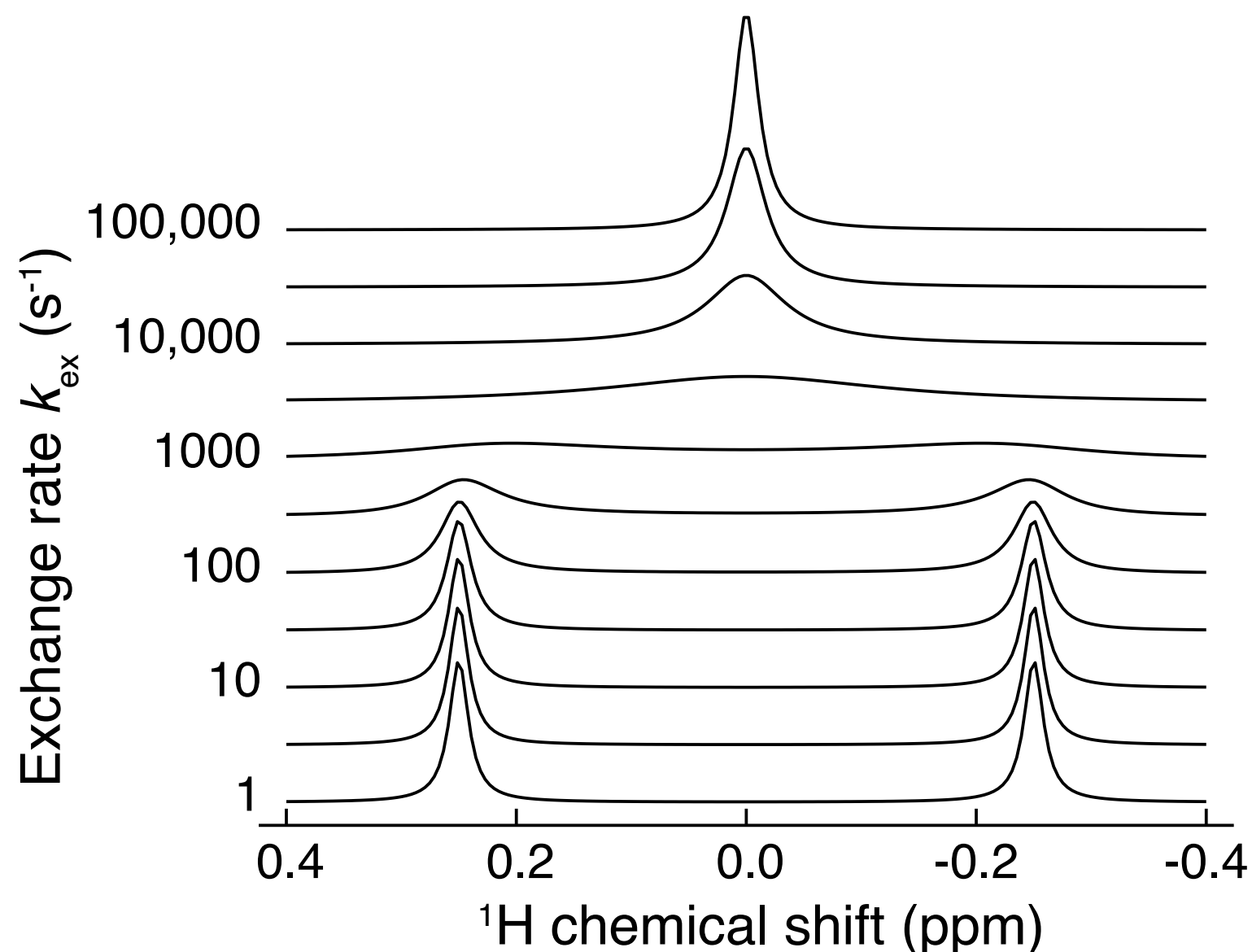
Spectra are most sensitive to exchange in the vicinity of the coalescence point

Line broadening effects can be observed over a wide range of parameter space, approximately:

$$\Delta\omega / 50 < k_{\text{ex}} < 50 \Delta\omega$$

Different spins within a molecule can also have difference $\Delta\omega$, bringing sensitivity to an even wider range of exchange rates!

Chemical exchange regimes: why is NMR unique?



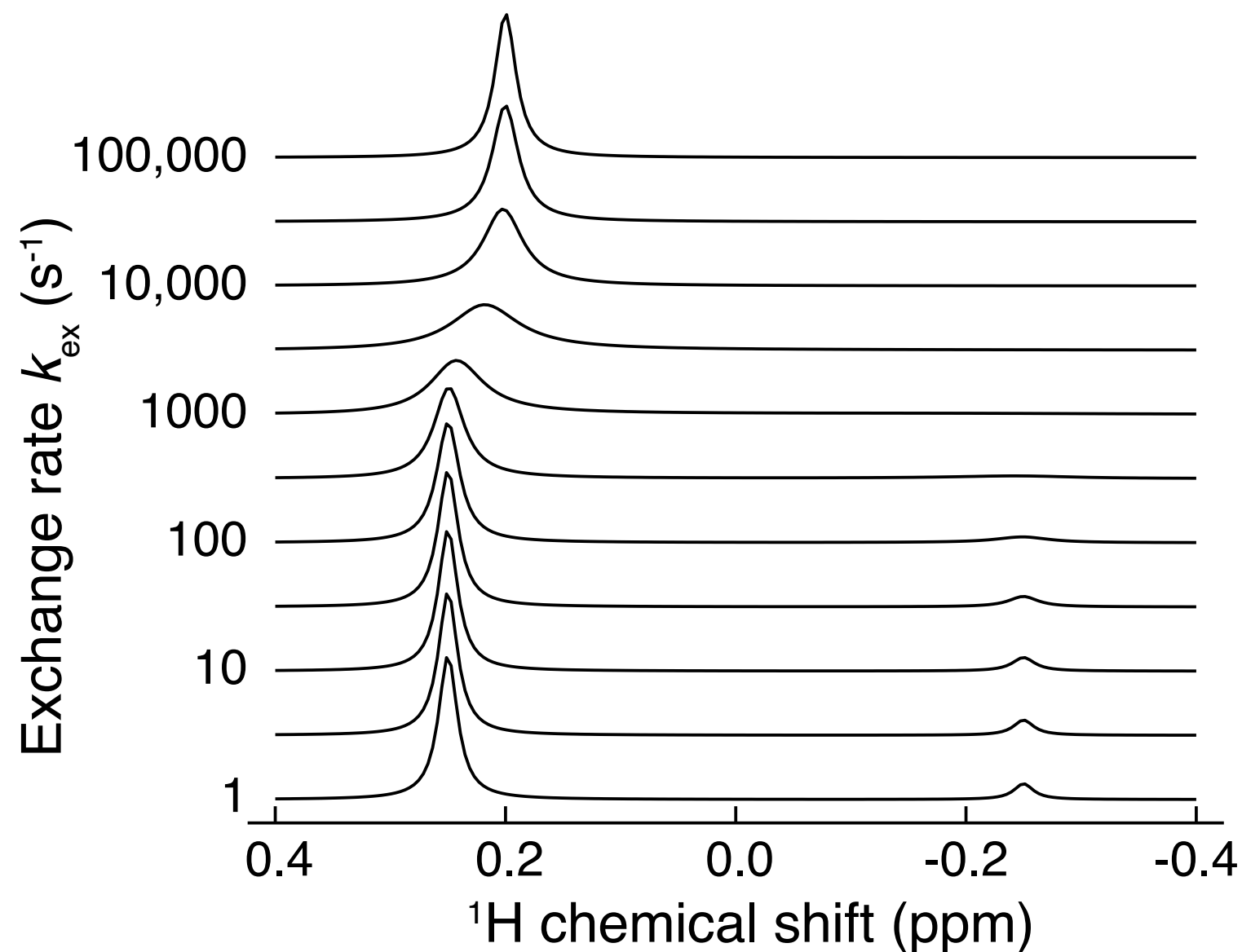
Why do other forms of spectroscopy (e.g. CD, UV, IR, fluorescence) not see similar chemical exchange effects?

...because the relevant frequency differences are **much** bigger!

e.g. two species absorbing at 500 nm and 520 nm have frequencies of 6×10^{14} Hz and 5.8×10^{14} Hz

$$\Rightarrow \Delta\omega \approx 1.2 \times 10^{14} \text{ s}^{-1}!$$

Chemical exchange regimes: unequal populations

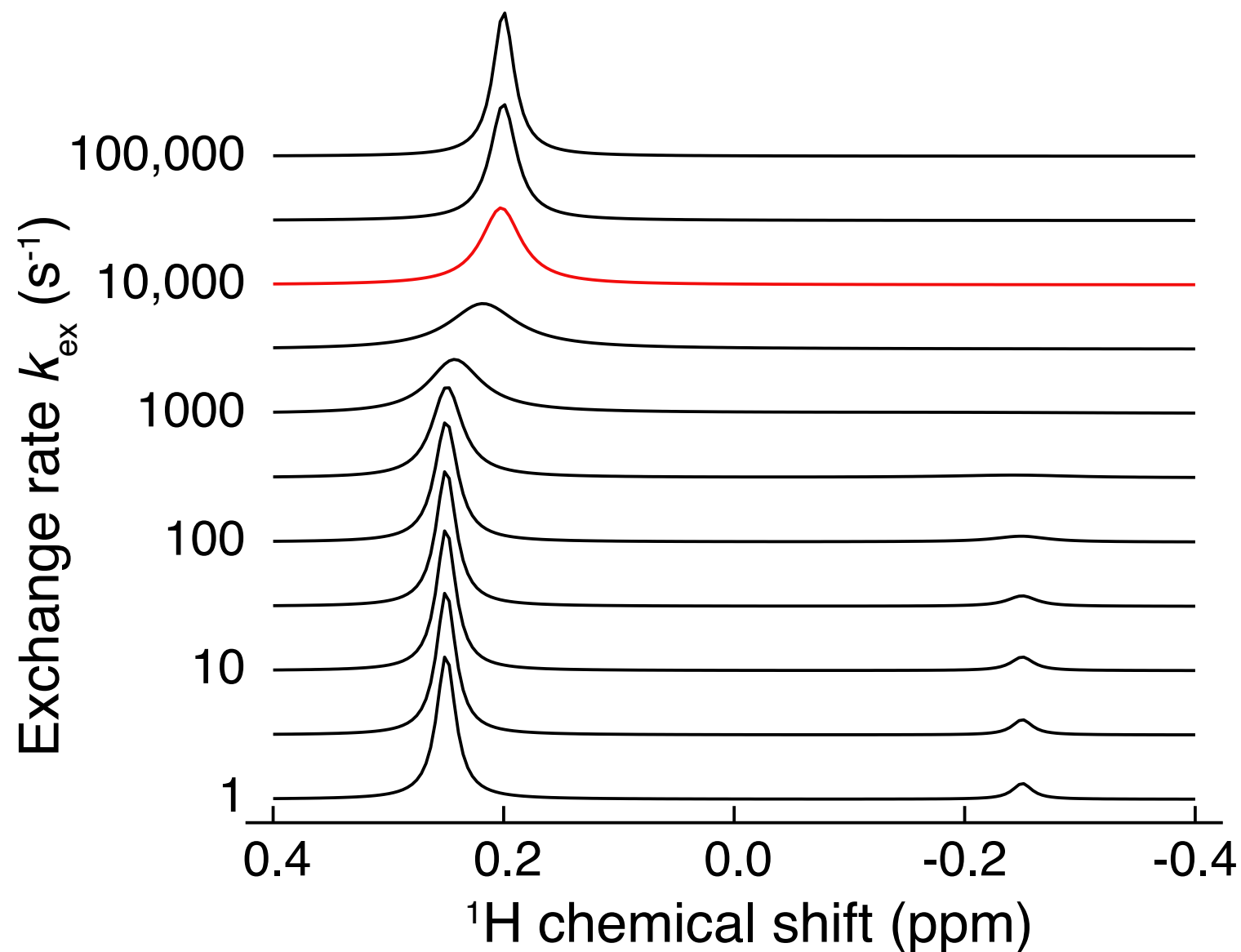


Unequal populations can arise in many circumstances:

- early stages of a titration
- sparsely populated intermediates in biomolecules
- spins in exchange with the solvent (solvent is the major state!)

Simulated resonance line shapes for unequal populations (90% / 10%)

Chemical exchange regimes: unequal populations



In fast exchange, we observe a single resonance at the population-weighted average frequency:

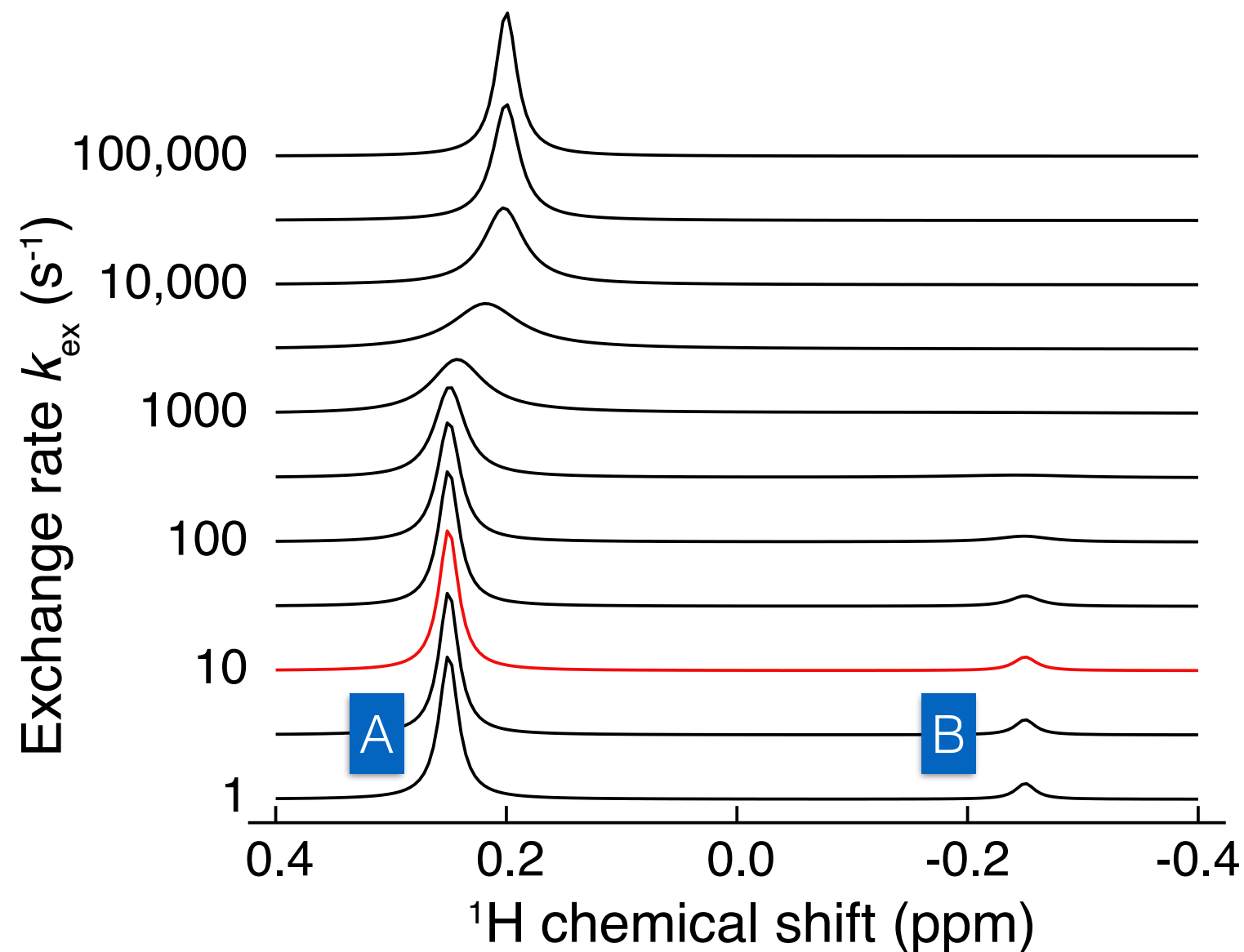
$$\omega_{\text{obs}} = p_A\omega_A + p_B\omega_B$$

with exchange broadening as for symmetric populations:

$$R_{\text{ex}} = \frac{p_A p_B \Delta\omega^2}{k_{\text{ex}}}$$

Simulated resonance line shapes for unequal populations (90% / 10%)

Chemical exchange regimes: unequal populations



Simulated resonance line shapes for unequal populations (90% / 10%)

In slow exchange, we observe two resonances with population-weighted **amplitudes**

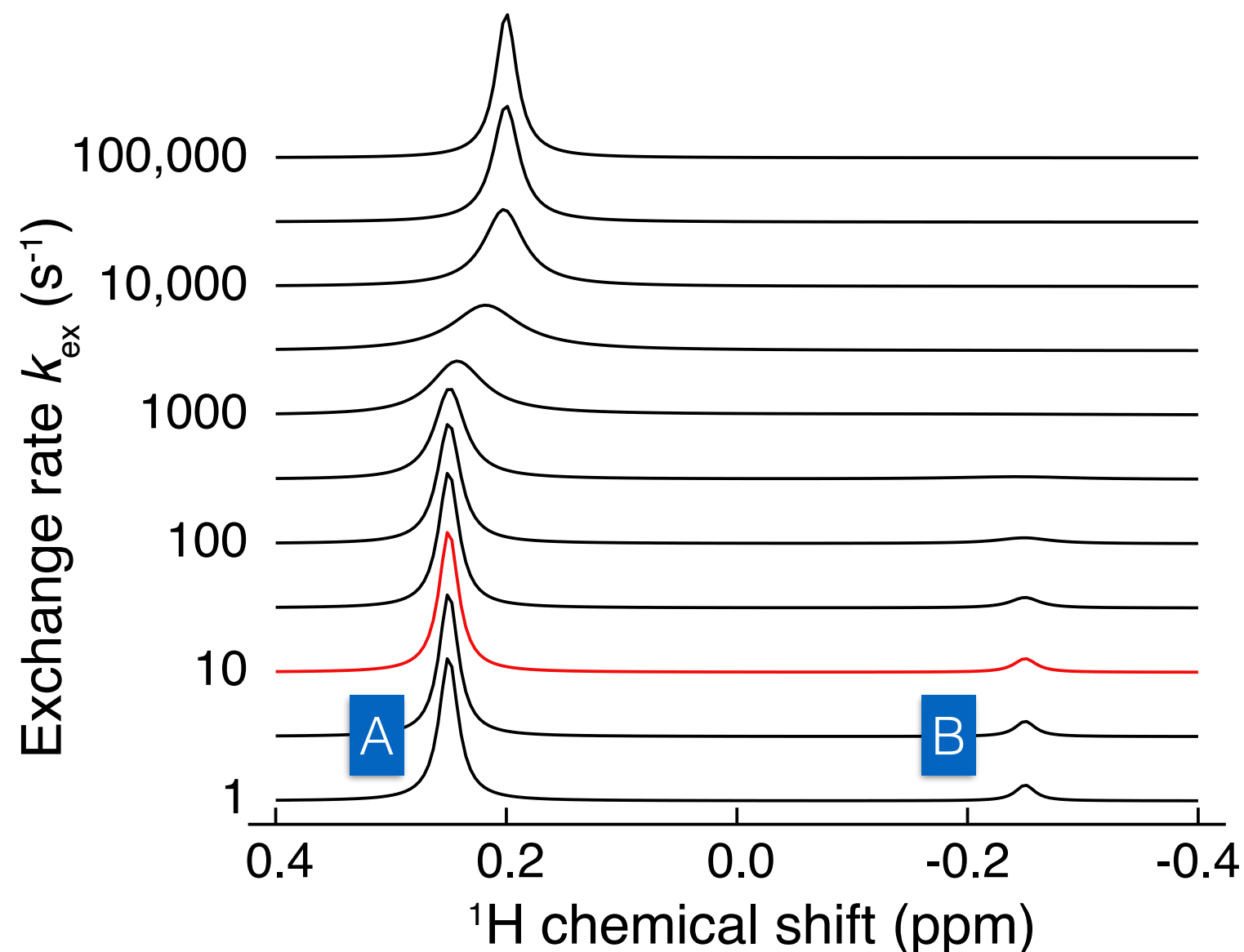
Major and minor peaks both exhibit **lifetime line broadening**, but the impact of this is very different for the two peaks

$$R_{\text{ex,A}} = k_{AB} \quad \text{small}$$

$$R_{\text{ex,B}} = k_{BA} \quad \textbf{LARGE}$$

$$\text{intensity} \sim \frac{\text{amplitude}}{R_{2,0} + R_{\text{ex}}}$$

Chemical exchange regimes: unequal populations



Simulated resonance line shapes for unequal populations (90% / 10%)

In slow exchange, we observe two resonances with population-weighted **amplitudes**

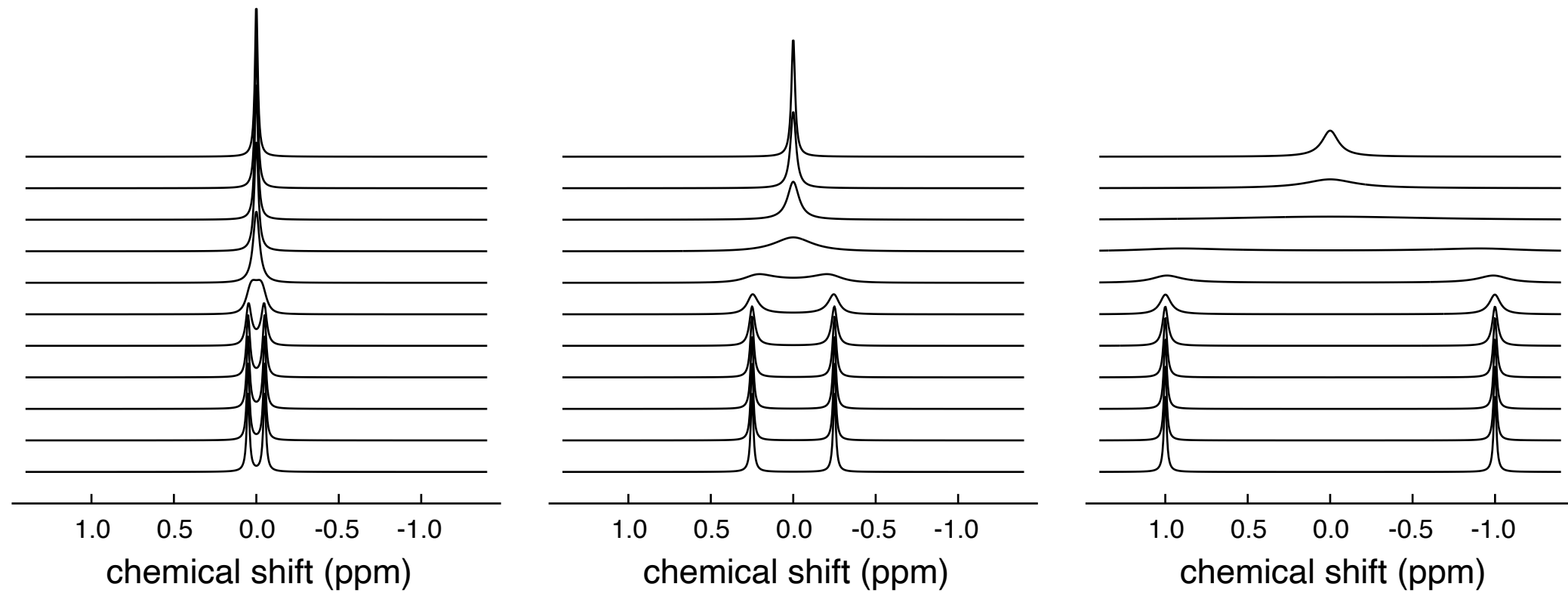
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$$R_{\text{ex,A}} = k_{AB} \quad \text{small}$$

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Minor states are often effectively 'invisible' and experiments such as CEST and CPMG may be required to detect and probe them

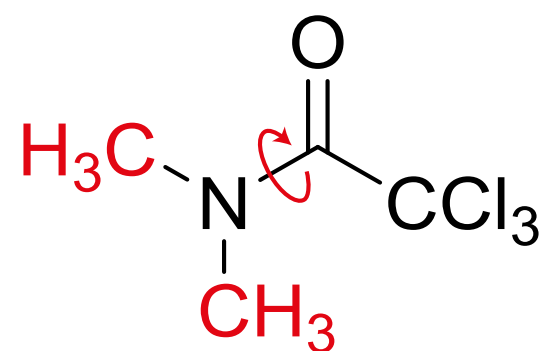
Modulating chemical exchange regimes



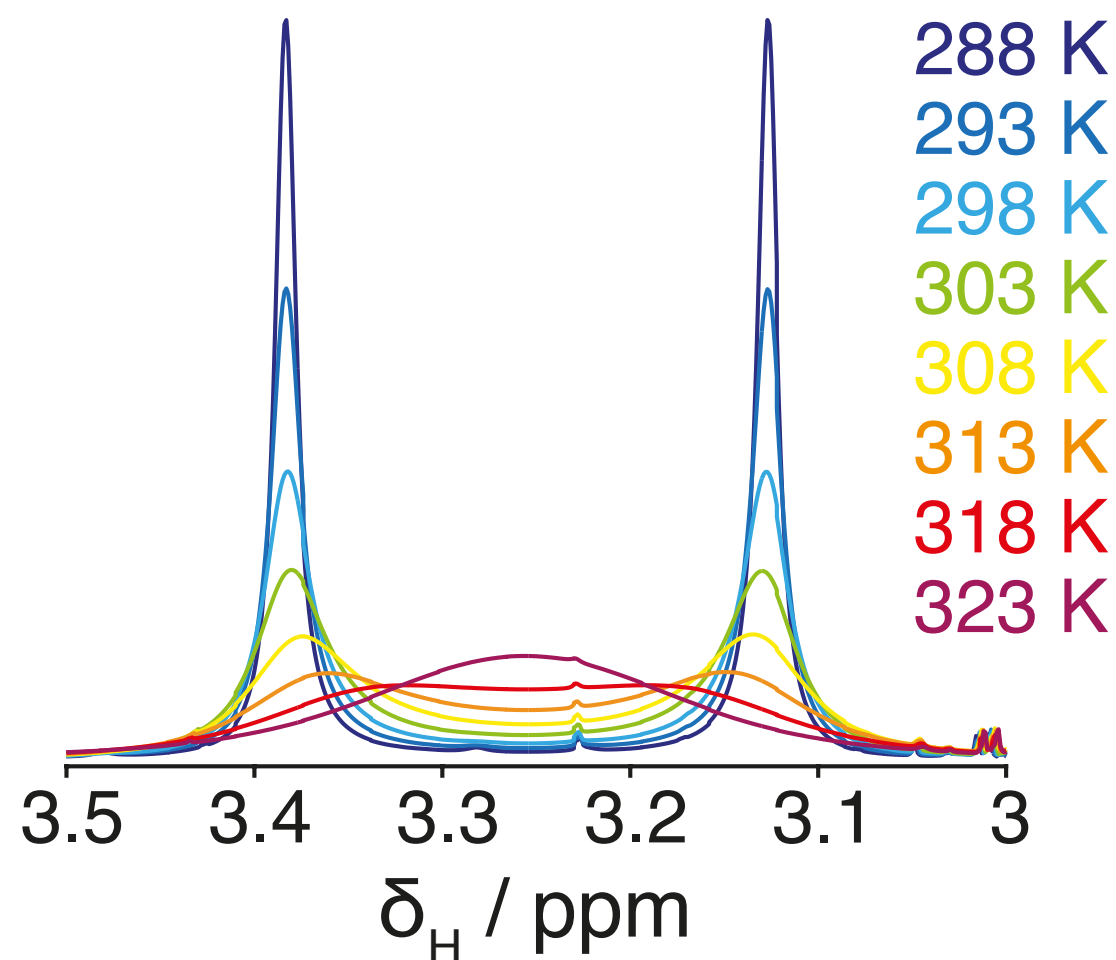
Varying the magnetic field strength will vary $\Delta\omega = \gamma\Delta\delta B_0$

Alternatively, most molecules will contain a range of spins that experience a variety of chemical shift changes between states

Modulating chemical exchange regimes

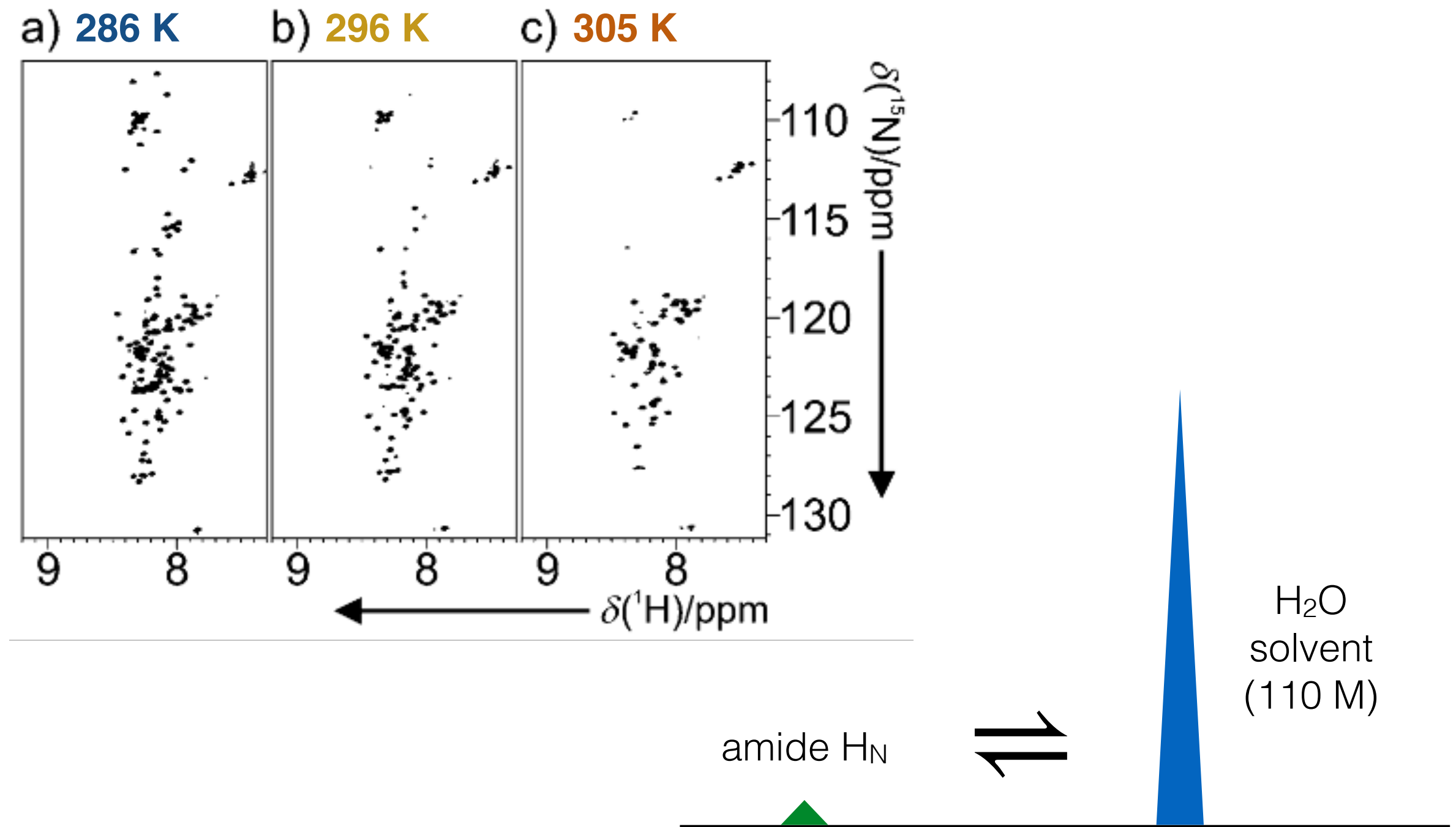


$$\begin{aligned}\Delta\delta_{\text{H}} &= 0.26 \text{ ppm} \\ \Delta\delta_{\text{C}} &= 0.62 \text{ ppm} \\ {}^1J_{\text{CH}} &= 140 \text{ Hz} \\ k_{\text{ex}} &= 125 \text{ s}^{-1} \\ &\quad (298 \text{ K})\end{aligned}$$



Changing the temperature can change the kinetics of the exchange process

Application of VT NMR to intrinsically disordered proteins

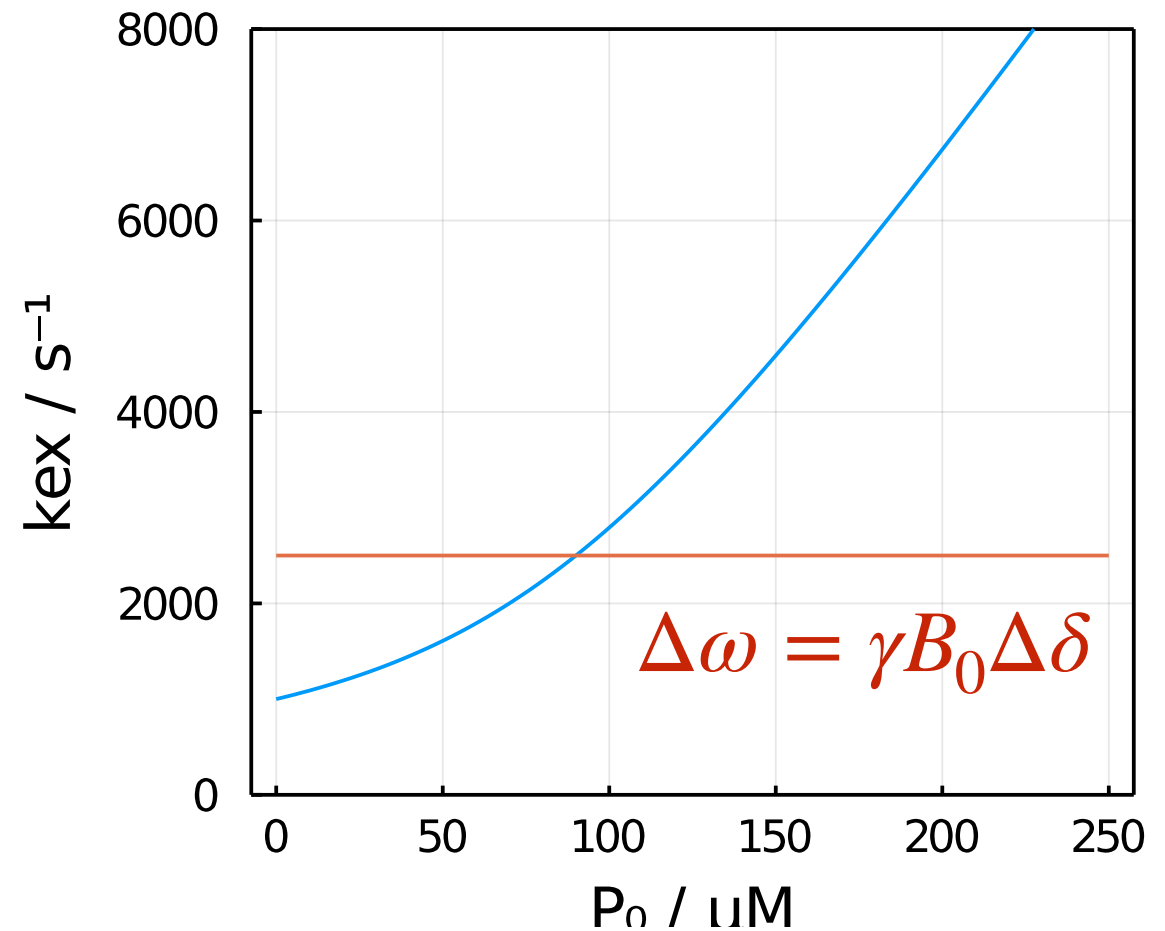
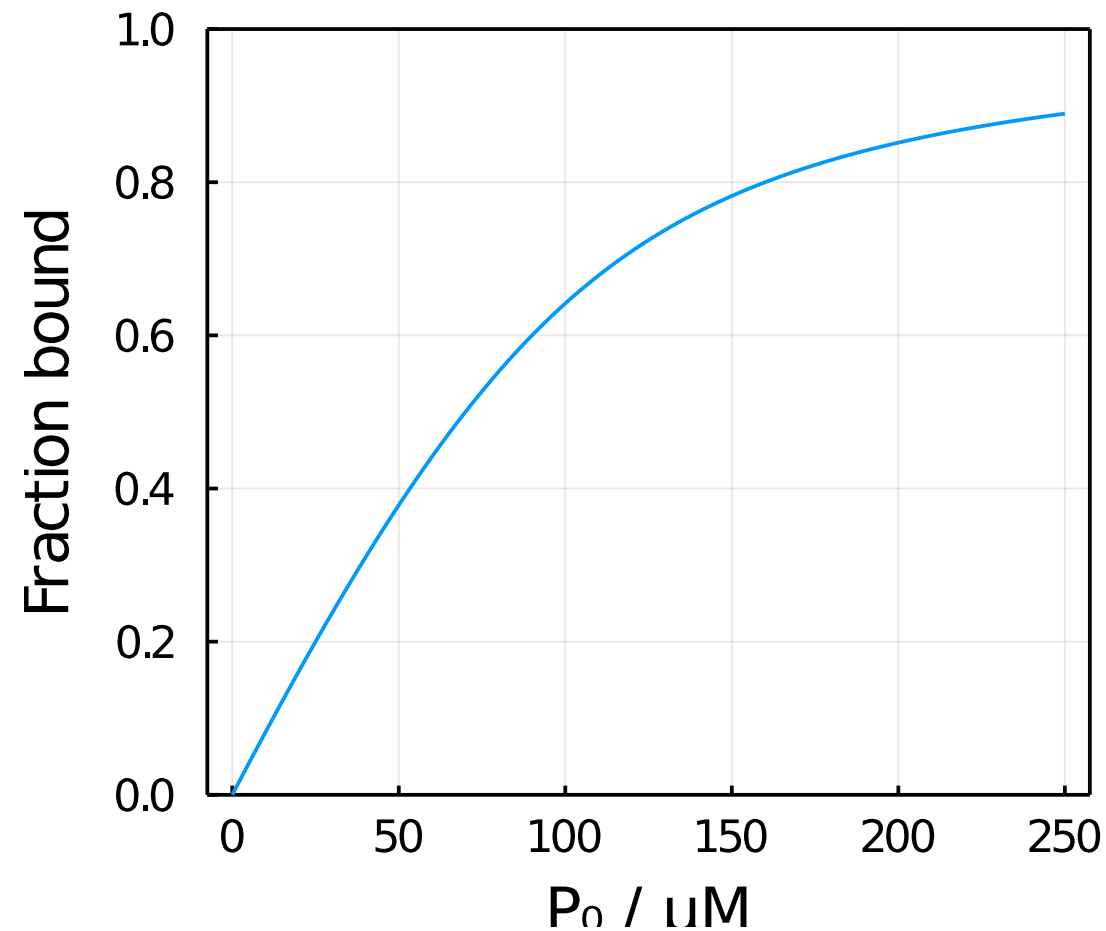


lifetime line broadening due to solvent hydrogen exchange of amide minor state leads to loss of resonances in 2D spectra

Titration experiments

$$k_{\text{ex}} = k_{AB} + k_{BA}$$

$$= k_{\text{on}}[L] + k_{\text{off}}$$



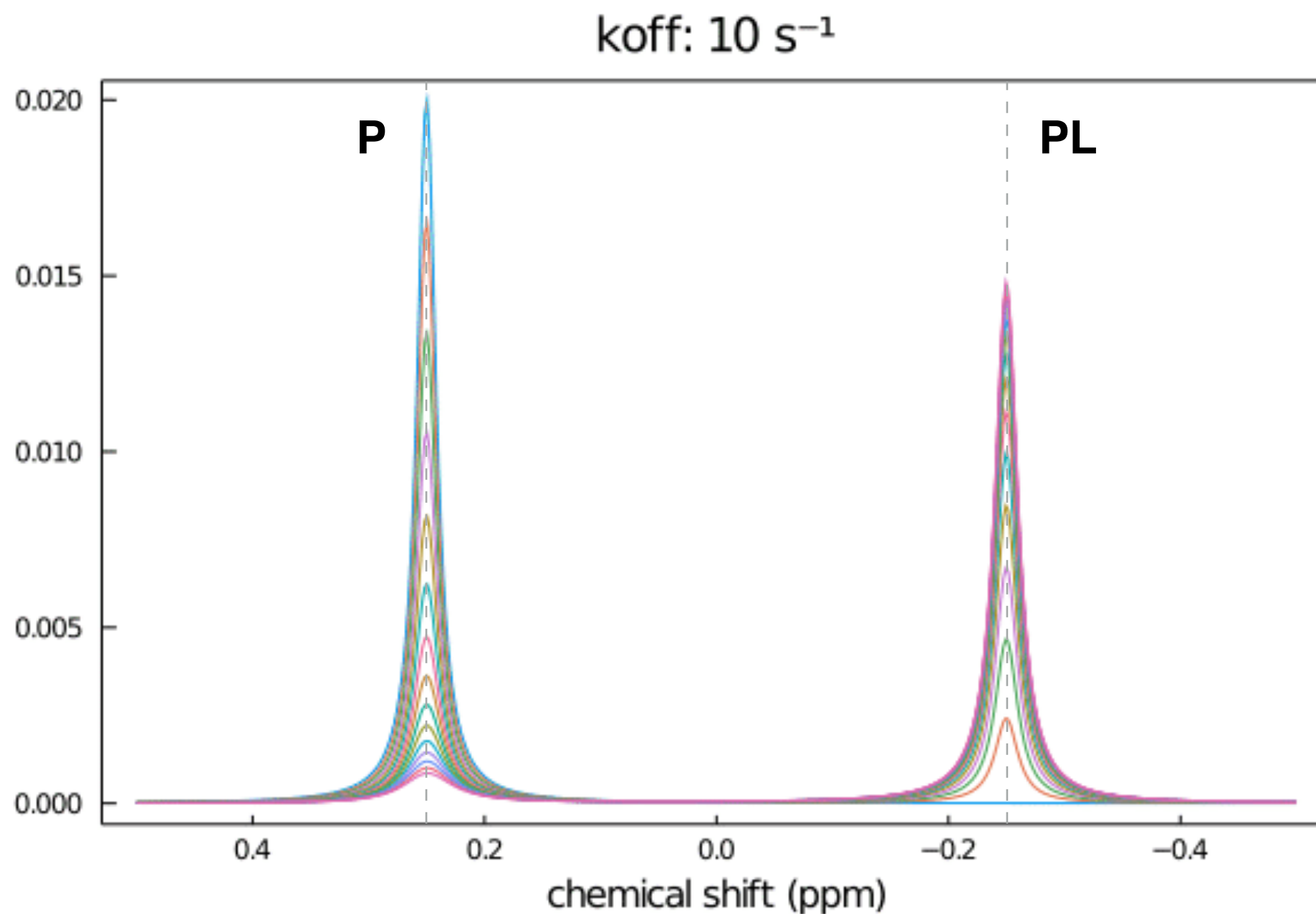
$$K_d = 20 \mu\text{M}$$

$$k_{\text{off}} = 1000 \text{ s}^{-1}$$

$$[P]_0 = 100 \mu\text{M}$$

$$\Delta\delta (^1\text{H}) = 0.5 \text{ ppm (800 MHz)}$$

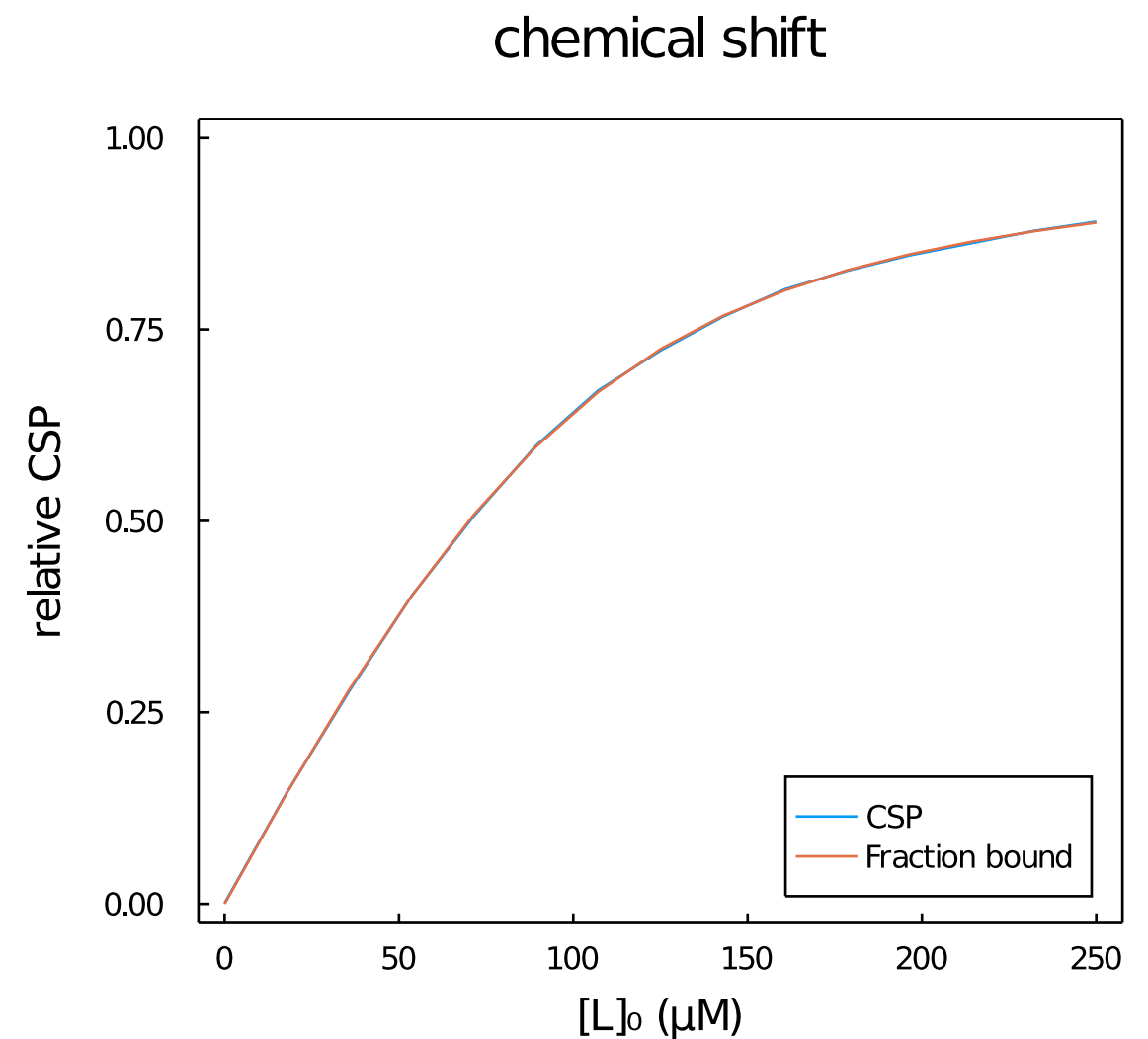
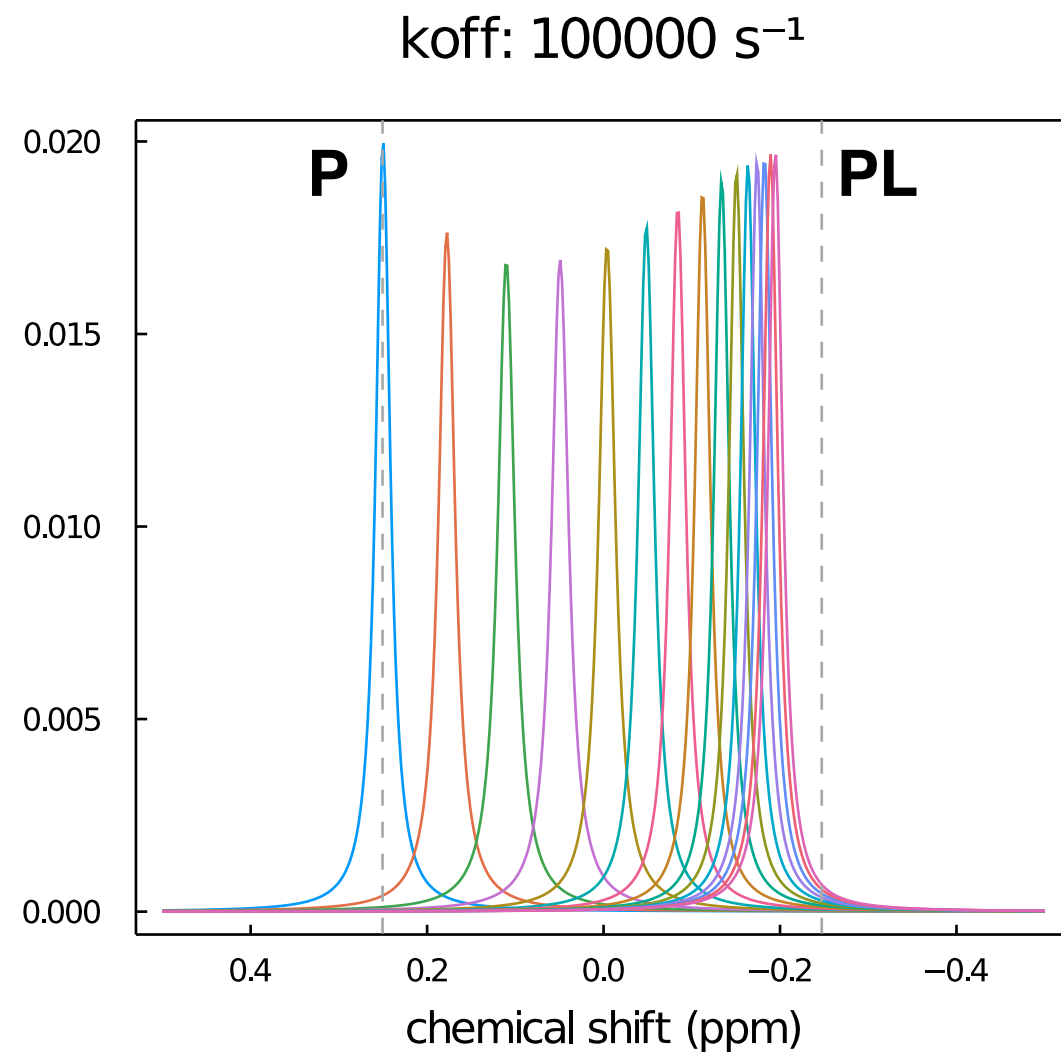
Titration experiments: effect of varying dissociation rate



$\Delta\delta (^1\text{H}) = 0.5 \text{ ppm (800 MHz)}$
 $\Delta\omega = 2500 \text{ s}^{-1}$
 $K_d = 20 \text{ }\mu\text{M}$

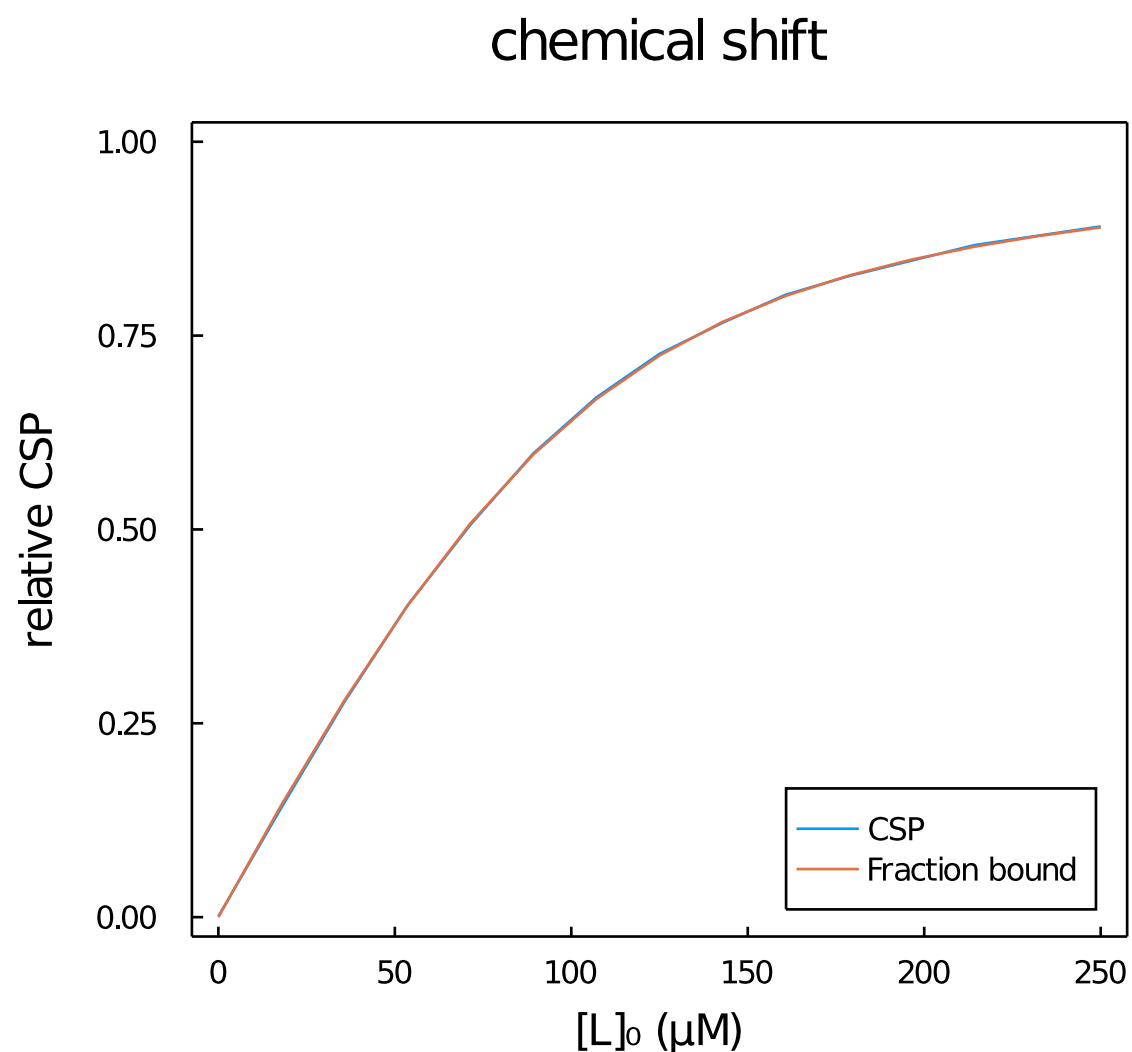
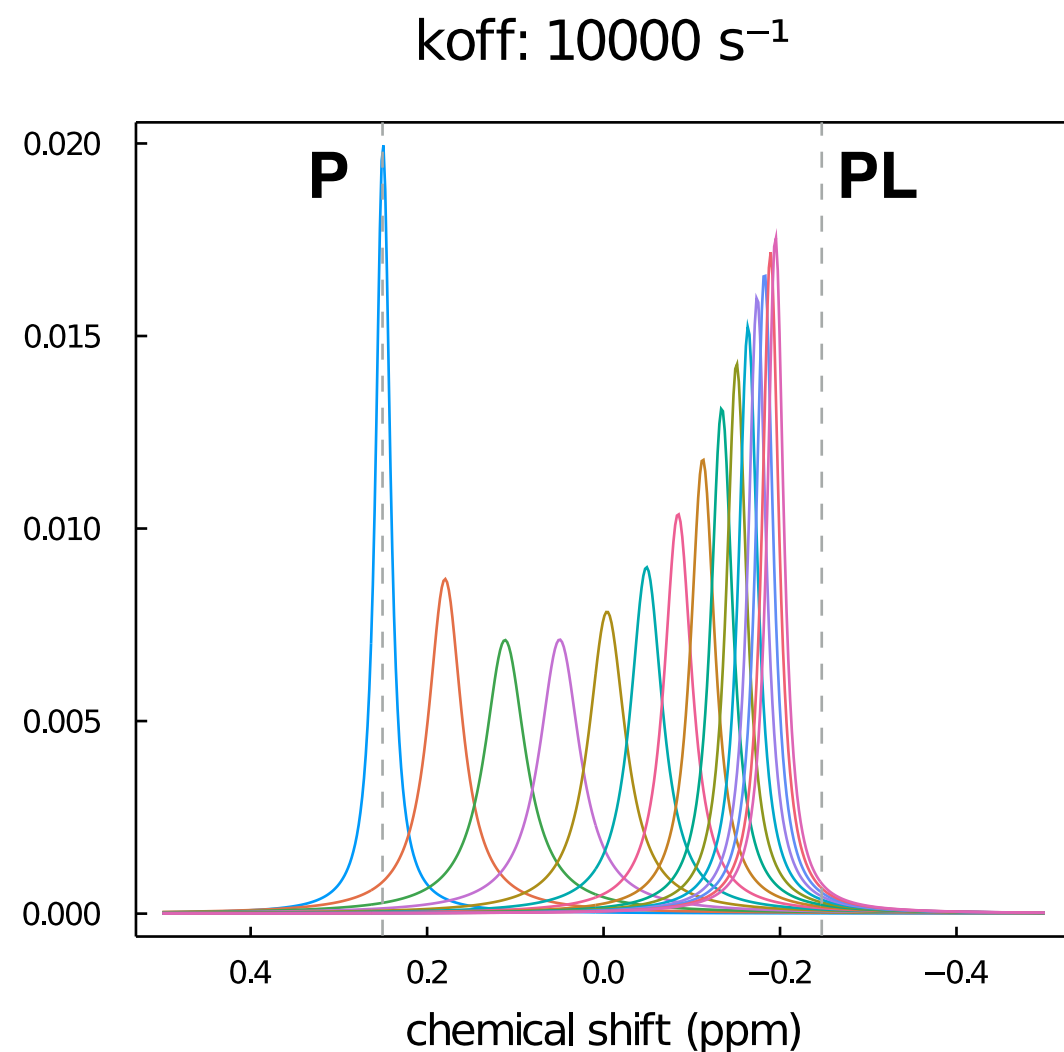
$[\text{P}]_0 = 100 \text{ }\mu\text{M}$
 $[\text{L}]_0 = 0 - 250 \text{ }\mu\text{M}$

Titration experiments: fast exchange



CSPs strongly correlated
with fraction bound (easy to
analyse)

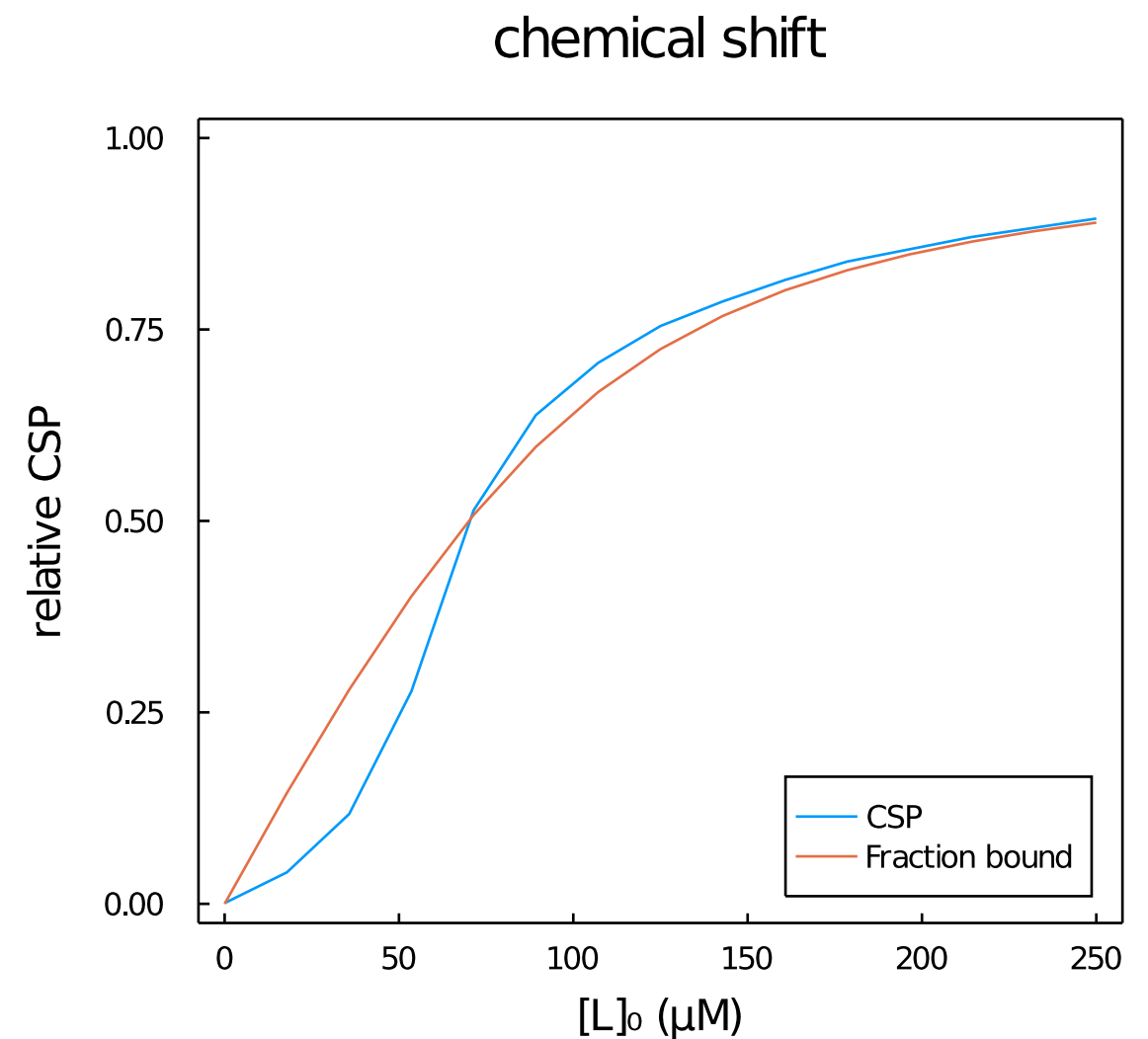
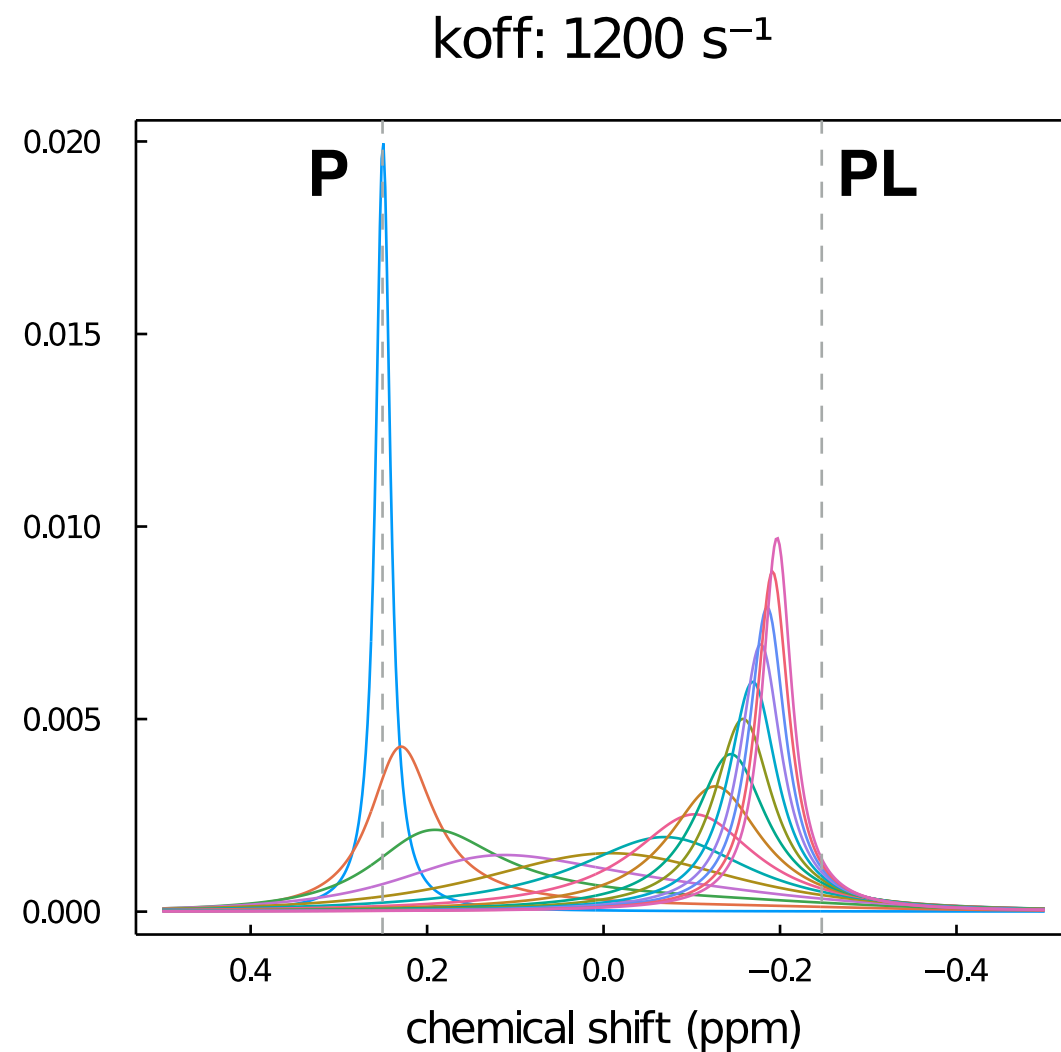
Titration experiments: fast exchange



Exchange
broadening

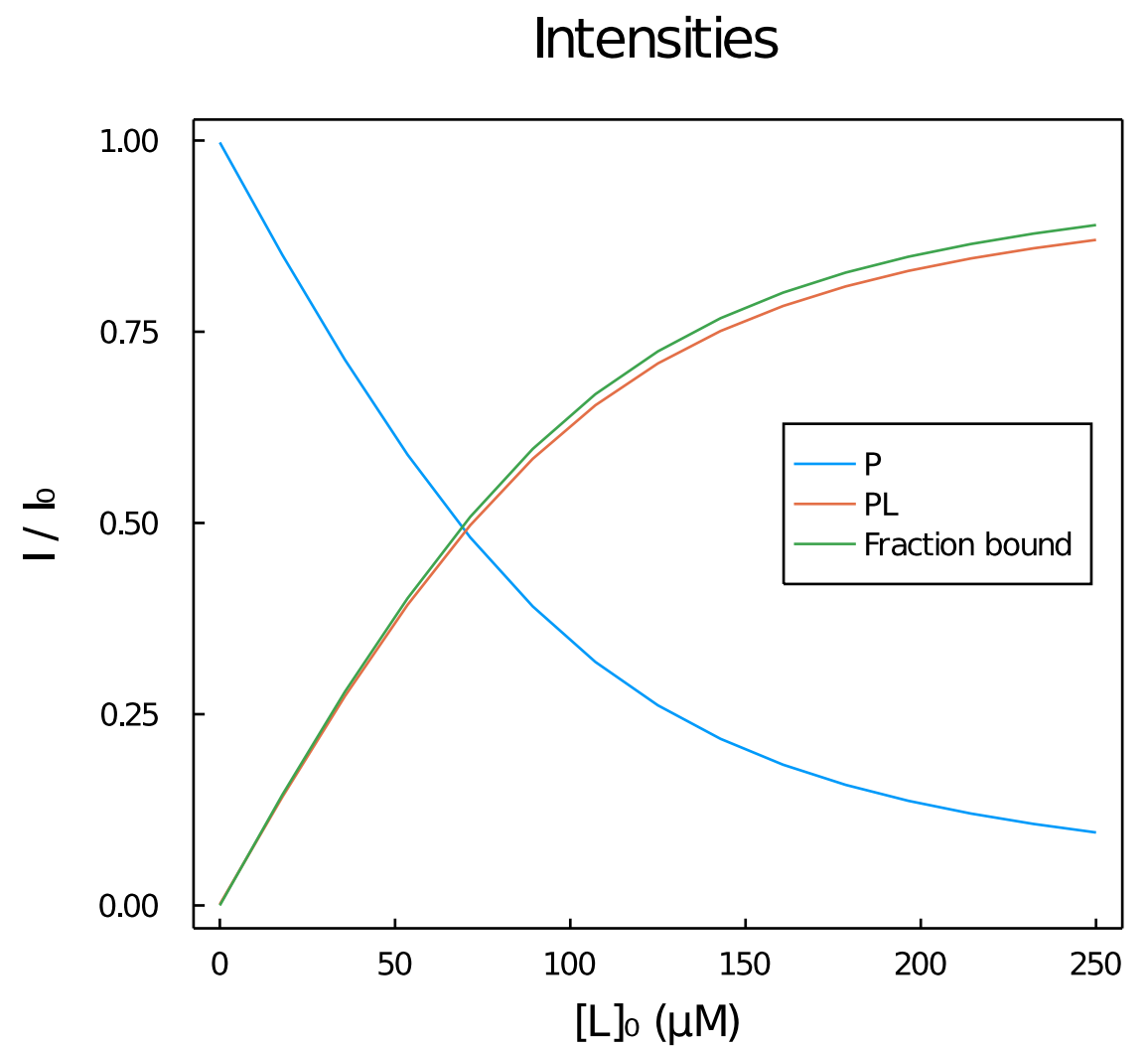
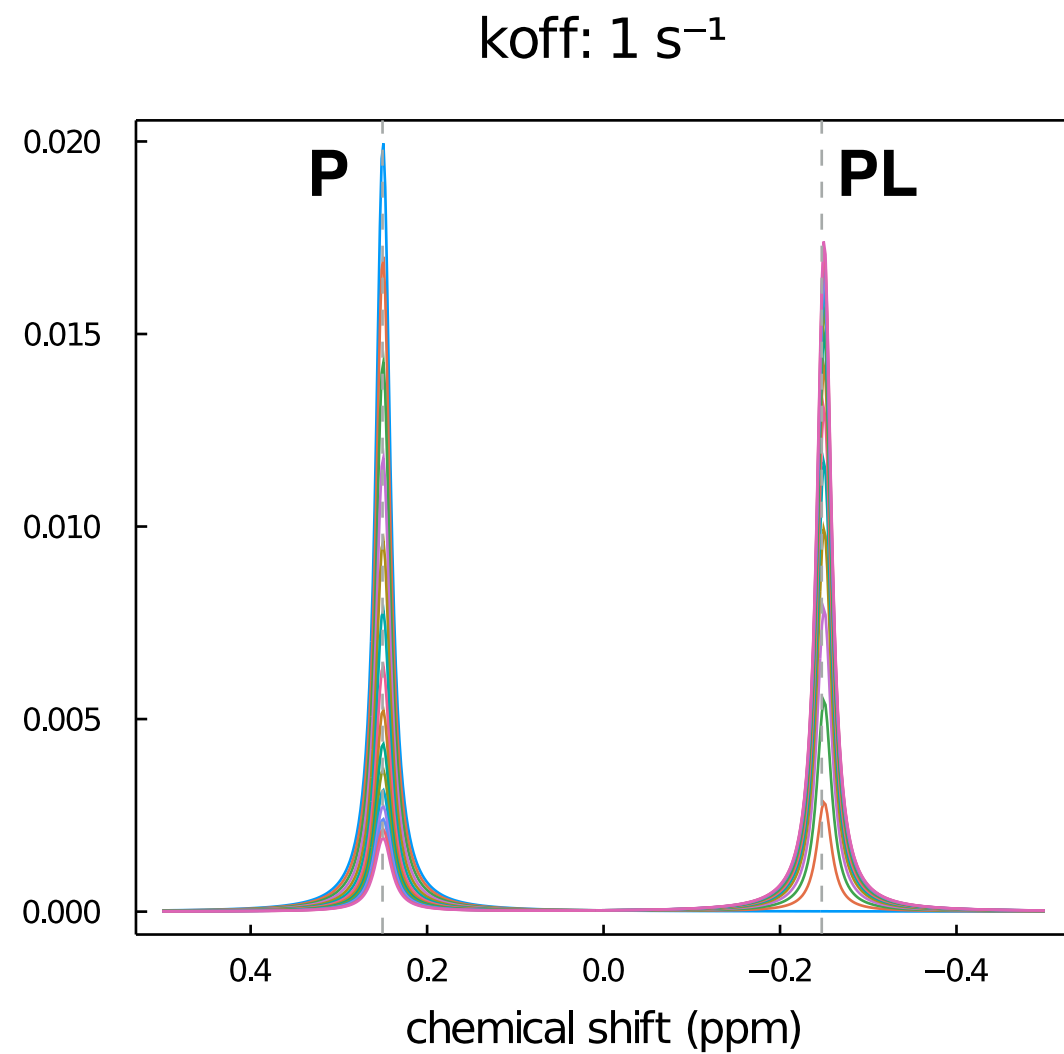
$$R_{\text{ex}} = \frac{p_A p_B}{k_{\text{ex}}} \Delta\omega^2$$

Titration experiments: intermediate exchange

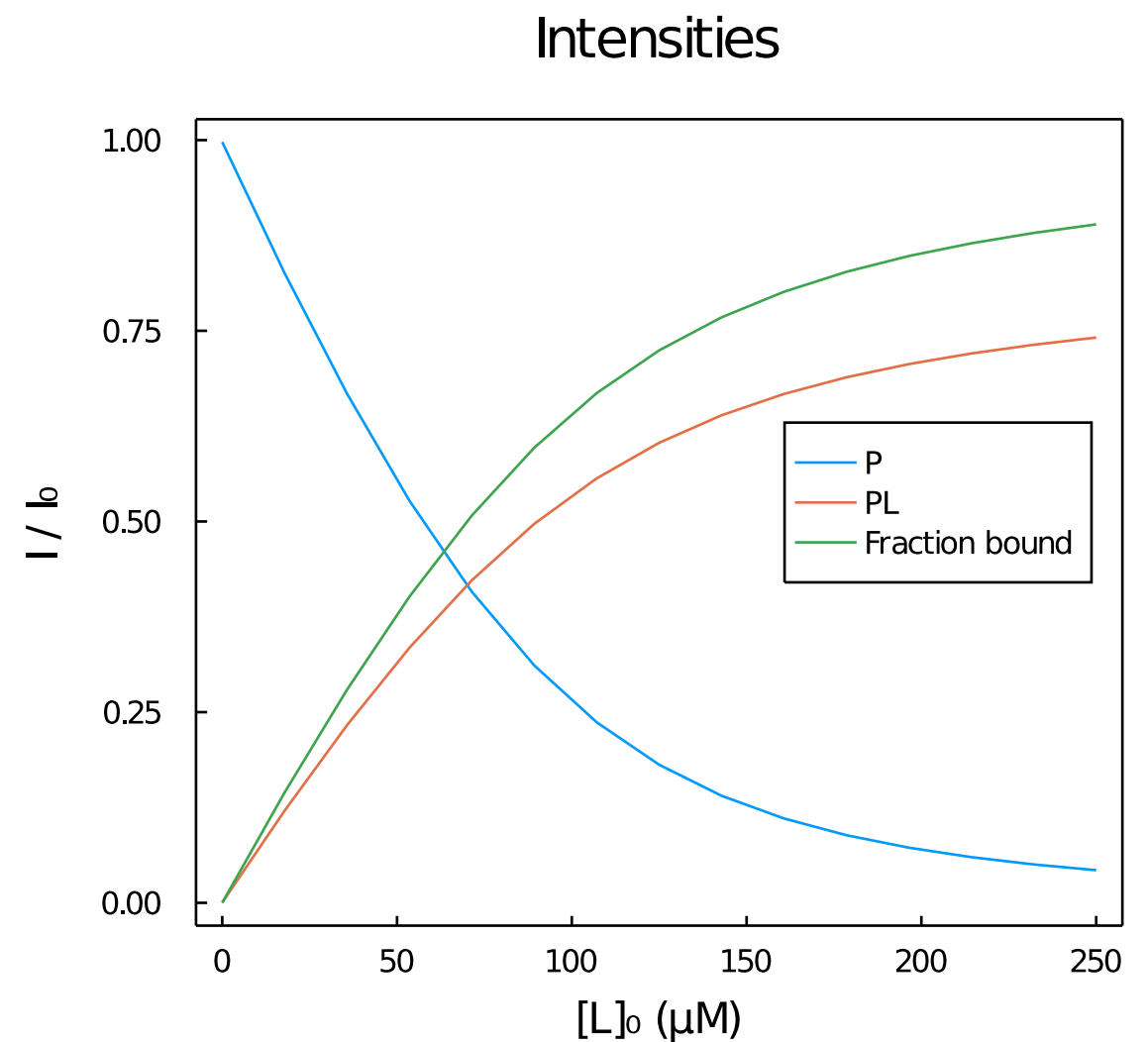
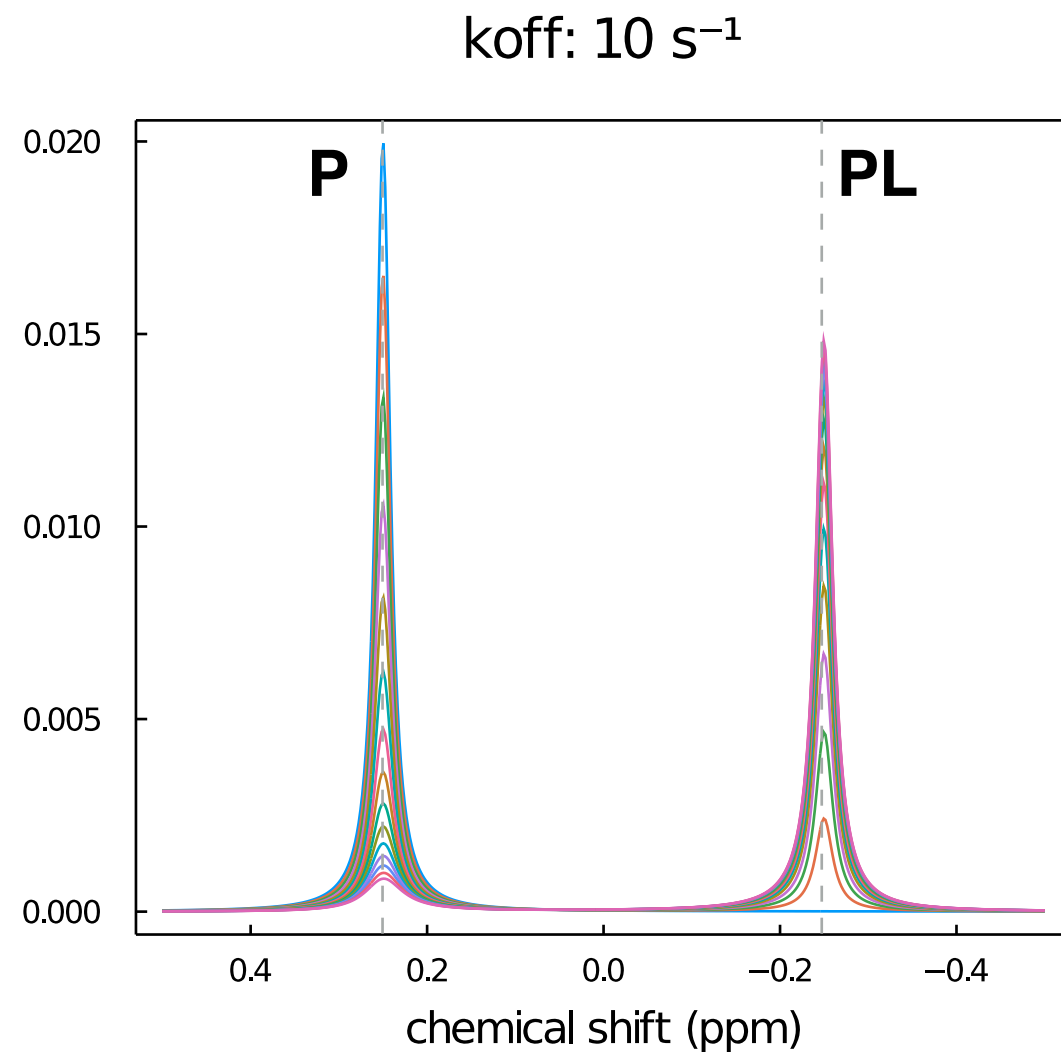


CSPs are no longer a good reporter of fraction bound

Titration experiments: slow exchange

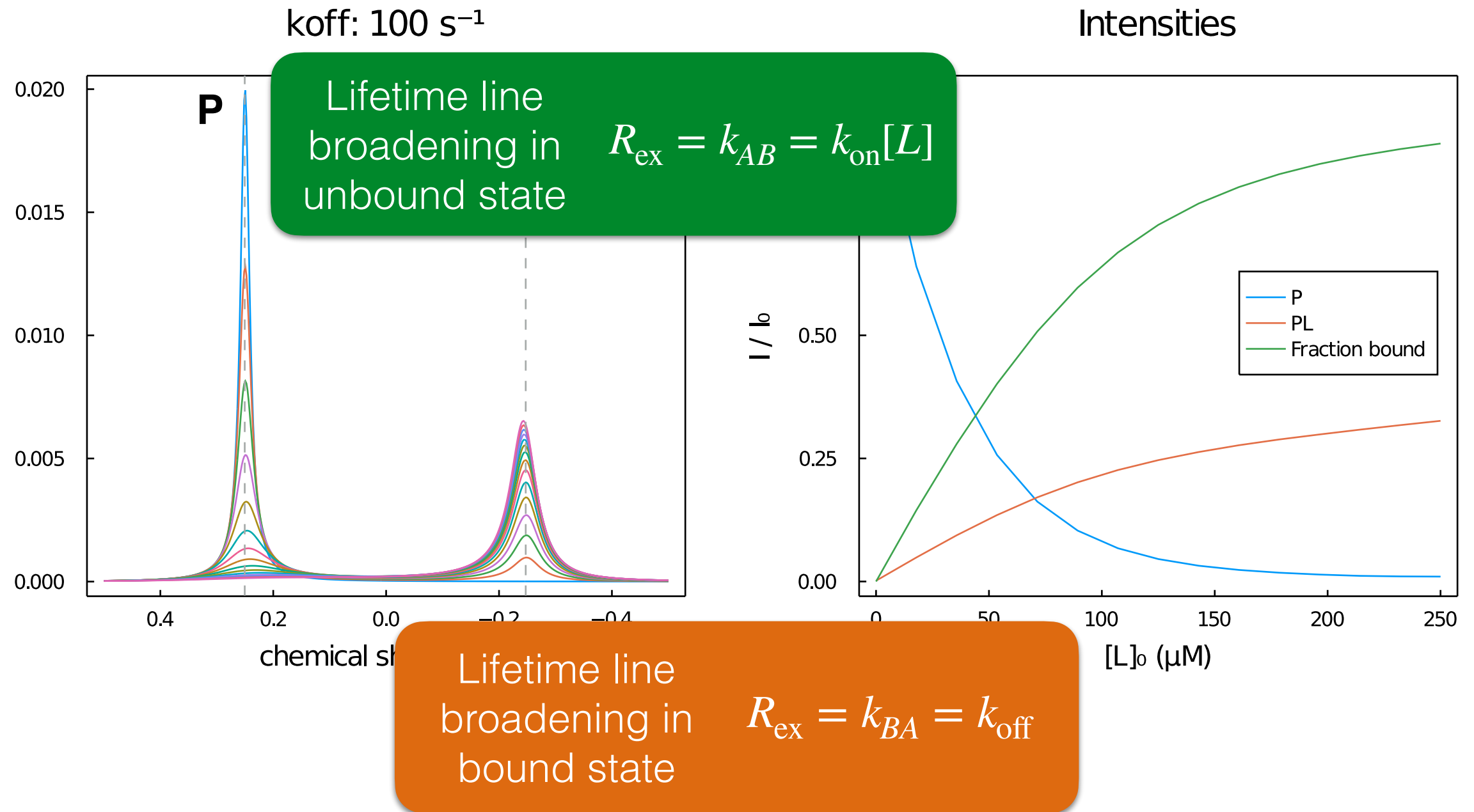


Titration experiments: slow exchange

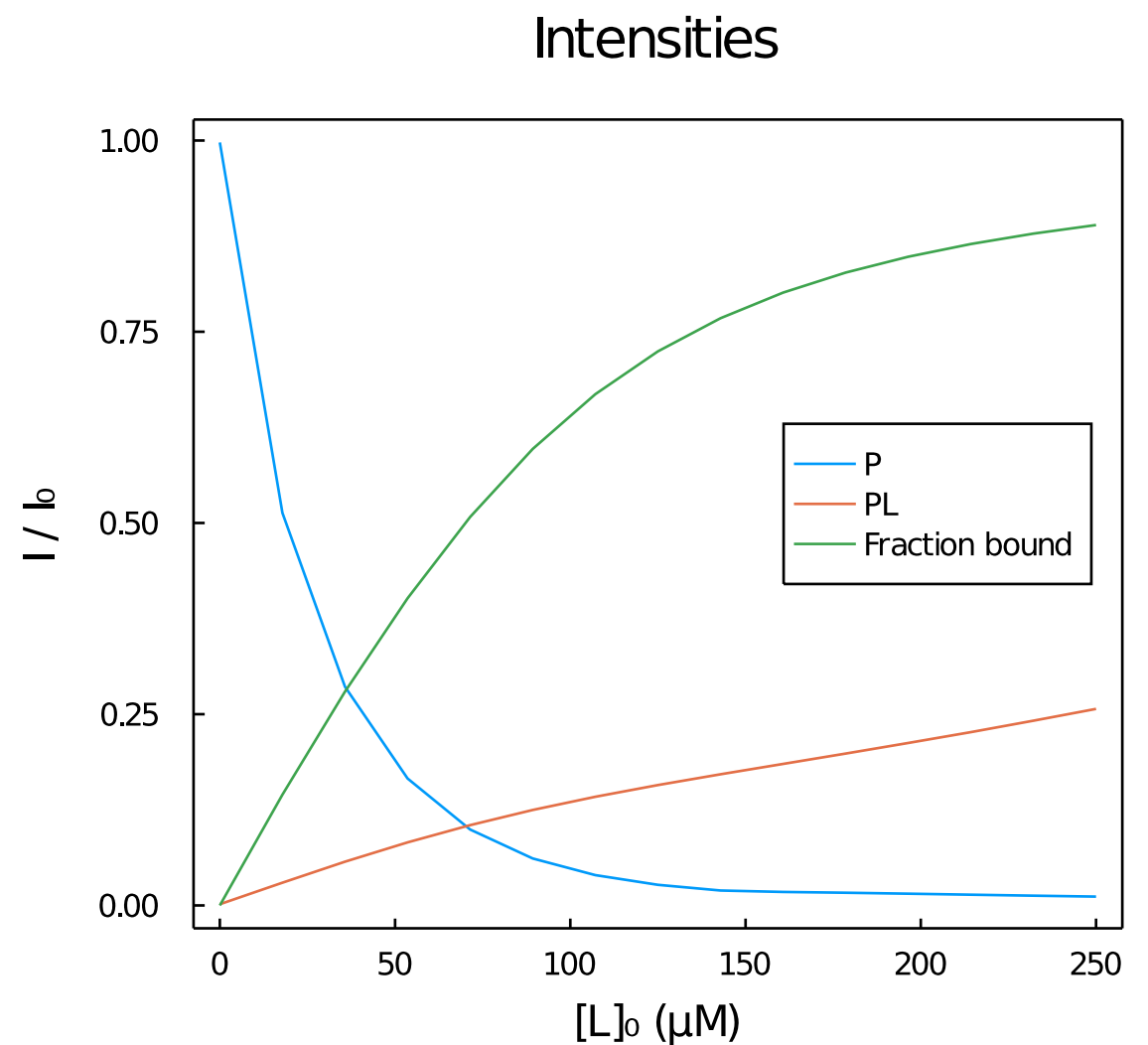
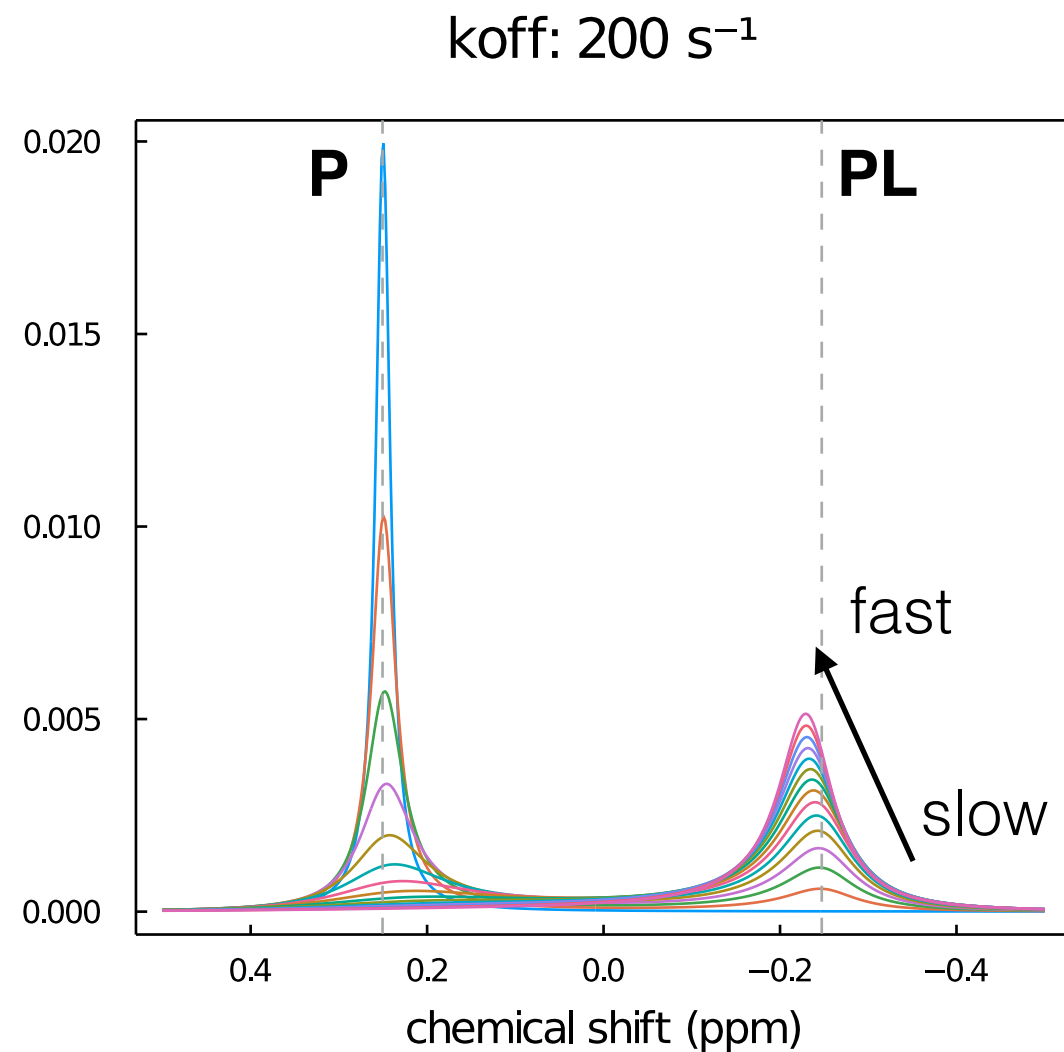


Peak intensities may not be a good measure of fraction bound

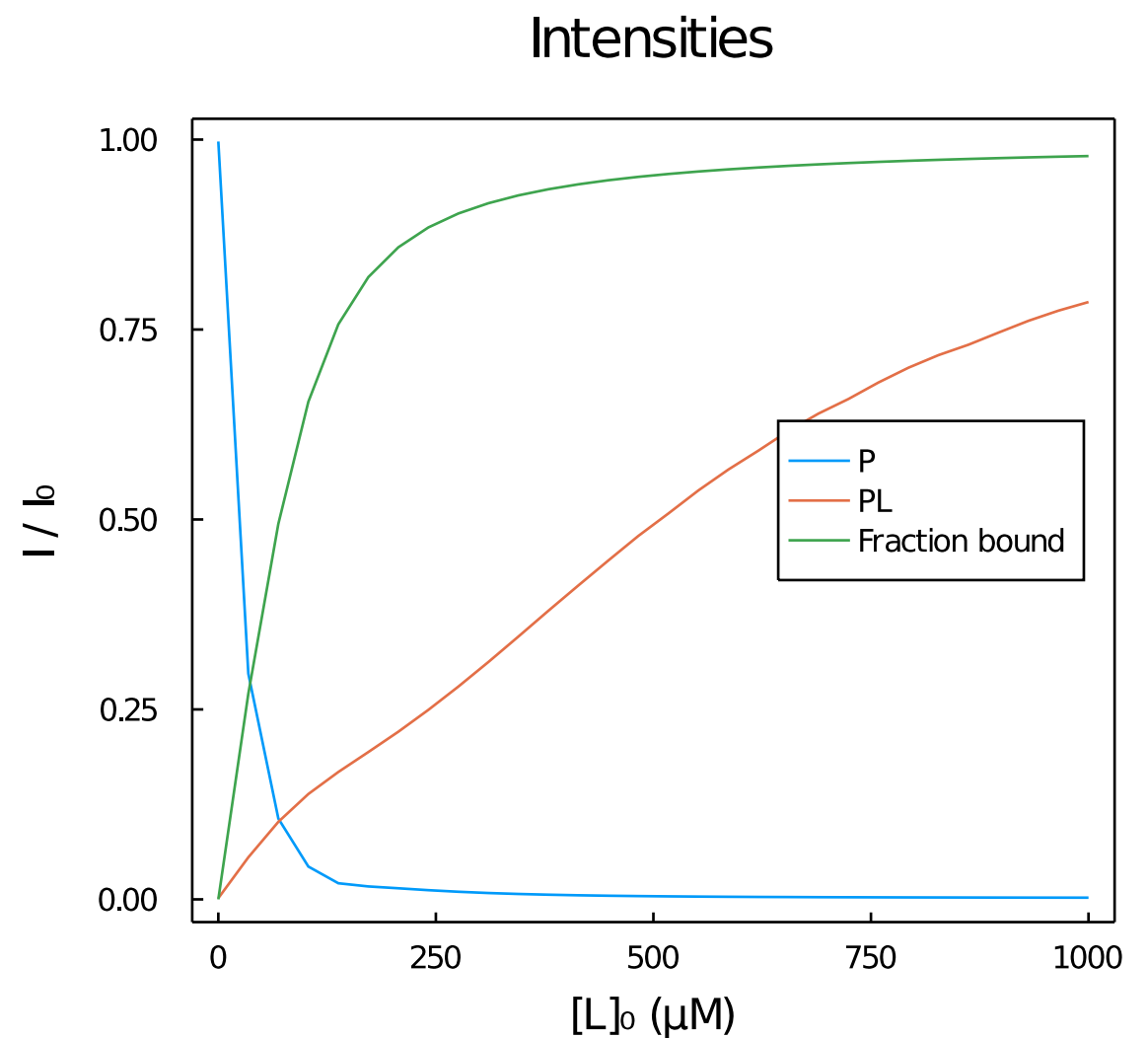
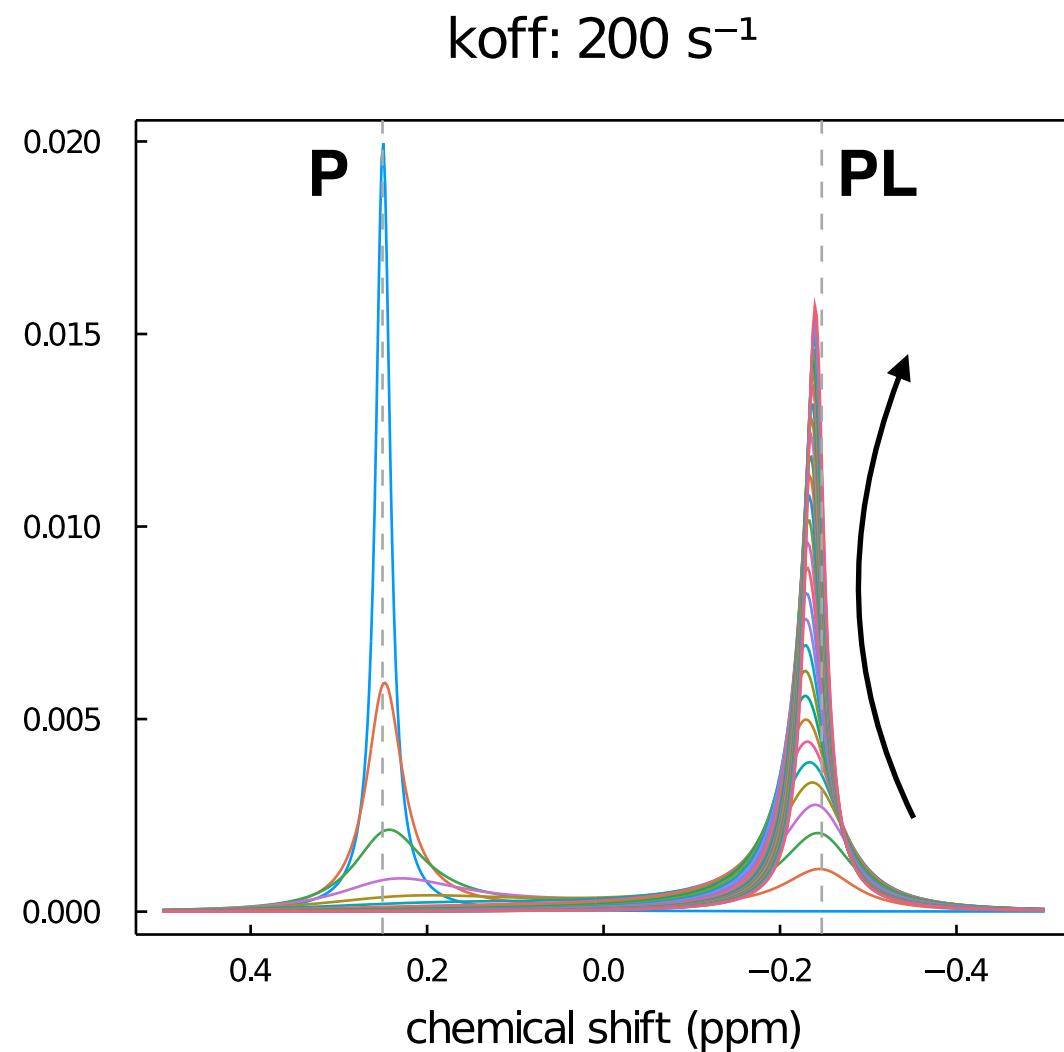
Titration experiments: slow exchange



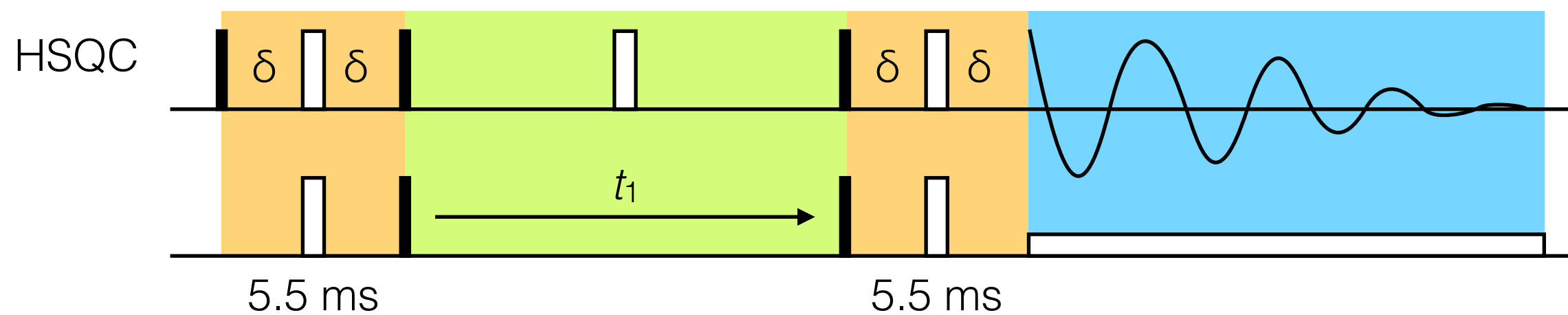
Titration experiments: cross-over effects



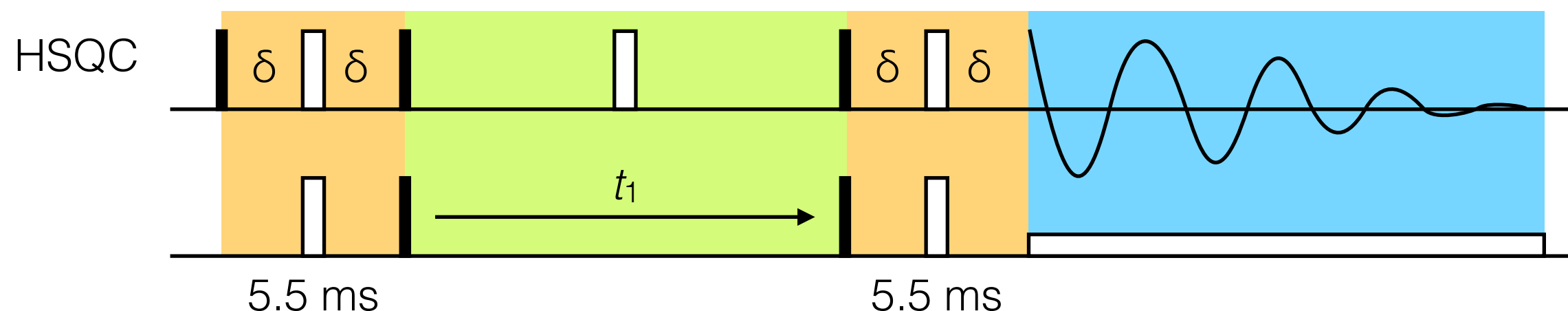
Titration experiments: cross-over effects



Chemical exchange in 2D experiments



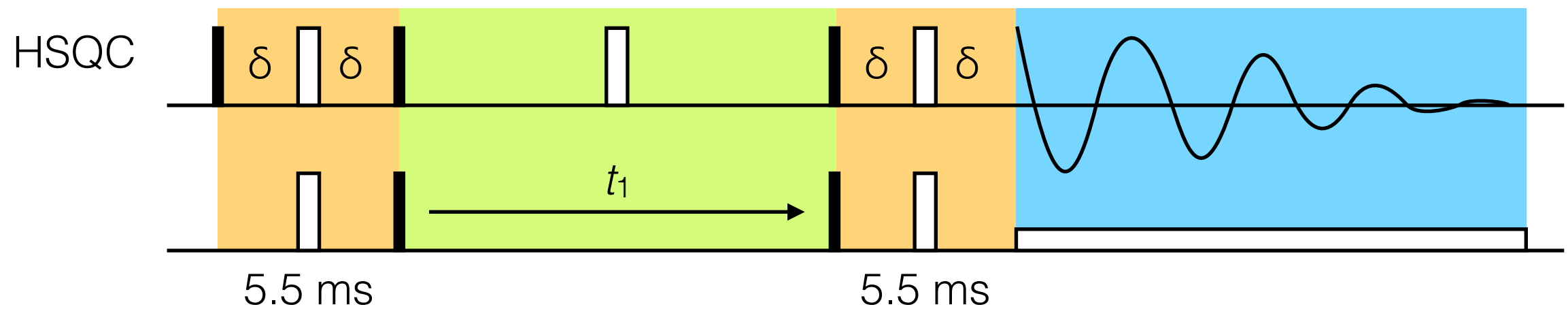
Chemical exchange in 2D experiments



Impact of chemical exchange on cross peak intensities is more significant than in 1D experiments – twice as many opportunities to lose signal!

$$I = I_0 \cdot (\text{relaxation loss during CTPs}) \cdot \frac{1}{R_{2,0}^{\text{indirect}} + R_{ex}^{\text{indirect}}} \cdot \frac{1}{R_{2,0}^{\text{direct}} + R_{ex}^{\text{direct}}}$$

Chemical exchange in 2D experiments

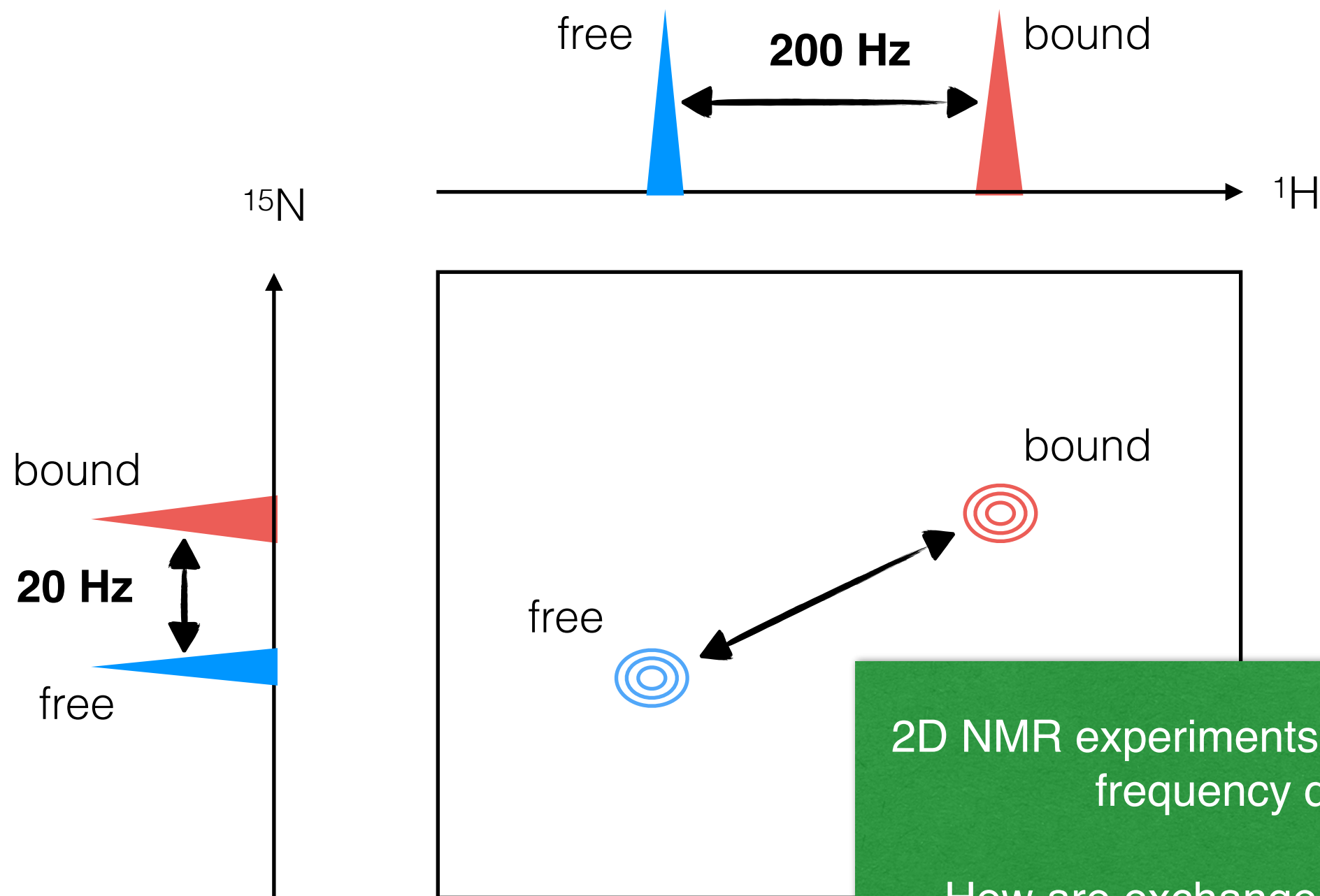


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$$I = I_0 \cdot (\text{relaxation loss during CTPs}) \cdot \frac{1}{R_{2,0}^{\text{indirect}} + R_{ex}^{\text{indirect}}} \cdot \frac{1}{R_{2,0}^{\text{direct}} + R_{ex}^{\text{direct}}}$$

conversely – 2D experiments can be much more sensitive probes of exchange

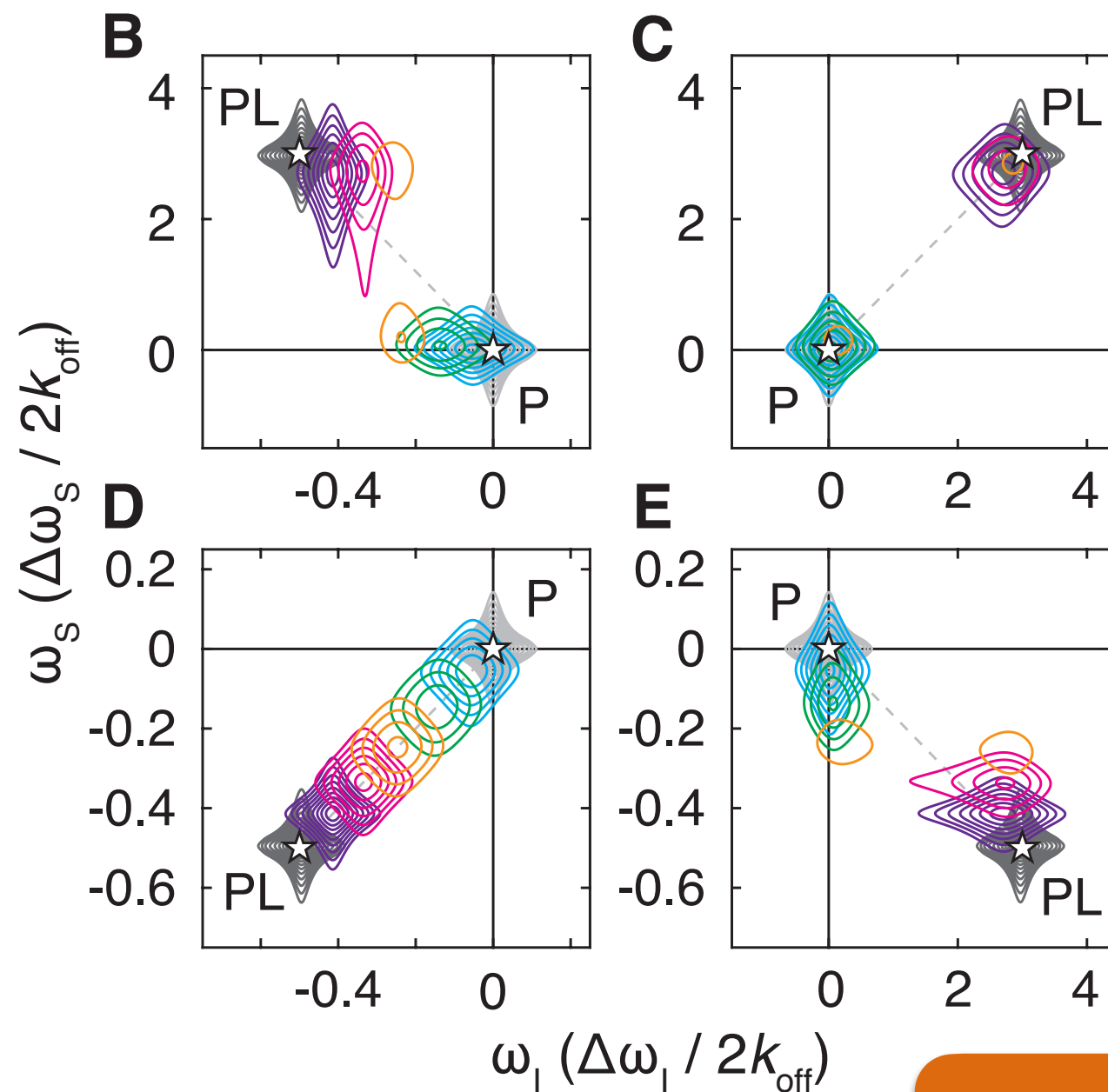
Chemical exchange regimes in 2D experiments



2D NMR experiments involve two different frequency differences

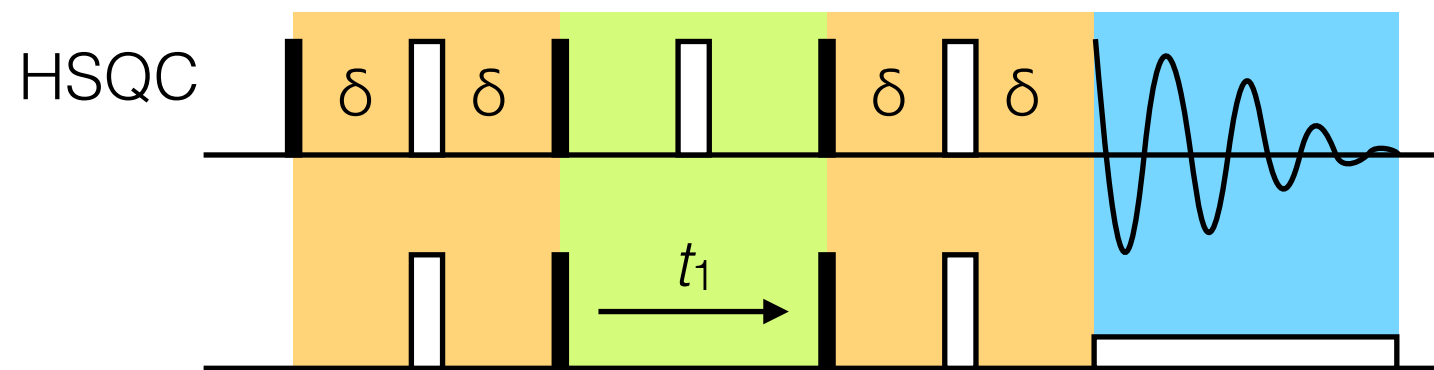
How are exchange regimes defined?

Chemical exchange regimes in HSQC experiments



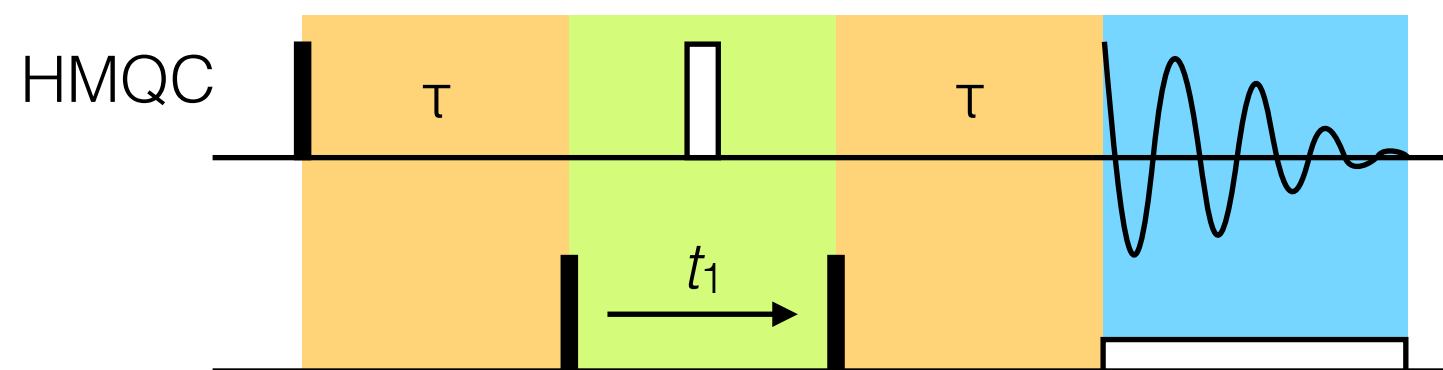
Exchange can be fast or slow with respect to both direct and indirect chemical shift differences

Different pulse programs have different exchange effects



Magnetisation is SQ during t_1

=> chemical exchange effects depend on $\Delta\omega^{\text{SQ}}$ vs k_{ex}

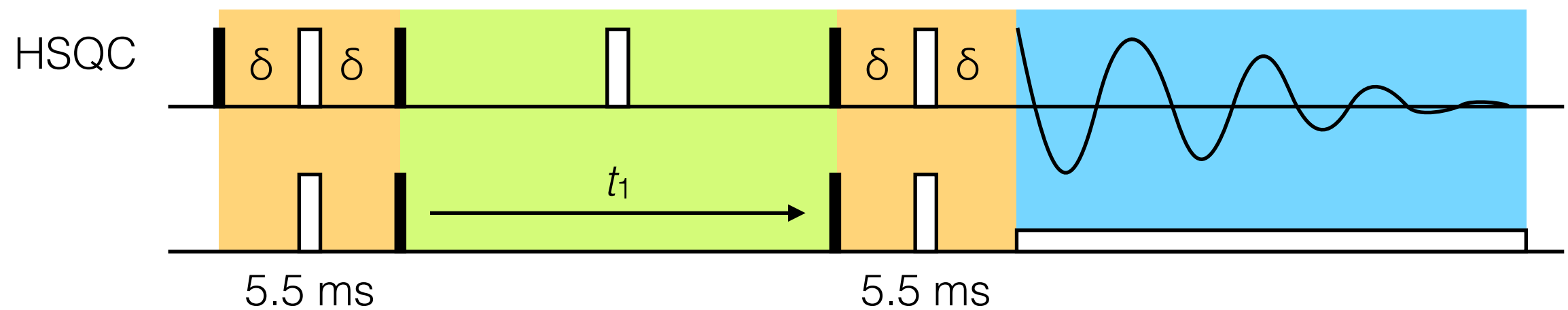


Magnetisation is a mixture of ZQ and DQ coherences during t_1

=> chemical exchange effects depend on *both* $\Delta\omega^{\text{ZQ}}$ and $\Delta\omega^{\text{DQ}}$ vs k_{ex}

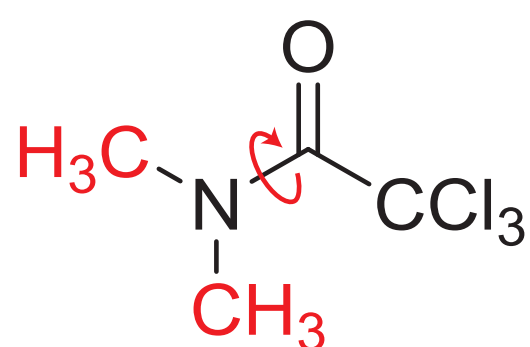
In general, HMQC is more sensitive to chemical exchange than HSQC

Unexpected exchange cross-peaks in 2D experiments

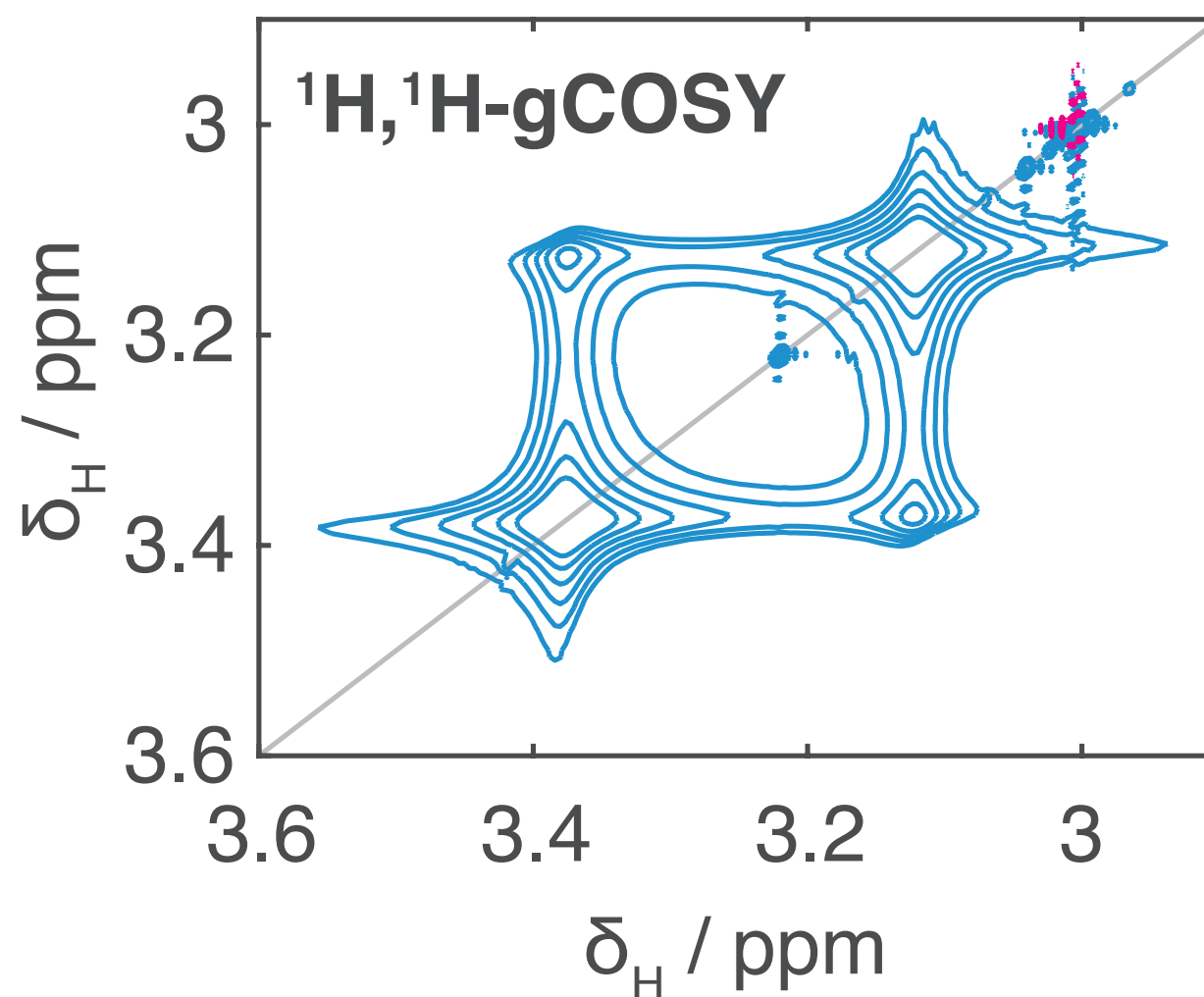
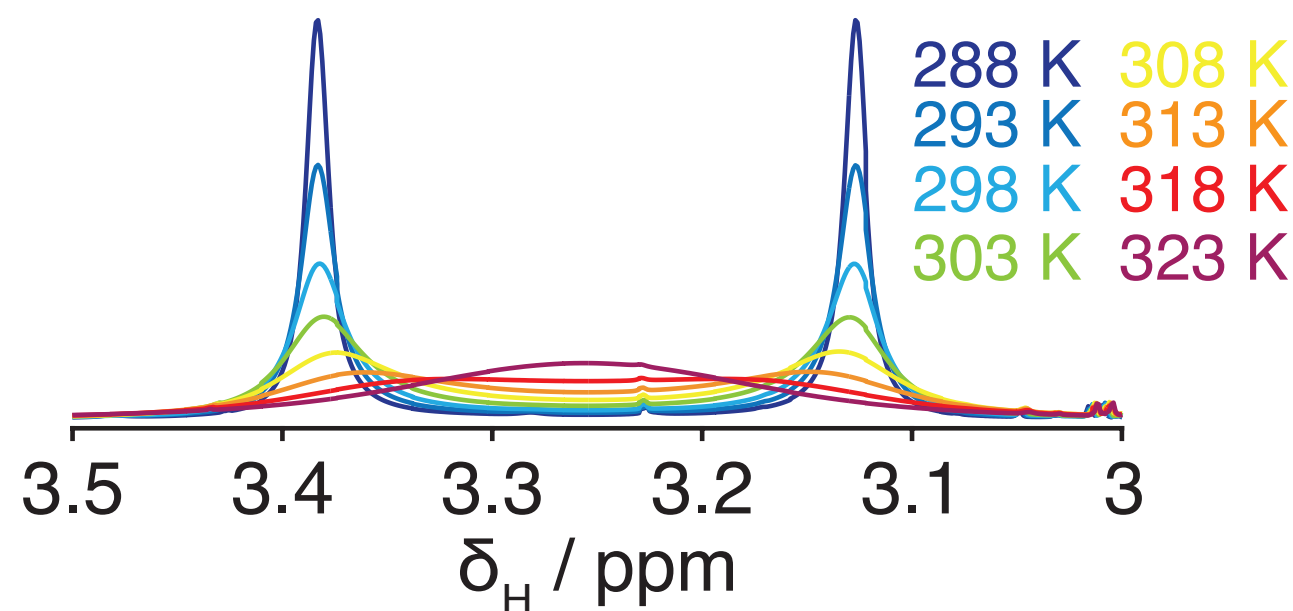


*Chemical exchange during successive evolution periods
or during coherence transfer periods can give rise to
unexpected cross-peaks in 2D experiments*

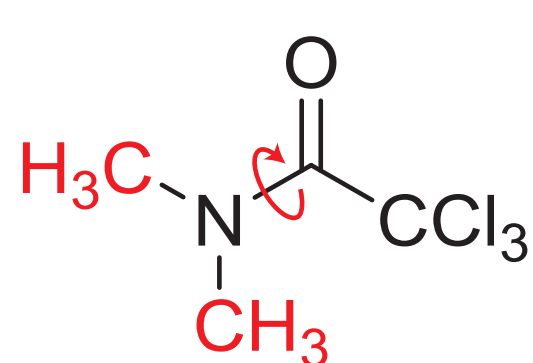
Unexpected exchange cross-peaks in 2D experiments



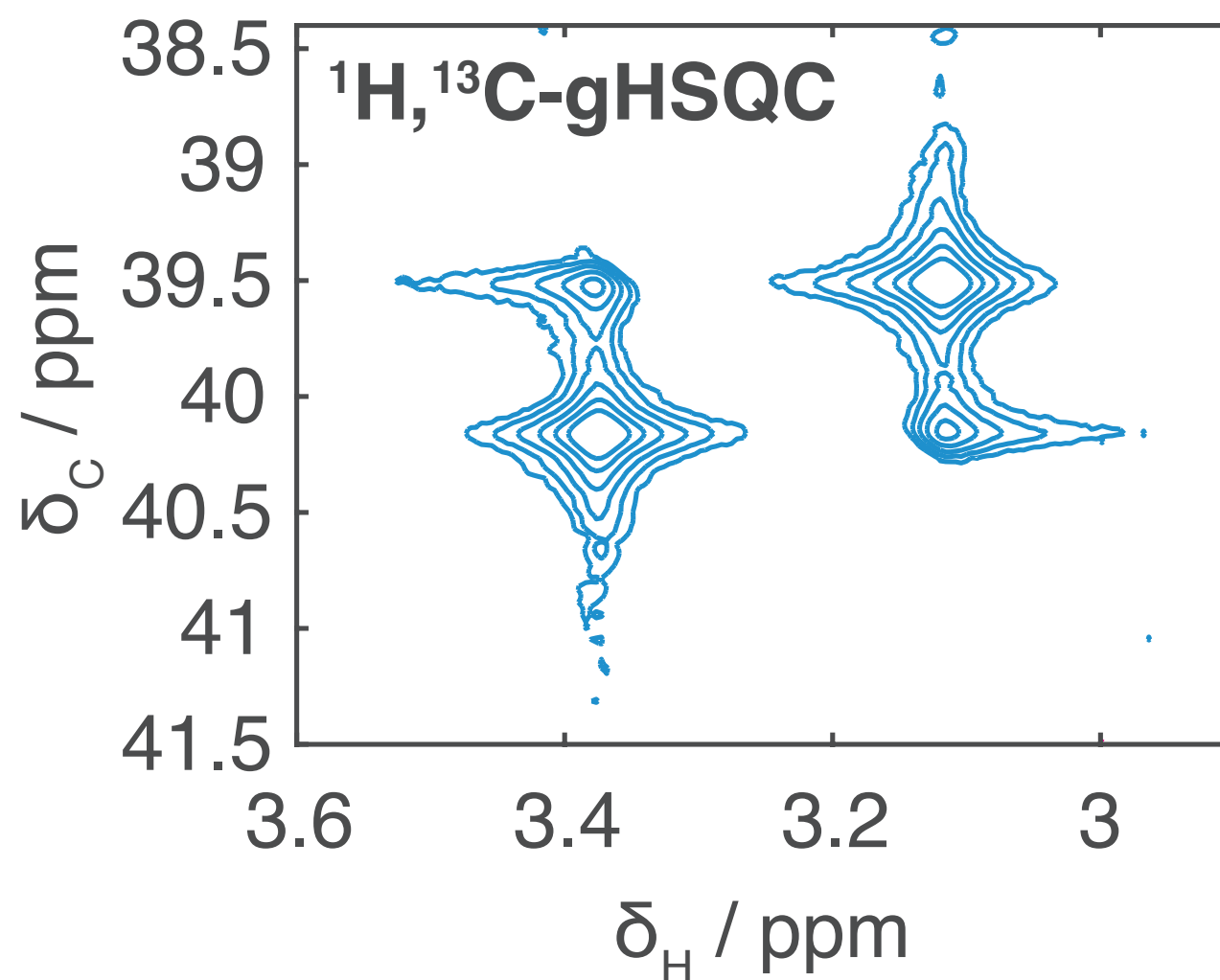
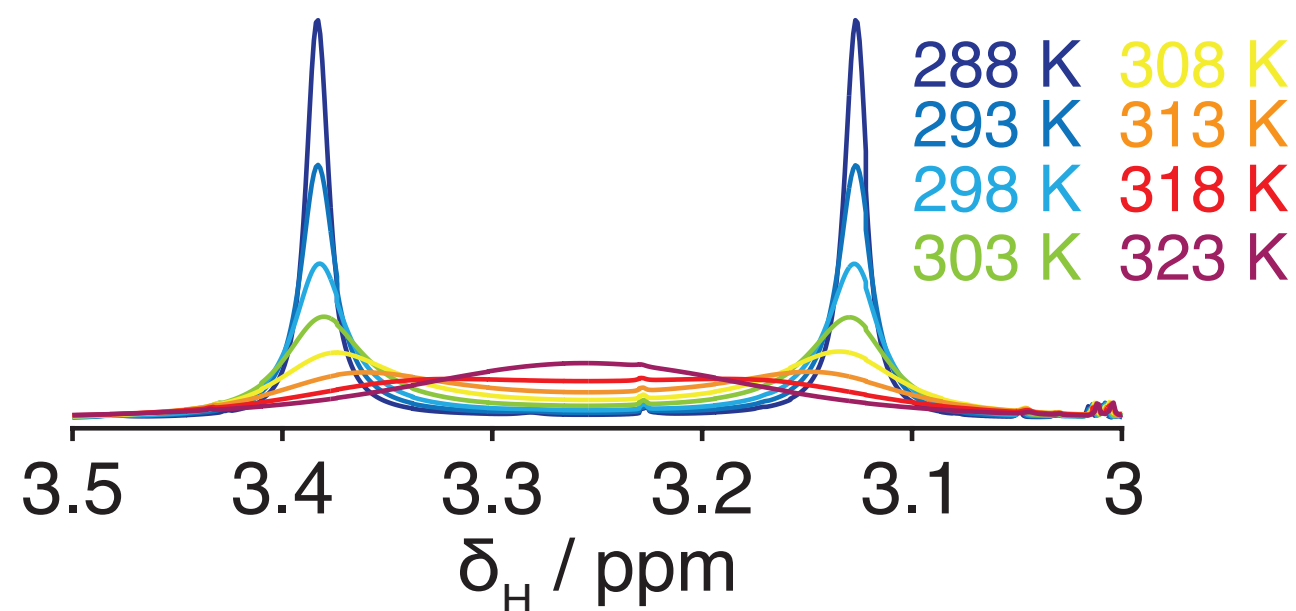
$\Delta\delta_{\text{H}} = 0.26 \text{ ppm}$
 $\Delta\delta_{\text{C}} = 0.62 \text{ ppm}$
 $^1J_{\text{CH}} = 140 \text{ Hz}$
 $k_{\text{ex}} = 125 \text{ s}^{-1}$
 (298 K)



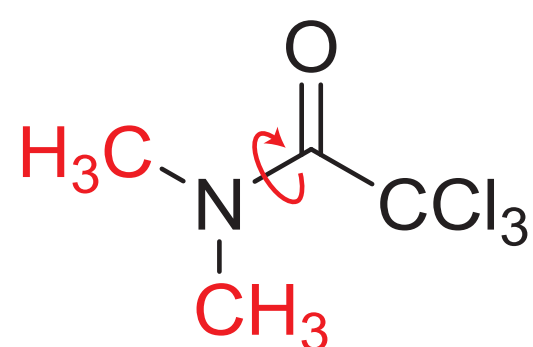
Unexpected exchange cross-peaks in 2D experiments



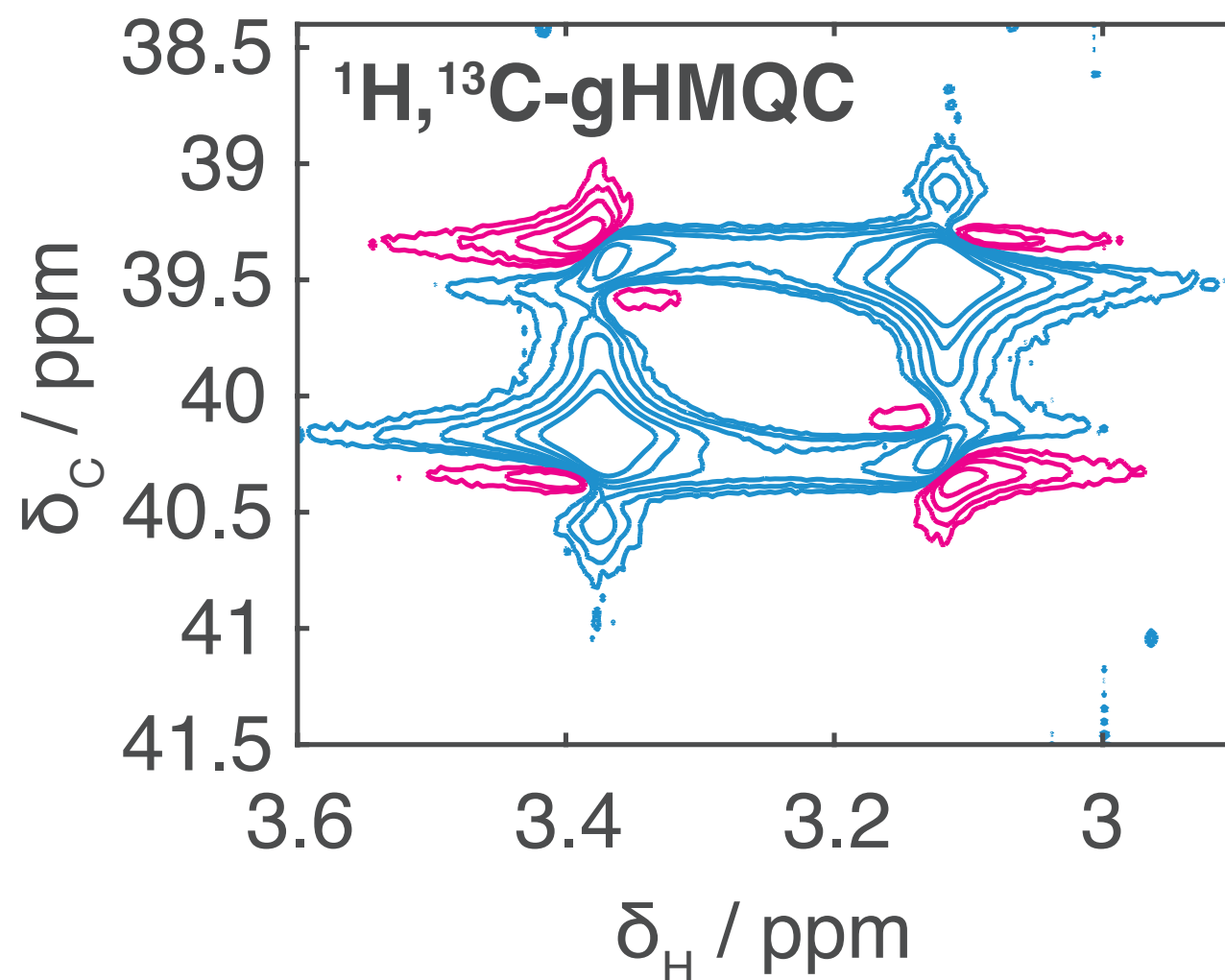
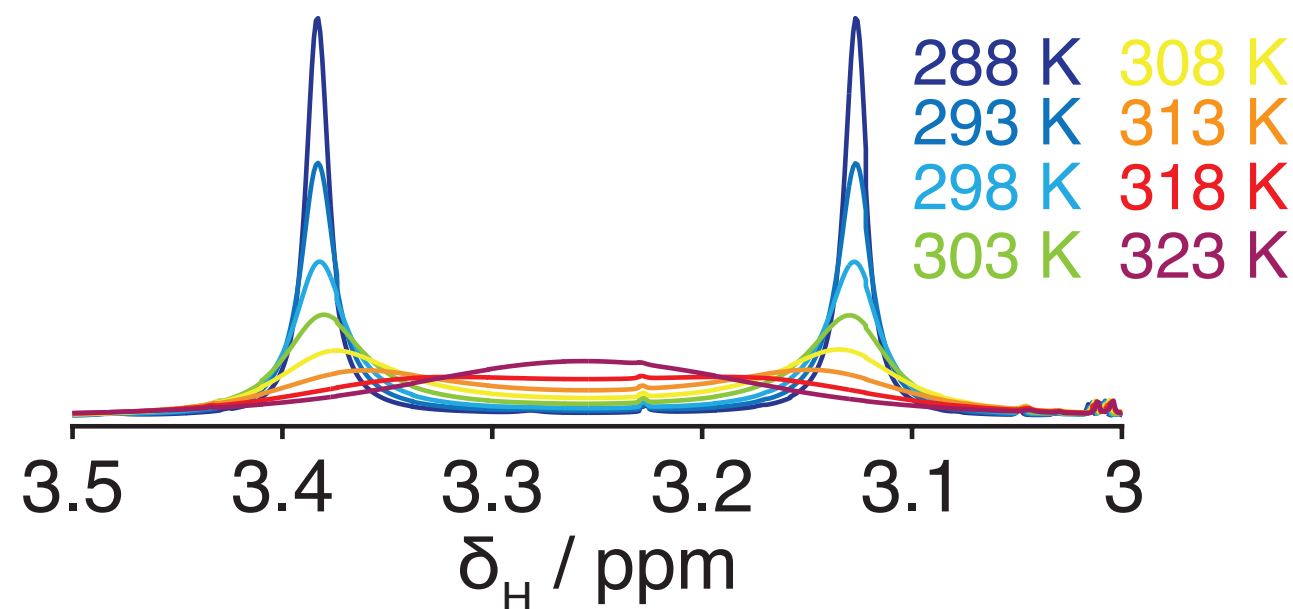
$\Delta\delta_{\text{H}} = 0.26 \text{ ppm}$
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 $^1J_{\text{CH}} = 140 \text{ Hz}$
 $k_{\text{ex}} = 125 \text{ s}^{-1}$
(298 K)

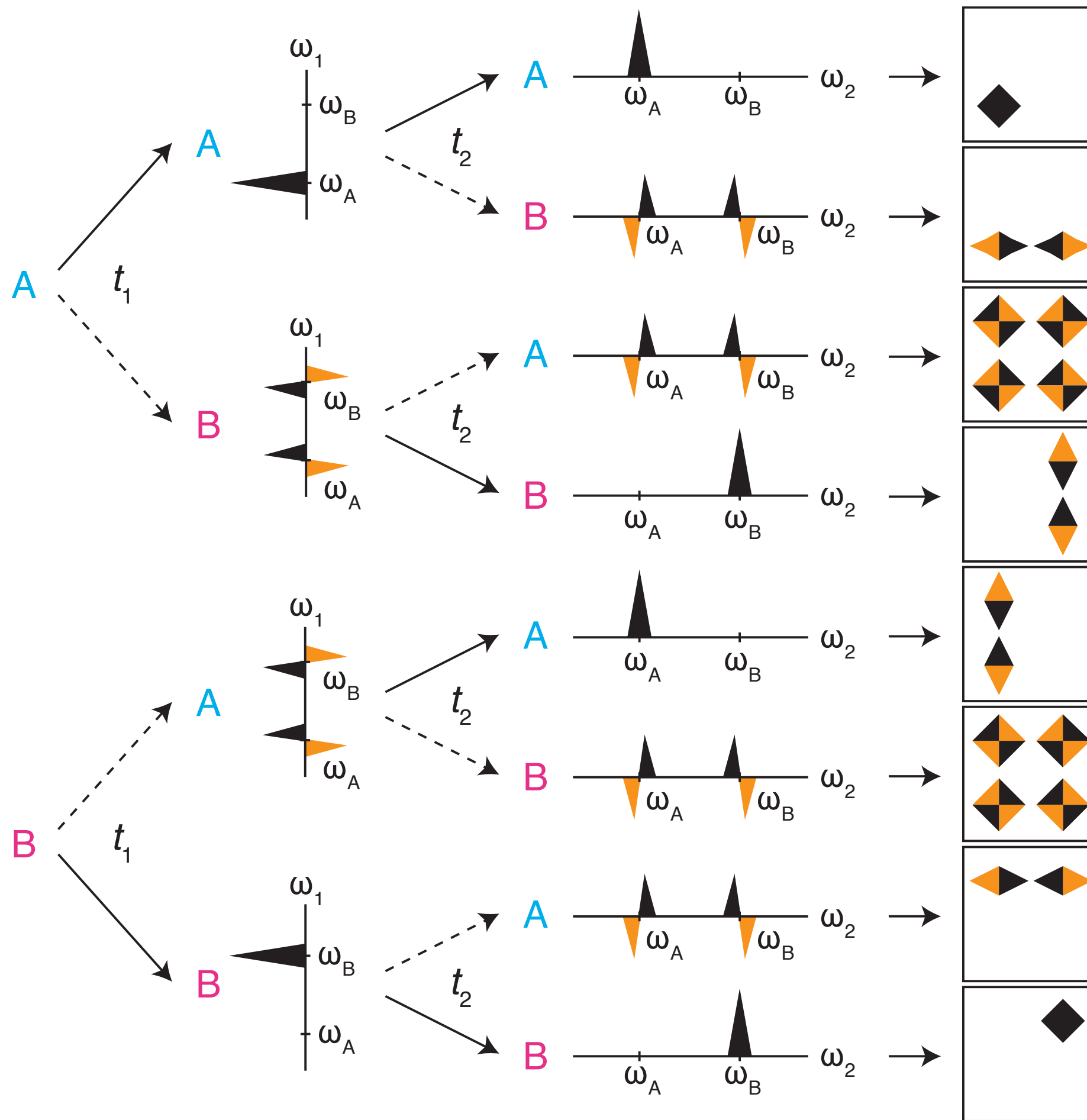


Unexpected exchange cross-peaks in 2D experiments

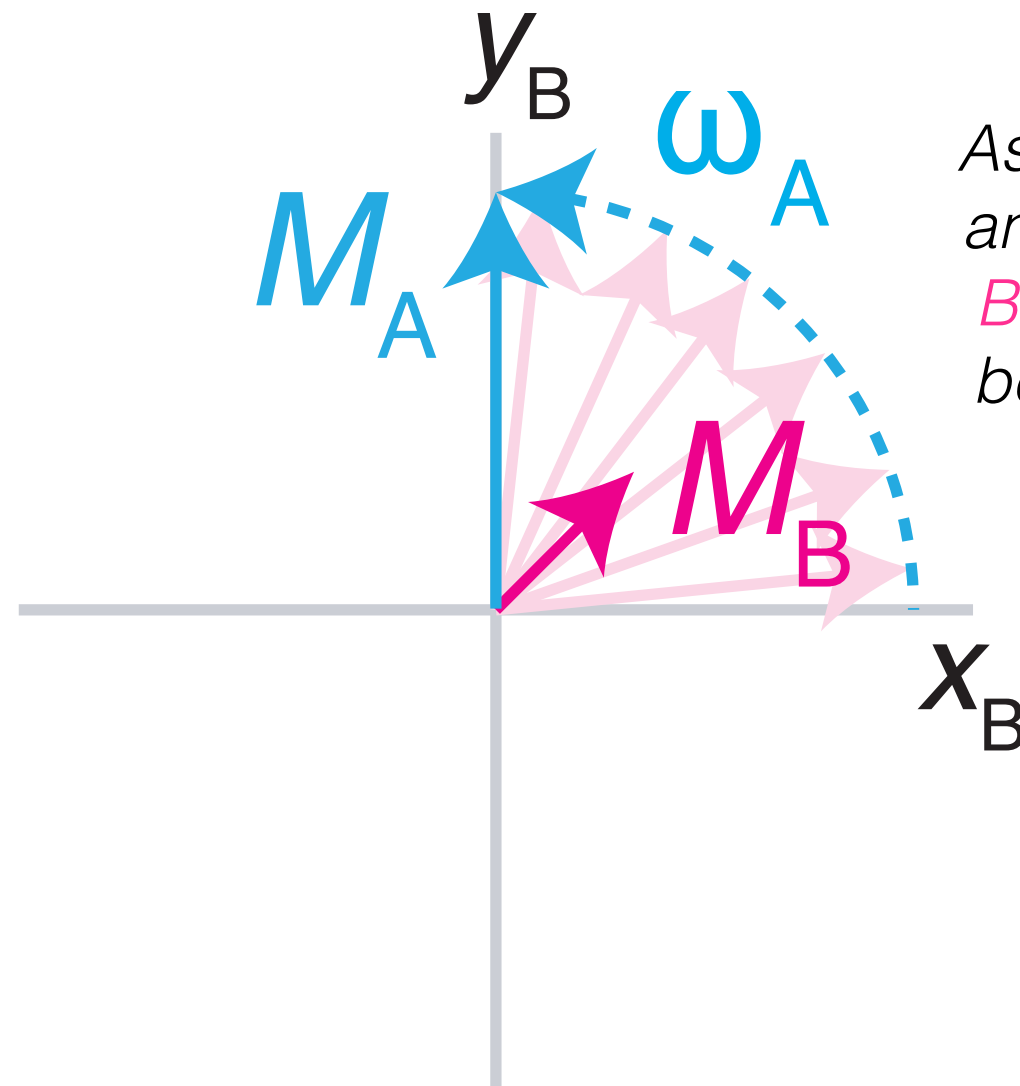


$\Delta\delta_{\text{H}} = 0.26 \text{ ppm}$
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 $^1J_{\text{CH}} = 140 \text{ Hz}$
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 (298 K)





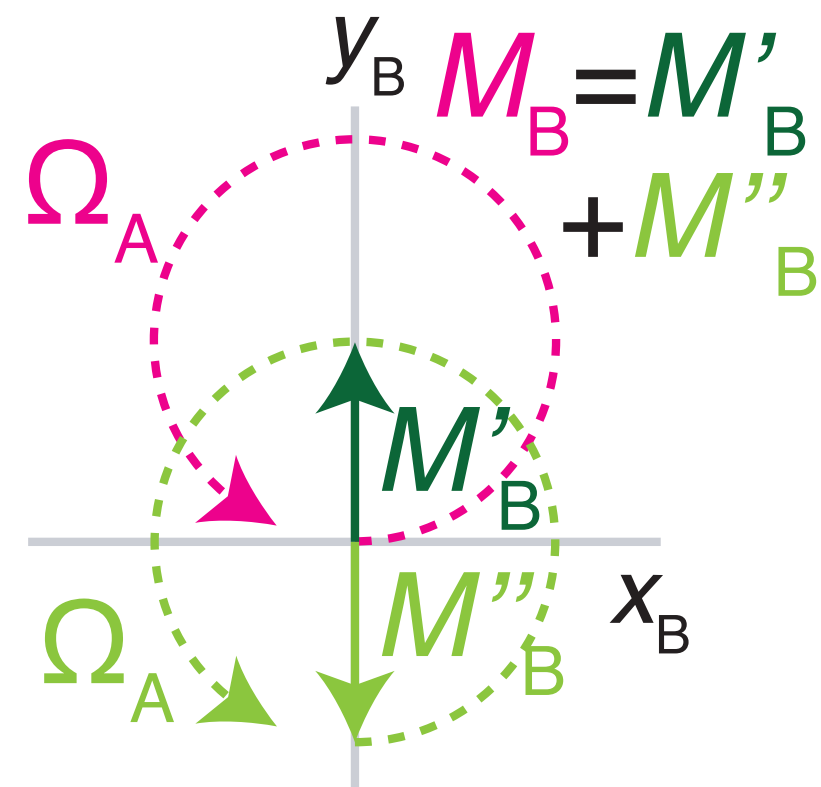
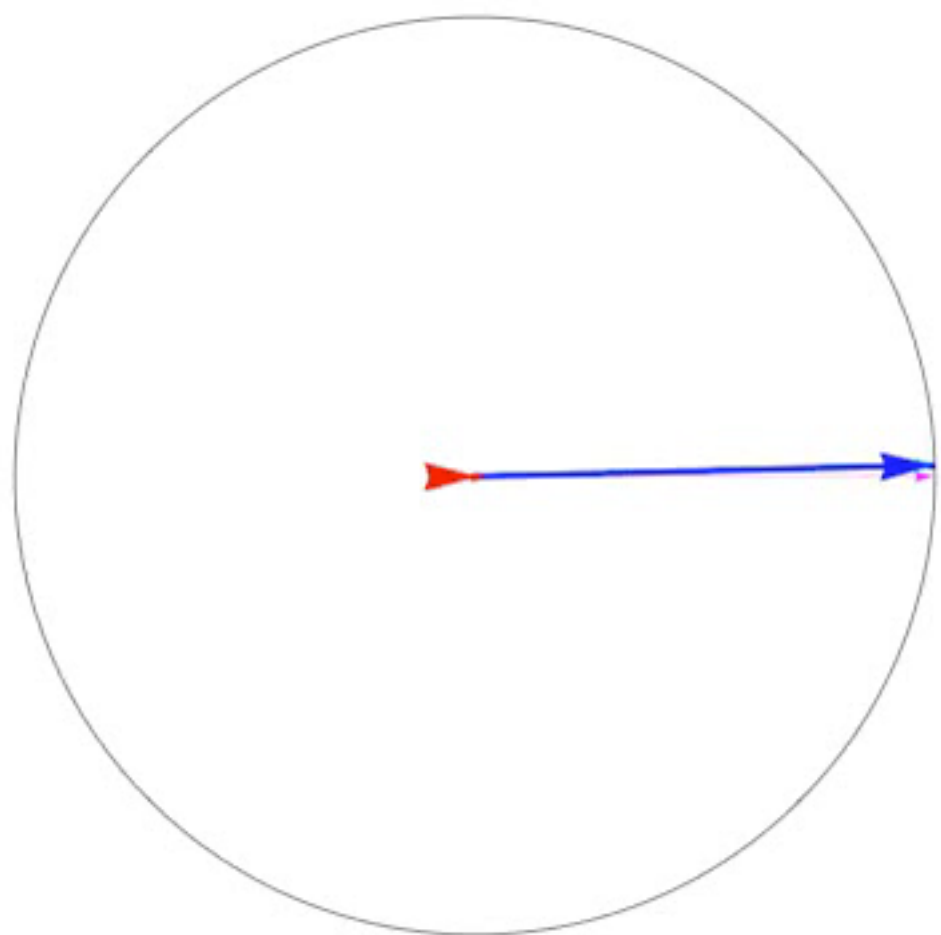
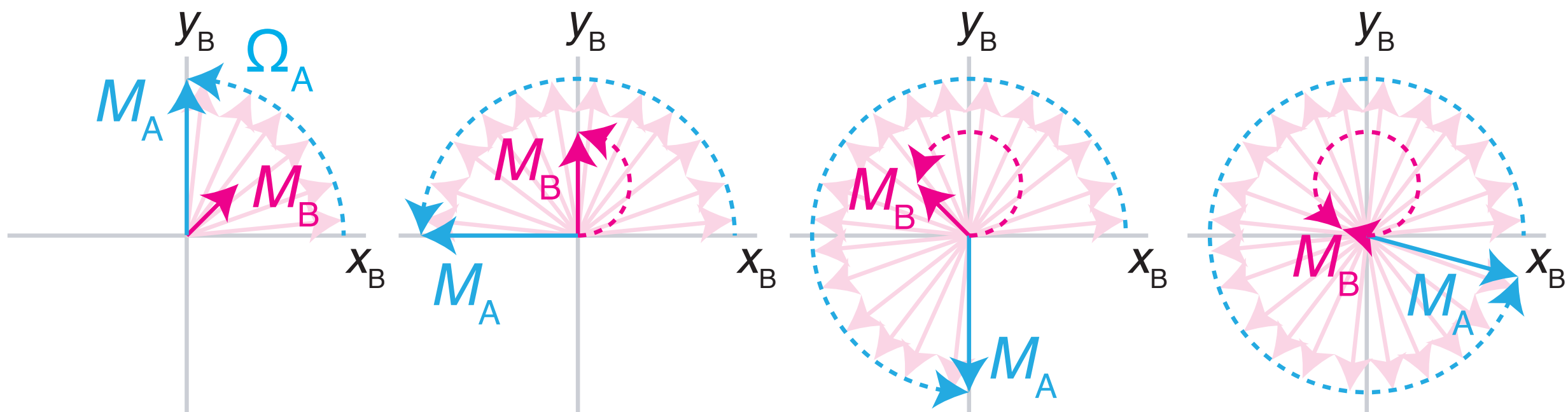
Origin of exchange-induced crosspeaks



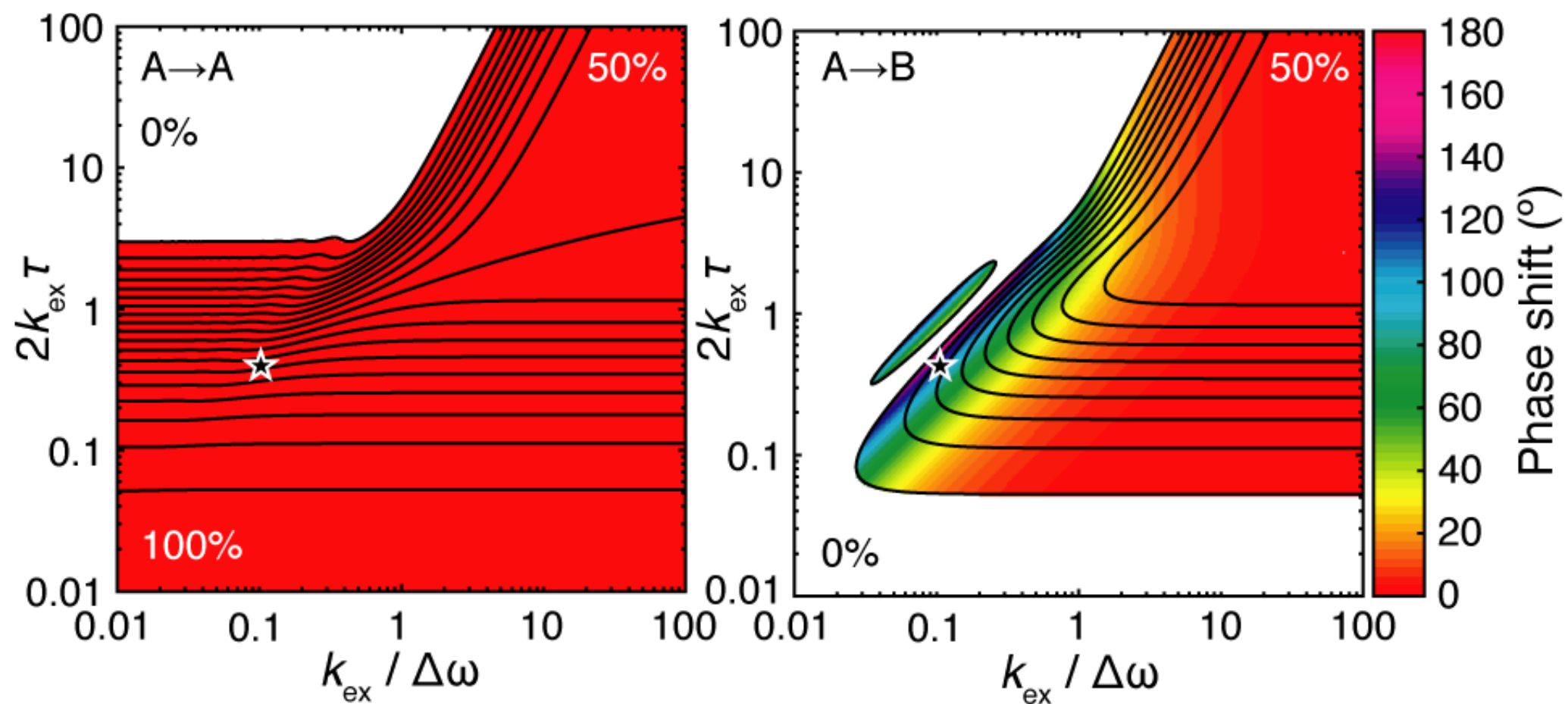
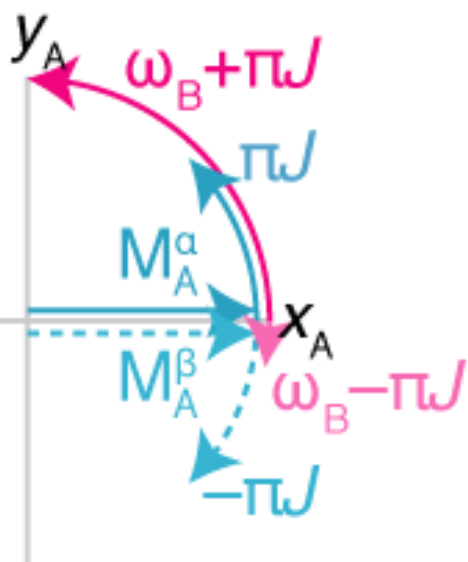
As A chemically reacts and exchanges into B, B spins are 'dropped' behind the evolving A magnetisation

Diagram shown in rotating frame of spin B

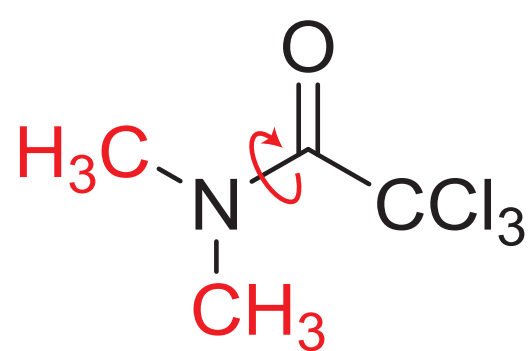
Origin of exchange-induced crosspeaks



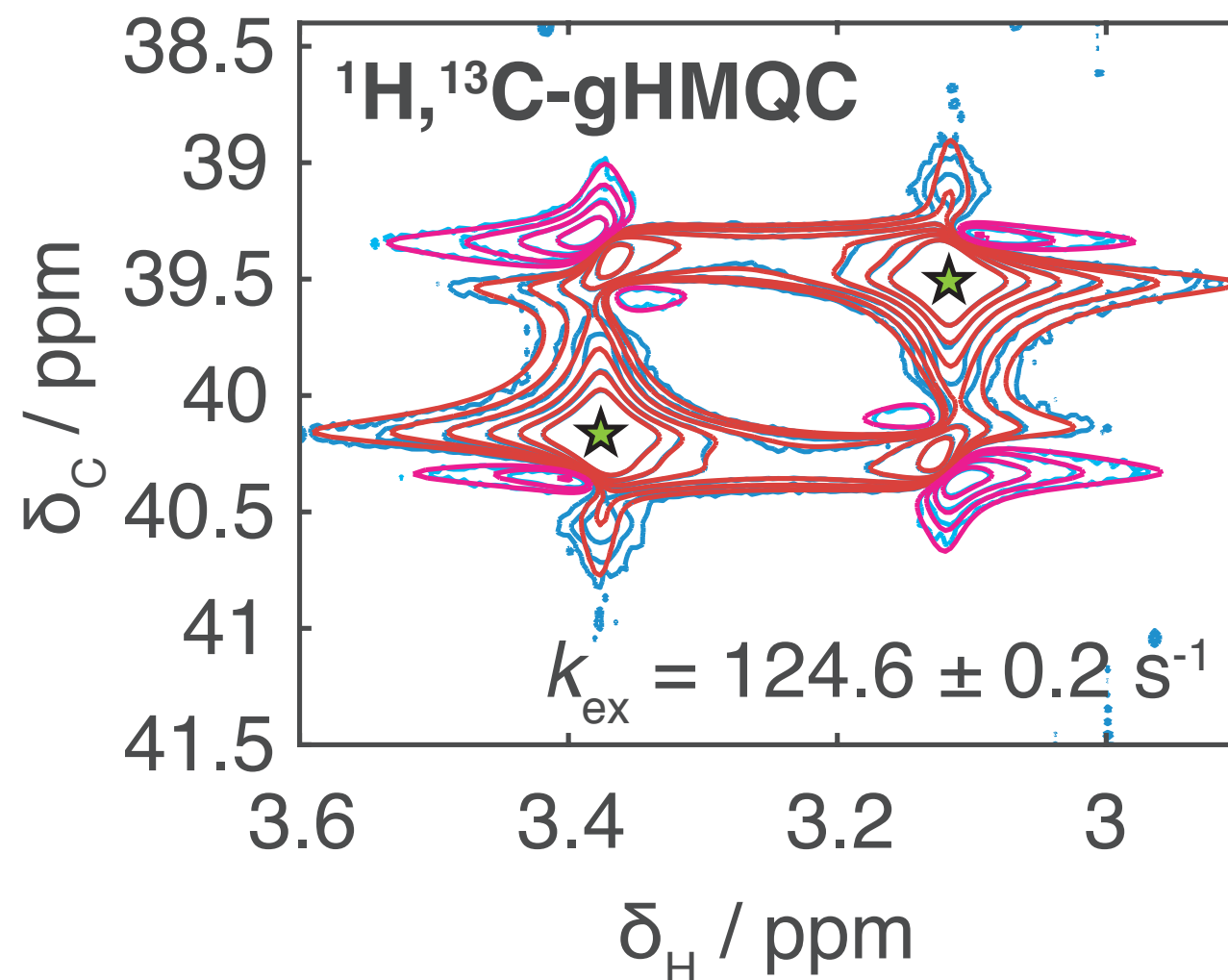
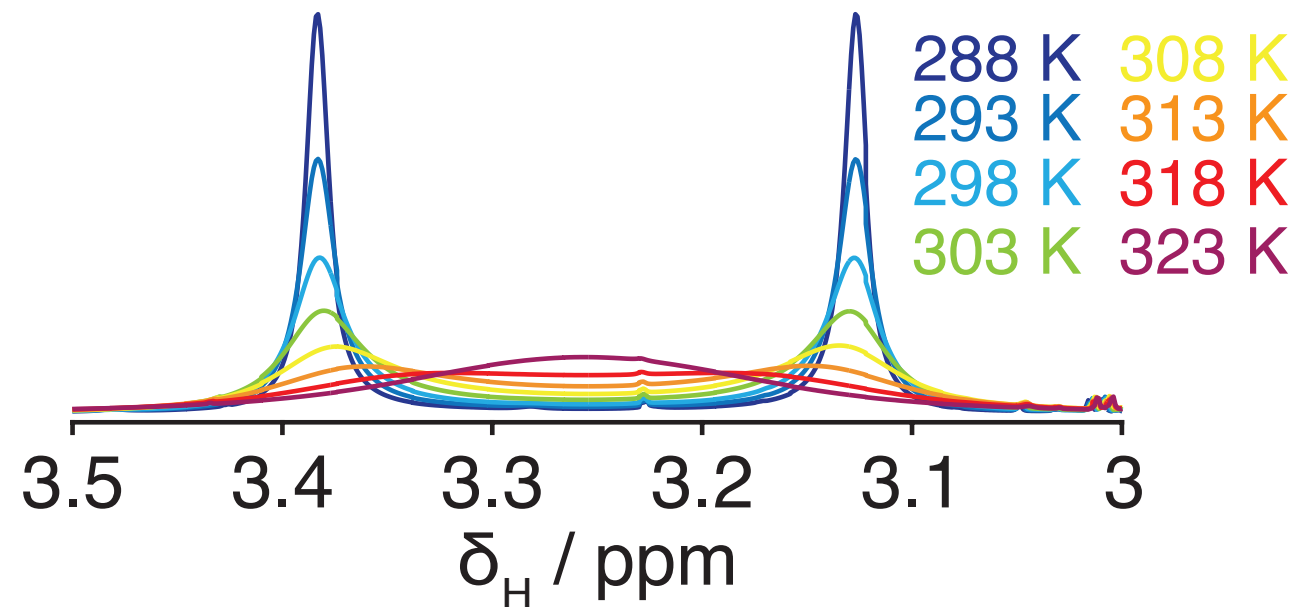
Exchange during INEPT coherence transfer periods



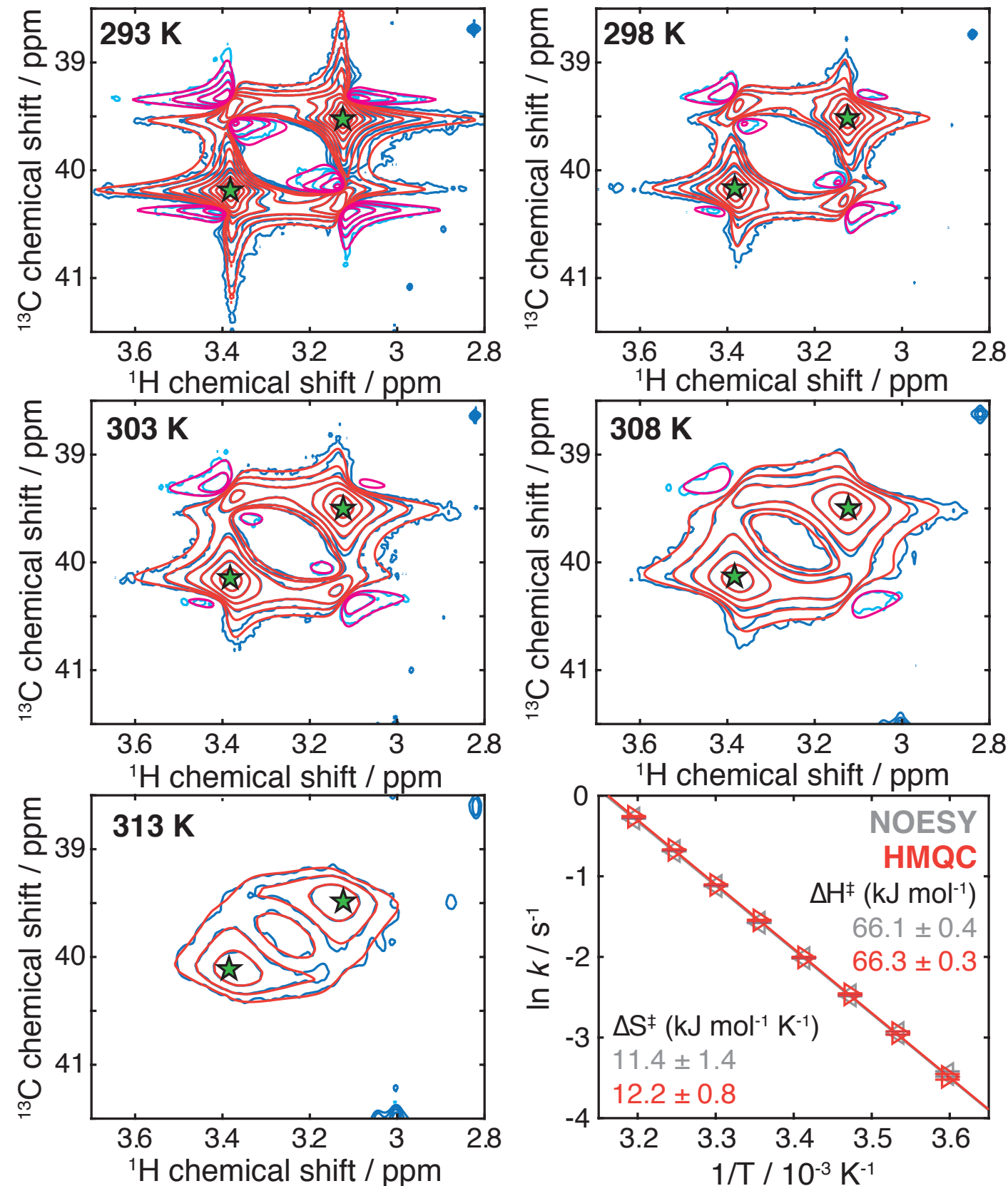
Unexpected exchange cross-peaks in 2D experiments



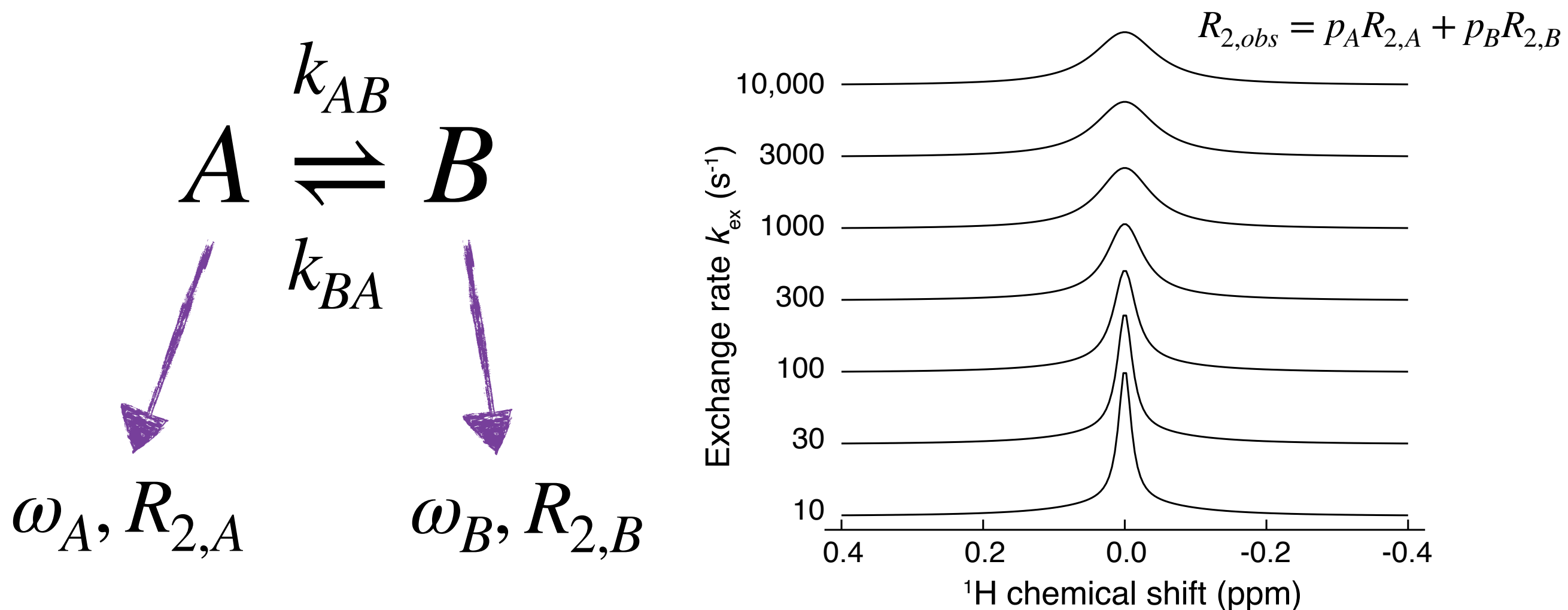
$$\begin{aligned}\Delta\delta_{\text{H}} &= 0.26 \text{ ppm} \\ \Delta\delta_{\text{C}} &= 0.62 \text{ ppm} \\ {}^1J_{\text{CH}} &= 140 \text{ Hz} \\ k_{\text{ex}} &= 125 \text{ s}^{-1} \\ &\quad (298 \text{ K})\end{aligned}$$



Unexpected exchange cross-peaks in 2D experiments



Exchange beyond the chemical shift: relaxation

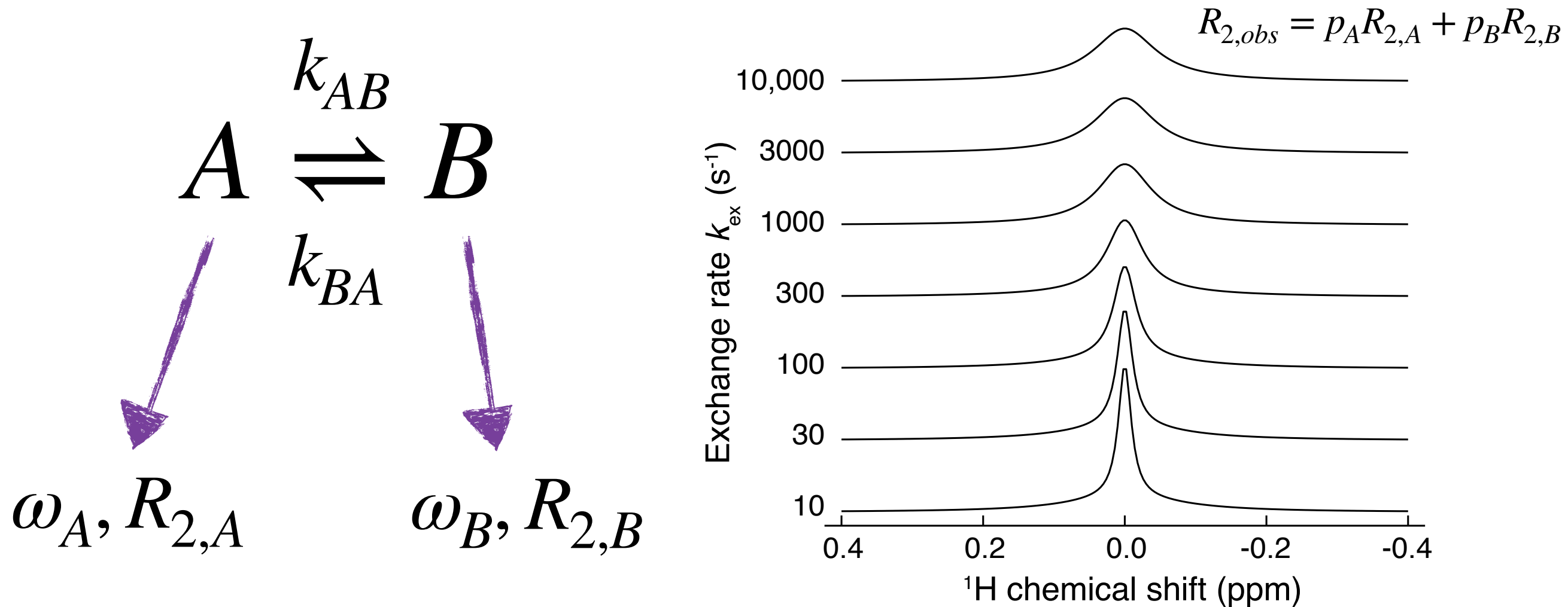


Chemical exchange effects can also arise between states that differ only in linewidth (R_2)

The observed spectrum will depend on the exchange rate relative to

$$\Delta R_2 = \left| R_{2,A} - R_{2,B} \right|$$

Exchange beyond the chemical shift: relaxation

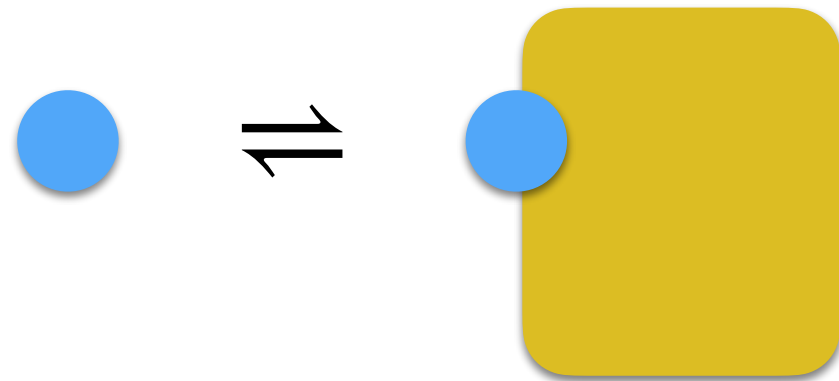


More generally, if both the frequency and linewidth change, the relevant quantity is:

$$|i\Delta\omega + \Delta R_2| = \sqrt{\Delta\omega^2 + \Delta R_2^2}$$

Exchange beyond the chemical shift: relaxation

Transferred relaxation through
ligand binding:

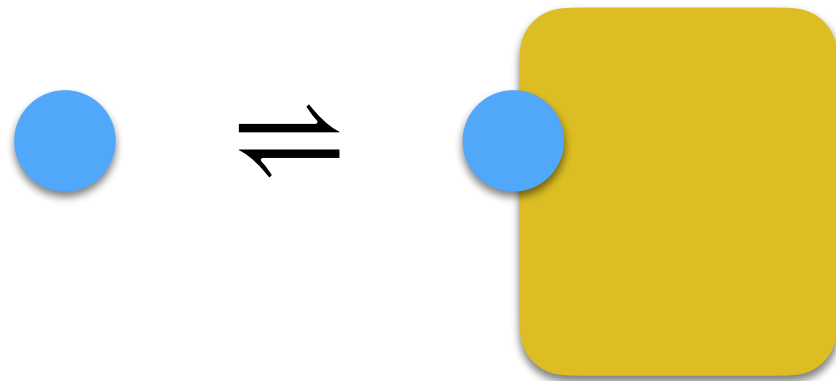


$$R_{2,obs} = p_A R_{2,A} + p_B R_{2,B}$$

If relaxation in the bound state is
rapid, even a small bound
population can have a large
effect on the appearance of the
free ligand

Exchange beyond the chemical shift: relaxation

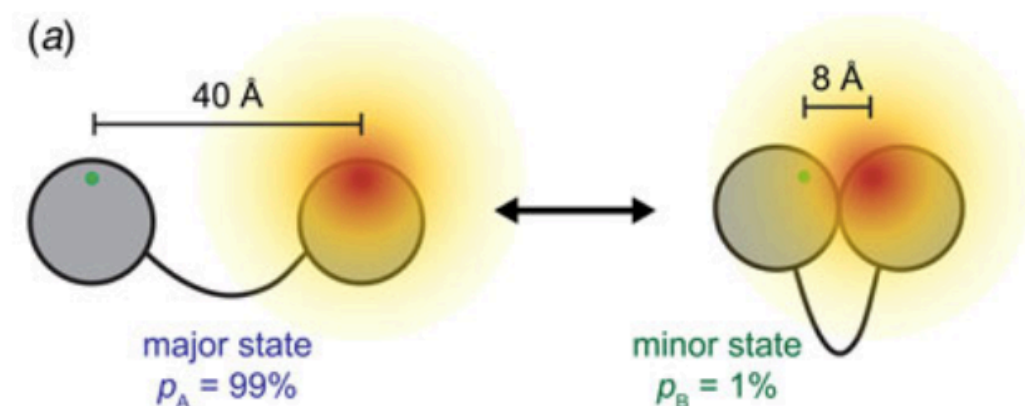
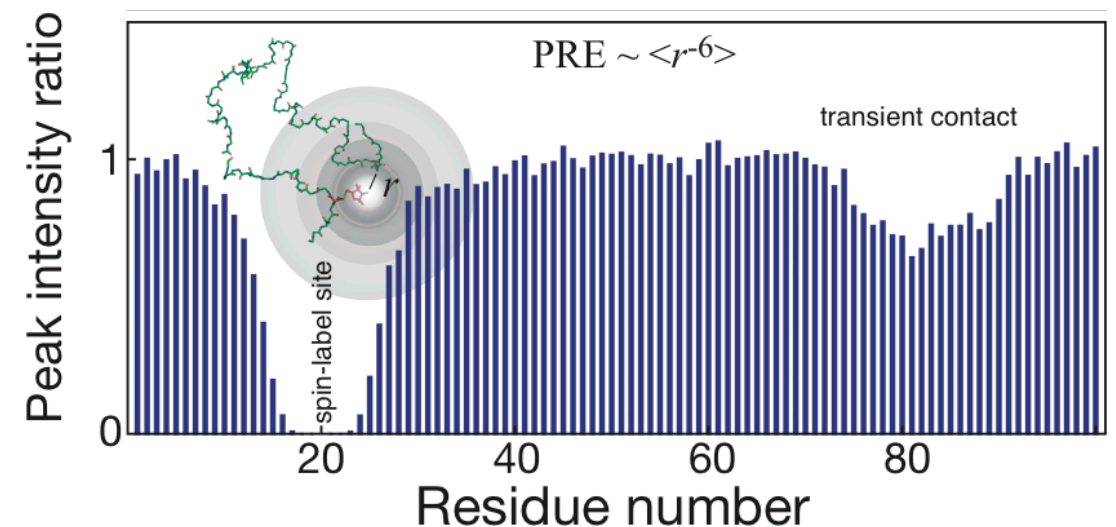
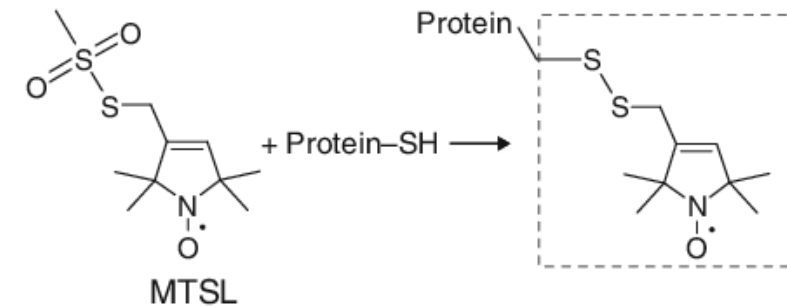
Transferred relaxation through ligand binding:



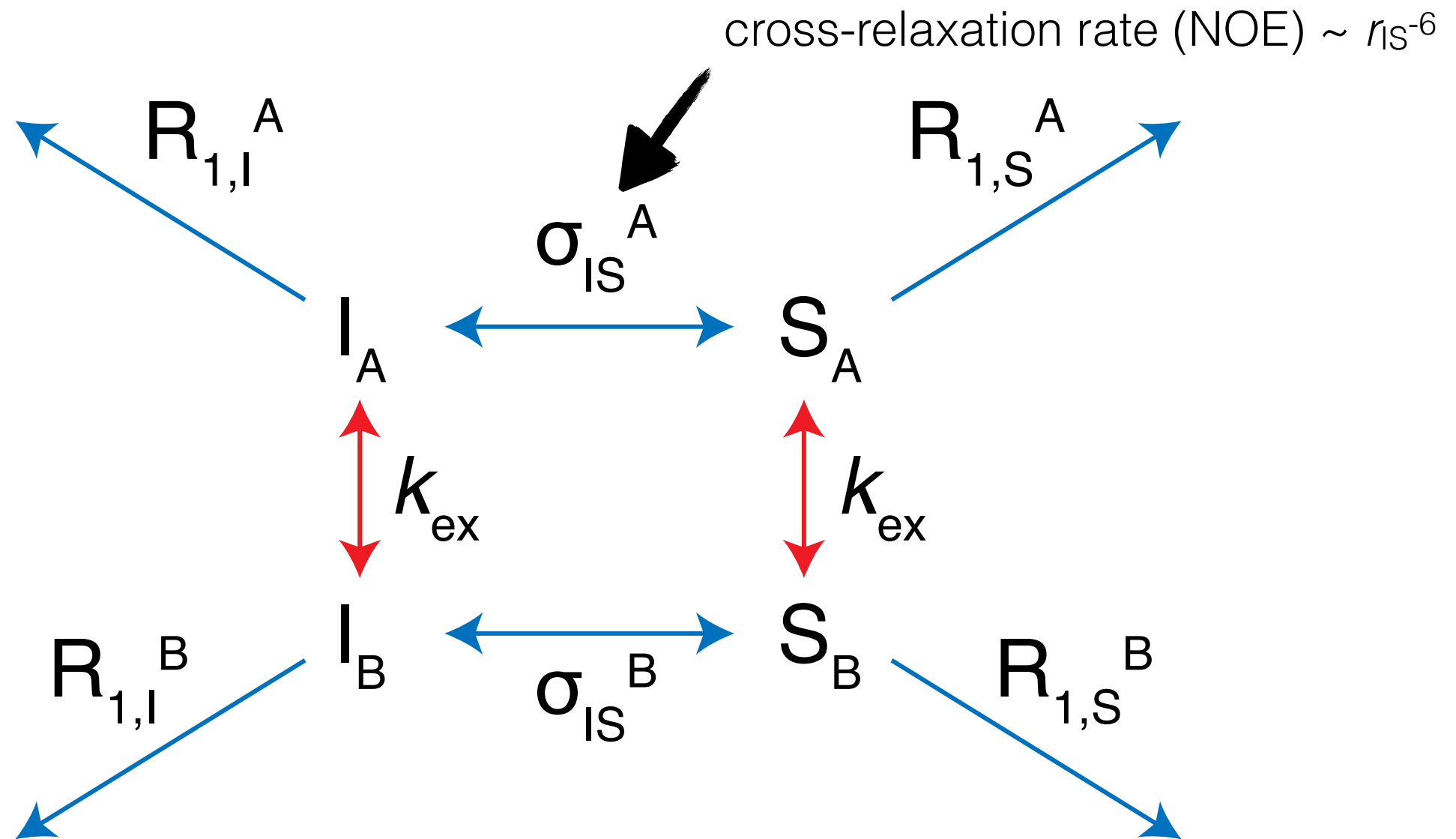
$$R_{2,obs} = p_A R_{2,A} + p_B R_{2,B}$$

If relaxation in the bound state is rapid, even a small bound population can have a large effect on the appearance of the free ligand

Paramagnetic relaxation enhancements (PREs):



Exchange beyond the chemical shift: cross-relaxation

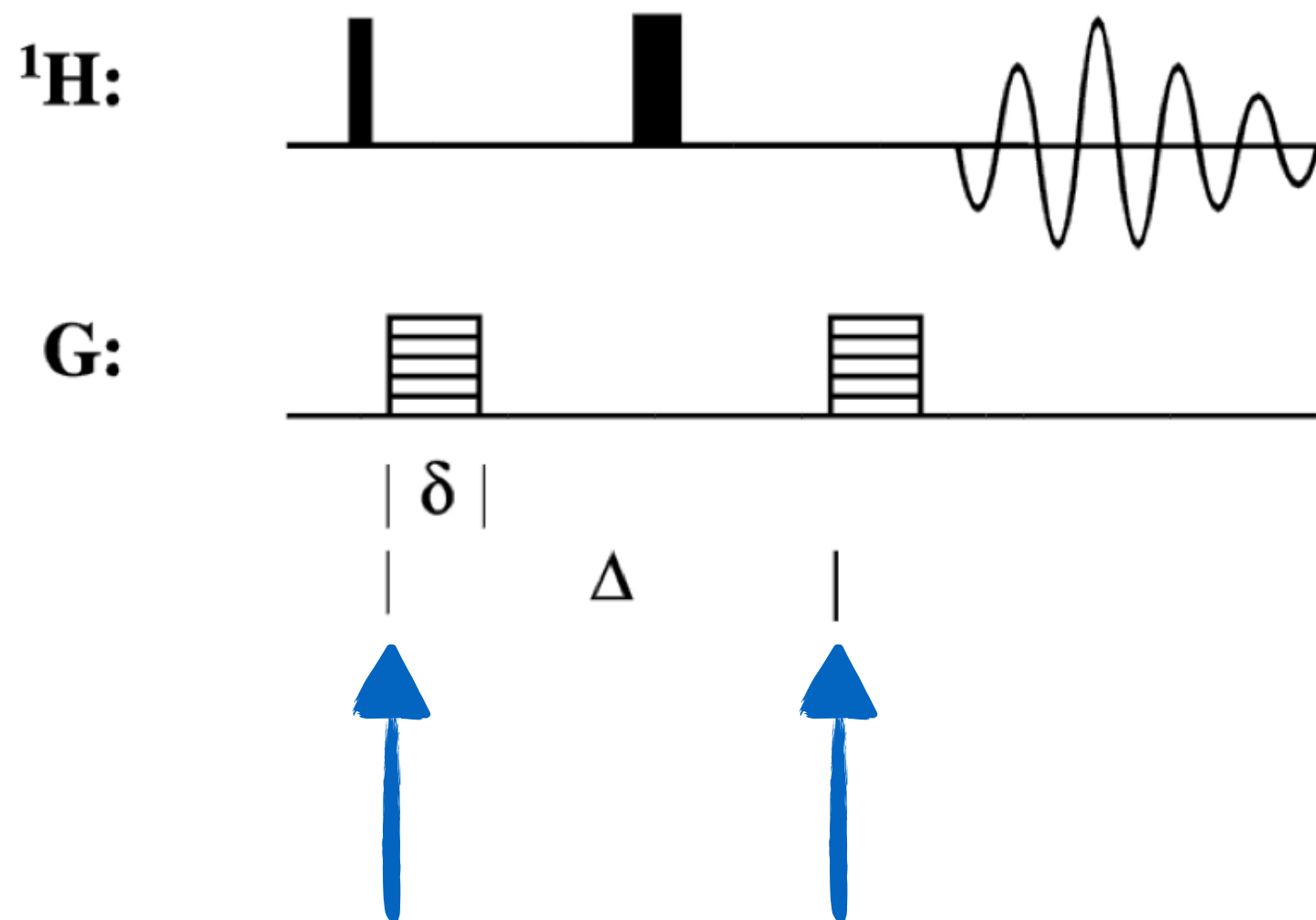


In fast exchange ($\Delta\sigma \ll k_{ex}$), a population-weighted average cross-relaxation rate is observed:

$$\sigma_{obs} = p_A \sigma_A + p_B \sigma_B$$

Exchange beyond the chemical shift: diffusion

Pulsed gradient spin echo experiment

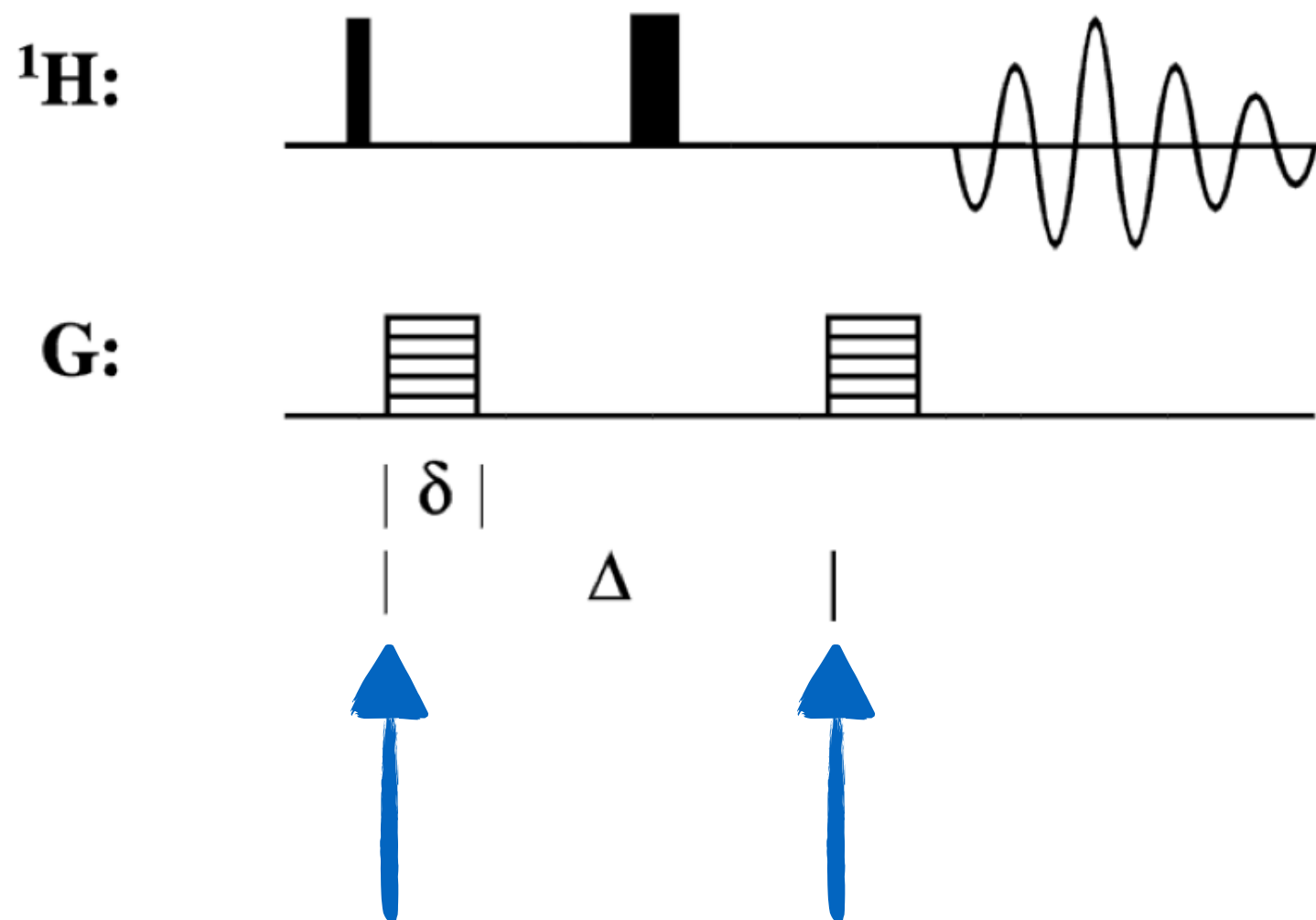


Pairs of gradient pulses encode and decode
the position of spins along the z axis

Diffusion during the intervening period, Δ , leads to a
loss of signal that can be analysed to measure the
diffusion coefficient

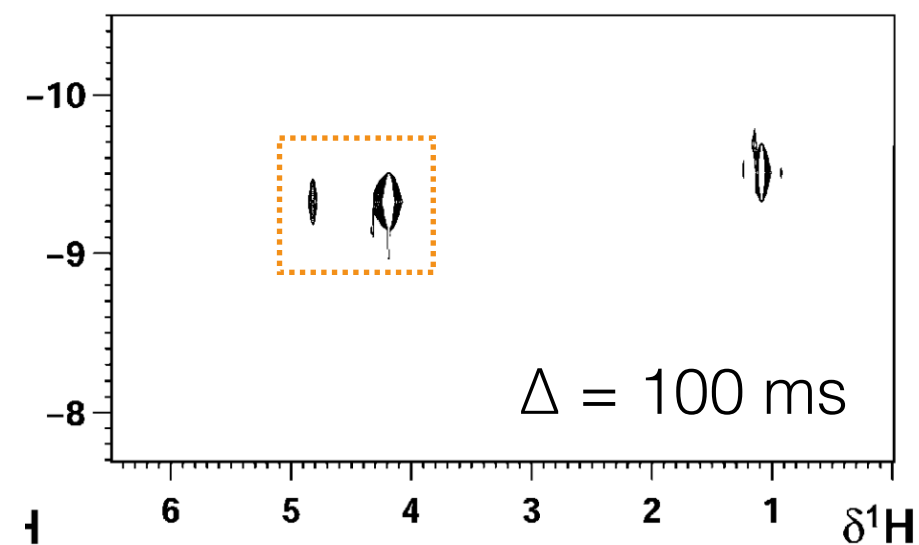
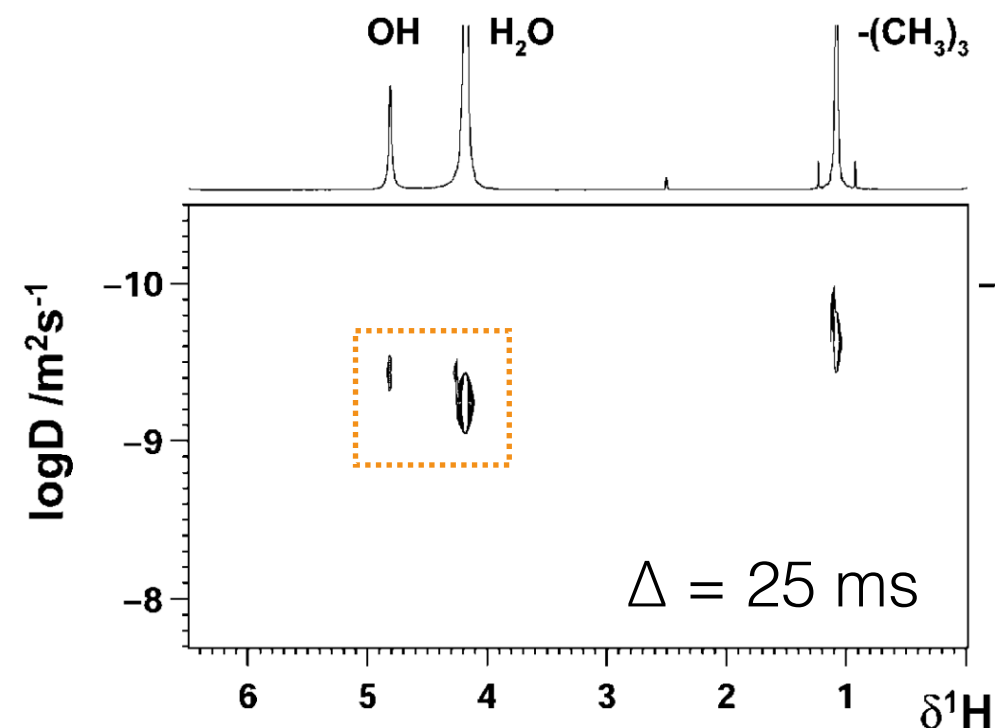
Exchange beyond the chemical shift: diffusion

Pulsed gradient spin echo experiment



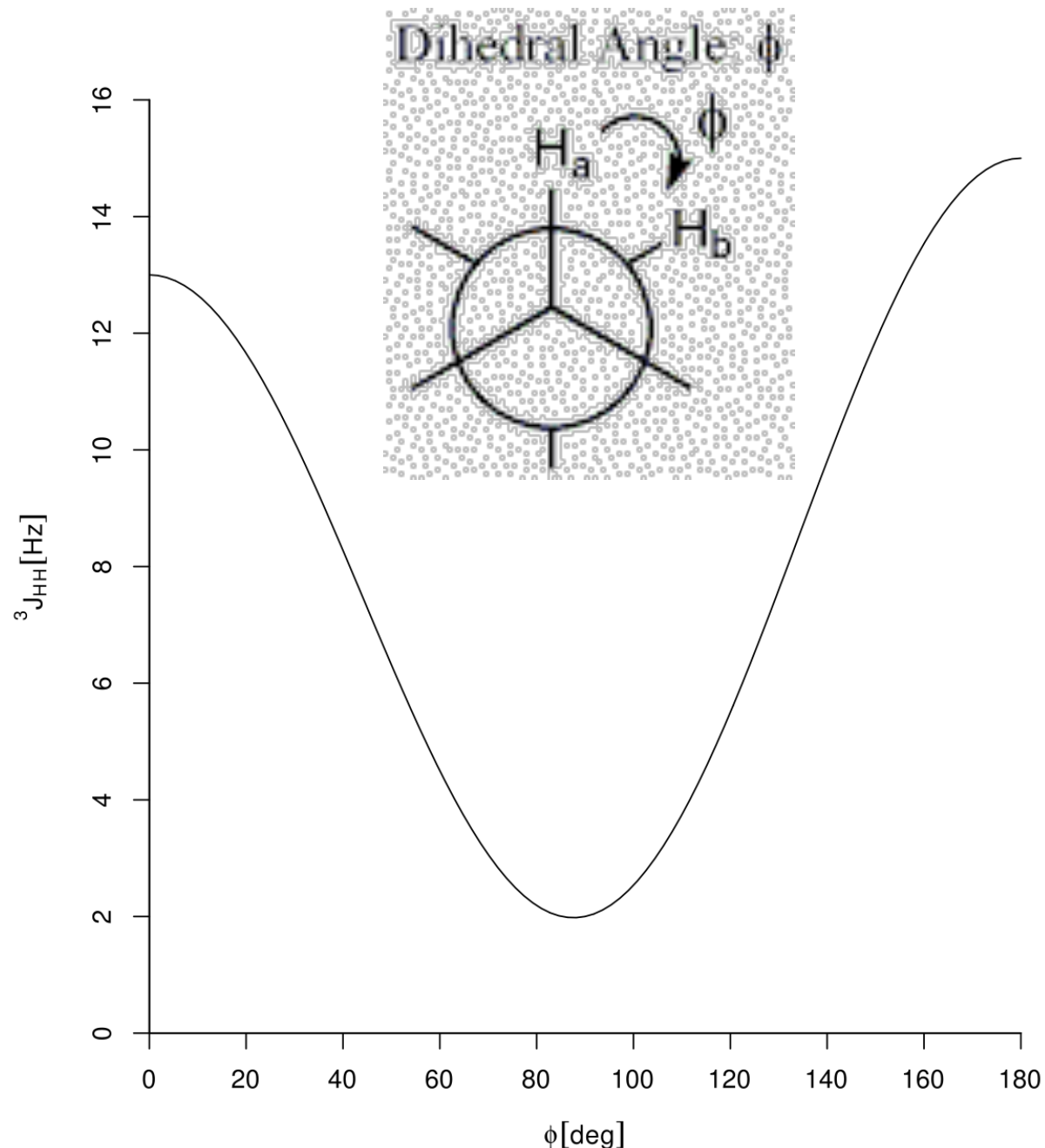
Pairs of gradient pulses encode and decode the position of spins along the z axis

Diffusion during the intervening period, Δ , leads to a loss of signal that can be analysed to measure the diffusion coefficient



Chemical exchange during Δ leads to averaging of the observed diffusion coefficient

Exchange beyond the chemical shift: scalar couplings



Karplus equation: $J = A \cos^2 \phi + B \cos \phi + C$

Intramolecular exchange
e.g. sidechain rotamers

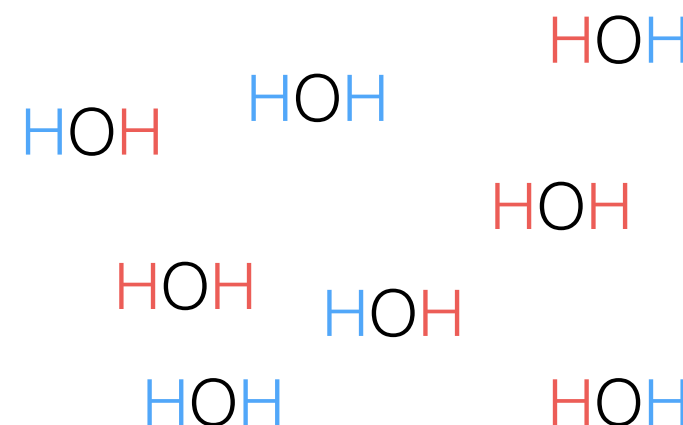
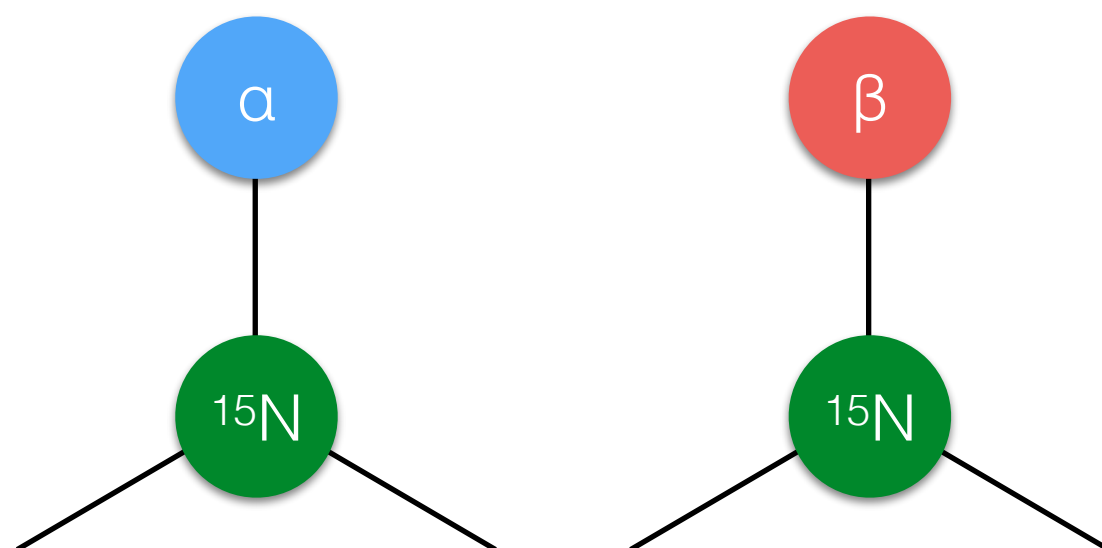
The dependence of the $^3J_{HH}$ scalar coupling on dihedral angle is described by a Karplus equation

Different rotamers will be associated with different coupling constants, but provided exchange between rotamers is rapid:

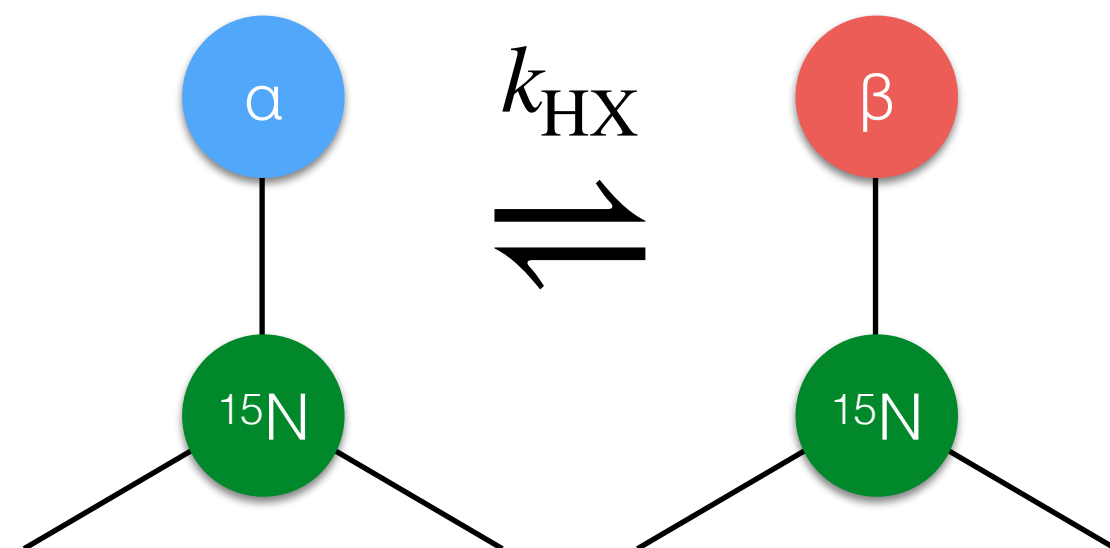
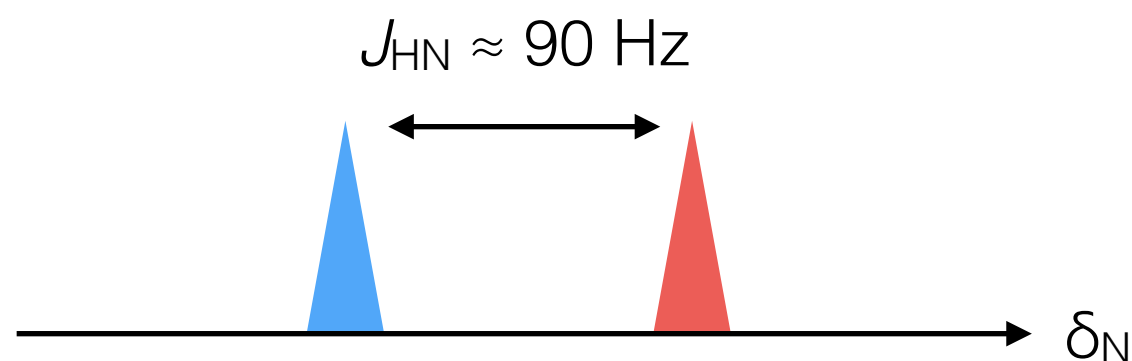
$$\Delta J \ll k_{\text{ex}}$$

then a single coupling constant will be observed corresponding to the population-weighted average

Scalar couplings and intermolecular exchange

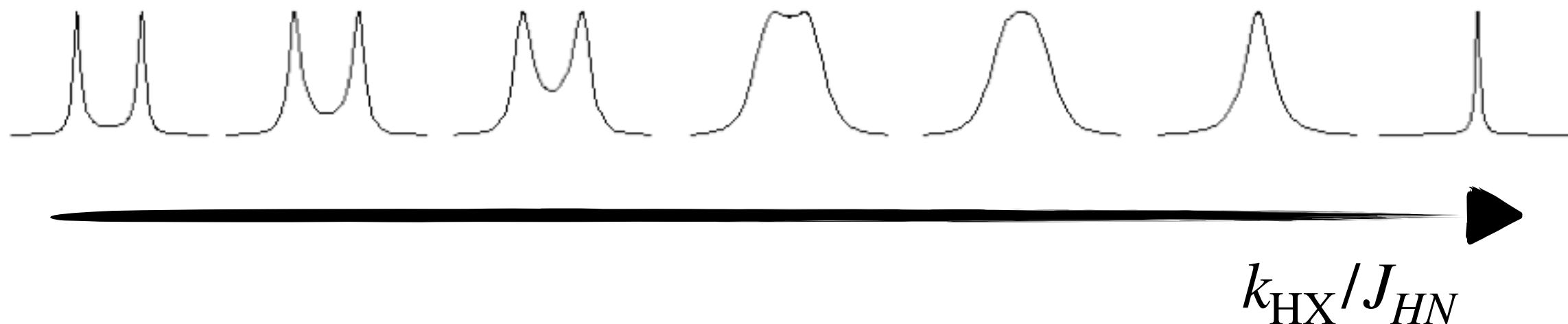
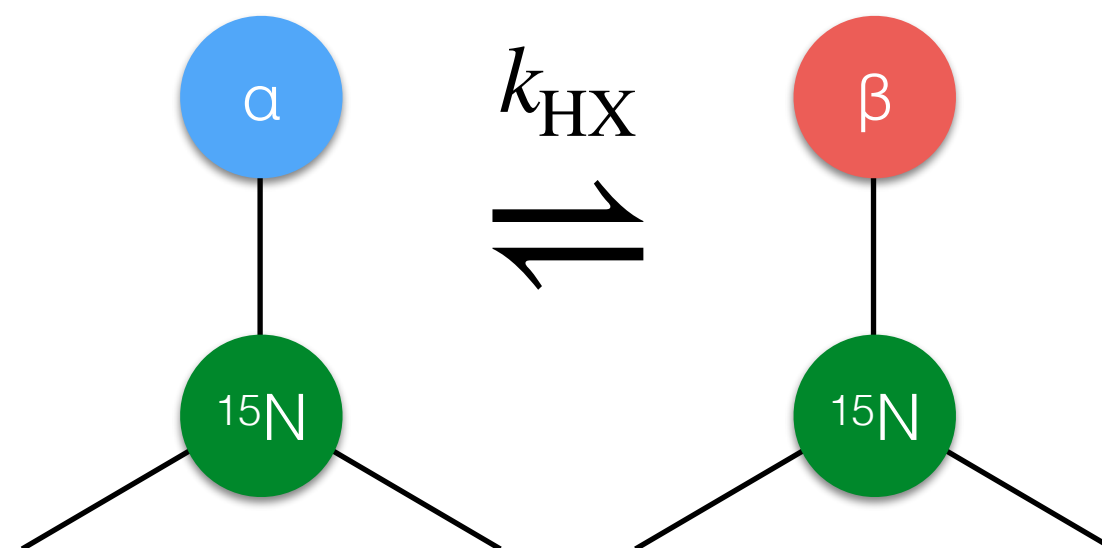
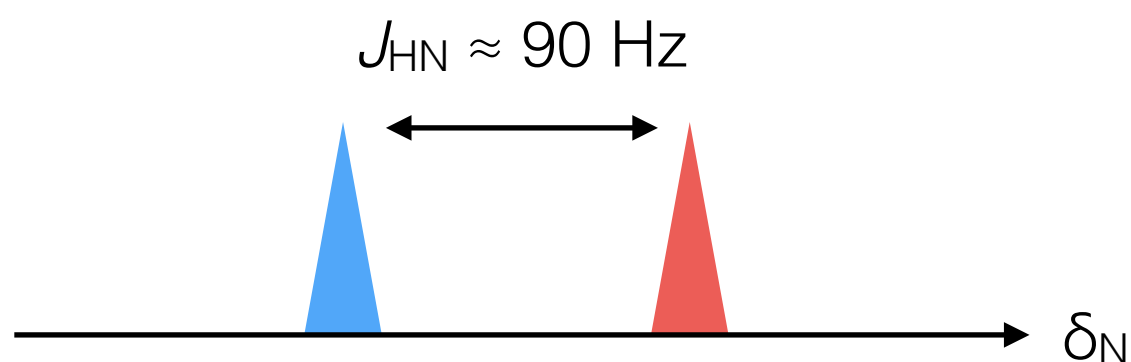


Chemical exchange of the coupled proton with the solvent randomises its spin state, which appears like exchange between α and β lines of doublet:



Scalar couplings and intermolecular exchange

Chemical exchange of the coupled proton with the solvent randomises its spin state, which appears like exchange between α and β lines of doublet:



NMR Sample Management

waudbylab.org/topspin-samples

crick-701/chris_HEWL_231009

Browse...

Go to current dataset

EMPTY

Last: lysozyme (2mM Gd)

Sample

- lysozyme
- lysozyme (1mM Gd)
- lysozyme (2mM Gd)

New...

Duplicate...

Edit

Mark as ejected

Delete

Settings...

Status: Found 11 samples in 1 directories

NMR Sample Manager (version ref: df31a15)

Sample Details

Timeline

Sample Catalogue

Search:

Refresh

Created	Experiment	Label	Components	Buffer
2025-03-24	danni_fragments_250324	test		
2023-10-09	chris_HEWL_231009	lysozyme	HEWL	10% D2O
2023-10-10	chris_HEWL_231009	lysozyme (1mM Gd)	HEWL, gadodiamide	10% D2O
2023-10-11	chris_HEWL_231009	lysozyme (2mM Gd)	HEWL, gadodiamide	10% D2O
2024-09-11	danni_nsp10_cnoesy_240911	13C Nsp10		
2025-10-13	chris_geoff_NG284_240422	test		HEPES, 10% D2O
2025-10-14	phay0029_compounds_251014	CH3-Trp	methyl-tryptophan	10% D2O
2025-10-20	phay0029_compounds_251014	Trp + BSA	BSA, Tryptophan	10% D2O
2025-10-16	phay0029_compounds_251014	Trp + methyl-Trp + ...	BSA	10% D2O
2025-10-16	phay0029_compounds_251014	Trp + methyl-Trp + B...	BSA	10% D2O
2025-10-16	phay0029_compounds_251014	Trp + methyl-Trp		10% D2O

View

Edit

Duplicate into current experiment

View on GitHub